

Nanosatellite Design with Design of Experiments, Optimization and Model Based Engineering

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by

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OPTIMIZATION AND MODEL BASED ENGINEERING**

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ABSTRACT

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Nano-satellite missions are an inexpensive tool used to perform scientific research functions and test new space technologies. From 2000 to 2016 there were 371 nanosatellite launches with 15.4% shown to complete their mission and another 22.6% which completed some aspect of their mission. The high failure rate of nano-satellites can be attributed to multiple factors such as system integration, non-space rated hardware, launch failure, and untested technology. By integrating design exploration, optimization and model-based system engineering techniques, some portion of nano-satellite risk may be mitigated.

This work presents a multi-disciplinary system exploration, design, and simulation approach for low-budget nano-satellite builders to get a better estimate of system performance before beginning the actual build. The use of design exploration minimizes the number of variables in optimization by finding which design variables have little options or impact on system performance and allows the design team to parameterize them. The system optimization process will give initial goals for the hardware mass, power and performance metrics which can then be simulated in a high-fidelity simulation to analyze mission and systems level requirements. This approach was implemented using a combination of open source tools and commercial programs. Open source packages such as pyOpt and OpenMDAO were used to perform design space exploration and multi-objective optimization. MatLabs Simulink was used as the model based engineering program as it provides a format which is readily available and familiar to students and engineering teams with little to no formal systems engineering background.

Design space exploration was performed by tools provided in the OpenMDAO package. Optimization was implemented by aggregating the constraints and objectives using the Kreisselmeier-Steinhaus method and using an unconstrained solver to minimize the envelope. The implementation of this algorithm was provided by the pyOpt package.

The current level for the models for each system is currently in an early development stage which should be used with caution for actual system engineering. However this proposed approach can be easily expanded with higher-fidelity models, design equations, and parameterization based off of historical data which will result in an initial starting point for nano-satellite build teams who can then make design decisions based off of currently available technology, time and monetary constraints.

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Nomenclature

\circ_k	Pointing knowledge of star tracker
ΔV	Change in velocity (impulse measurement)
λ	Transmitted signal wavelength (m)
λ_{max}	Maximum earth central angle (rad)
λ_{min}	Minimum earth central angle (rad)
μ	Standard Gravitational Parameter times the mass of the planet
ω	Argument of Periapsis
Ω	Longitude of the ascending node
${}^A\omega^B$	Angular velocity of reference frame B in reference frame A
Φ	Gravitational Potential Function
ρ	Density, angular radius
θ	True anomaly
\mathbf{a}	Acceleration
A	Cross sectional area
a	Semi-major axis for elliptical orbit
BER	Bit error rate
C	Received power (W)
c	Speed of light in vacuum
C_D	Coefficient of drag
D	Data total (bit), or spacecraft residual dipole
e	Orbit eccentricity
E_b	Received energy per bit (W)
$EIRP$	Effective isotropic radiated power (W)
\mathbf{F}_i	Force of i

F	Fractional reduction in viewing time (Dimensionless between [0 and 1])
G	Gravitational Constant
G_r	Receiver gain (dB)
G_t	Transmitter gain (dB)
H_{max}	Maximum angular momentum capacity of wheel
i	Orbit inclination or incidence angle (context sensitive)
I_{sp}	Specific Impulse
$IF\,OV$	Instantaneous field of view (one pixel)
IPS	Instructions per second
J_n	Geopotential coefficient
k	Boltzmann's constant ($1.38064852 \times 10^{-23} m^2 kg s^{-2} K^{-1}$)
L_a	Transmission path loss (dB)
L_l	Transmitter to antenna line loss (dB)
L_s	Space loss (dB)
M	Margin required to account for missed passes between [2,3]
M_e	Magnetic moment of earth ($7.96e15 Tesla \cdot m^3$)
m_i	Mass of object i
$\dot{\mathbf{n}}$	Time derivative of vector \mathbf{n}
$\ddot{\mathbf{n}}$	Second time derivative of vector \mathbf{n}
N_o	Noise density (W)
P	Transmitter power (W)
P_{EOL}	Power at end of life
P_{SA}	Power of solar array
q	Reflectance factor
\mathbf{r}_{ba}	Vector distance from object a to b, same as ${}^a\mathbf{r}^b$

R	Data rate (bits/s)
R_E	Mean radius of the earth
R_r	Effective radius of isotropic transmitting aperture (m)
$SLOC$	Source line of code
T_{init}	Time required to initiate communications pass (s), suggested to be two minutes
T_{max}	Maximum time in view (s)
T_i	Torque
T_s	System noise temperature (K)
V_g	Ground velocity
W_f	Power flux density (W/m^2)
X_i	Power system efficiency

Chapter 1

INTRODUCTION

The following chapter will focus on the motivation for developing and extending current modular and open architecture systems and their supporting technologies and methods. The models for a space plug and play system are focused on standardizing a set of self-describing frameworks and interfaces for each subsystem such that system integration requires very little input from the system integrator. This project is a focus on mission development using a generalized model, and incorporating a modular redundancy system as a new system feature for plug-and-play satellites.

1.1 Motivation

Plug and play (PNP) technology and scalable modular/open architectures expand the operational capabilities for satellites and provide a means of risk mitigation for missions. From an operational standpoint a plug and play system will minimize the time necessary to integrate a system which will directly lead to rapid launch capabilities. In addition the ability to swap parts in orbit with on-board reserves or through a servicing platform will help reduce the chance of complete loss of a system. An open-architecture (OA) model will provide a framework based on plug and play concepts in order provide modular redundancy, rapid deployment of satellites, in flight servicing capability, as well as provide a new method for risk management.

1.1.1 Problem at hand

The two issues which encumbers rapid satellite development and launch are system integration errors and the risk mitigation techniques. The risk mitigation techniques are required to ensure a functional satellite will be delivered to the customer and operate in orbit, as such removing them from the development cycle is not possible. In order to reduce time in the development phase the issues encountered by system integration must be relieved. Adopting an OA/PNP system can minimize the time spent on both of these issues by providing a standard set of modular redundancy protocols, inter-system communication frameworks, mechanical subsystem module connection interfaces, and a common flight software package. Significant work has been done in developing system architecture standards and flight software framework already. The focus for this study is to investigate modular redundancy advancements for mission development. One such advancement is the incorporation of radiation tolerance methods as a new feature for the OA/PNP system models. The use of radiation tolerant methods combined with commercial off the shelf (COTS) hardware will minimize the cost of nano-satellites and lead times, this is significant due to the fact that many nano-satellites are developed by universities and budget constrained research teams. Minimizing time and cost will provide greater access for universities and research teams access to space exploration and research projects.

1.1.2 Why investigate problem

With the expansion of commercial and government endeavors in space, there will be an evolving role to provide servicing requests to prevent the loss of satellite assets. While possible the servicing of satellites are still costly and designing a

system which can recover in the event of a subsystem failure should be considered first. Conventional life cycles for satellites typically occur in the time frame of up to 15 years from concept to launch and last for roughly about the same time in orbit[1]. For nano-satellites there is an even more dangerous gap over a year of development and less than a year for flight [2]. Often times these systems are custom made to order in cleanroom environments and vigorously tested at component, subsystem, and system levels. While the manufacturing process and rigorous testing is necessary to provide functional satellites, it prevents quick turnaround times for commercial, scientific and defense purposes. The most common commercial satellite bus is the SSL-1300 platform which first flew in 1989 and averages about six launches per year [3]. Despite the flight heritage and expertise that was gained from years of working with the spacecraft bus it still difficult to interface the mission payloads to the existing spacecraft bus. A modular OA/PNP system incorporating n-modular redundancy will provide one method for minimizing time in the design-build-fly cycles, while simultaneously providing easier servicing of satellites. In the past servicing of satellites was provided by the space shuttle program as part of its normal operation profile [4]. With the ending of the current space shuttle program, there is very little that can be done to recover and repair satellites that are failing in orbit. With the use of modular PNP systems in flight repairs of satellites which have been damaged during operation can be repaired more easily and possibly autonomously via nano-satellites, removing the need to have a crew intercept and provide manual integration and configuration to a satellite. Another advantage of OA/PNP system is to provide rapid launch capabilities. The U.S. Department of Defense (DoD) created the Operationally Response Space (OSR) unit to focus on rapid deployment space systems to support DoD operations. In conjunction with the Air Force Research Laboratory (AFRL) the OSR developed the Space Plug and

Play Architecture (SPA) in pursuit of a six day design-build-fly cycle [5]. Over the next ten years NASA, OSR, and AFRL worked on the improving the avionics standard and developed a variety of demonstrations such as the Modular Space Vehicle, TacSat3, adaptive wiring harnesses and components of TechEd Sat proving the viability of the OA/PNP system [5]. While many demonstrations missions have proven the viability of the OA/PNP concept there is still significant advancement necessary to enable the full benefits of the architecture.

1.2 Literature Review

The following section will cover some of the existing work related to spacecraft OA/PNP technologies, advances in technologies and methods, tolerance methods, as well as some companies which have developed intellectual property which support the OA/PNP model. Hardware adaptability is significant for this n-modular redundancy as such the use of FPGAs will be of interest as well.

1.2.1 FPGAs

Field programmable gate arrays (FPGAs) are the cornerstone of true system redundancy due to their ability to change functionality during normal and recovery operation modes. The ability for FPGAs to process large data streams in parallel also help alleviate the down-link budget. By providing more on-board processing for large data streams such as video and hyper-spectral imaging, the total data stream to the ground station is reduced [6]. While there are radiation hardened FPGAs they typically do not have the same performance as their terrestrial counterparts and have a higher end cost for the system developers [6]. FPGAs use a technique called scrubbing to effectively rewrite the FPGA code in whole or partially as a way to deal with environmental caused error. While effective in countering single event

upsets (SEU), it cannot prevent latch ups or more physically damaging faults. Work done by Hane and Buerkle have shown that the use of radiation sensors in conjunction with multiple FPGAs can improve robustness for SEUs by up to ten times even in severe solar flares[7]. However there have been other studies which show that after the first spare, there are significant diminishing returns. The optimal situation for low earth orbits is enabling TMR with scrubbing using an additional spare which has a short activation time than the repair time of the original upset FPGA [8]. Other advancements in space based FPGA programming can be found in dynamic fault tolerance. FPGAs utilizing triple modular redundancy (TMR) can see system resources increase by over two times, this expands out significantly as you increase the number of modular redundancy systems. Jacobs et. al have found that implementing a reconfigurable fault tolerant framework provides over double the performance in low radiation environments over traditional TMR systems.

1.2.2 N-Modular Redundancy and Supporting Technologies

N-modular redundancy (NMR) is a significant topic for long-life missions as well as nano-satellite COTS bus systems. For deep space missions the ability for a spacecraft to make simply arrive to its mission location in an operating form is as challenge in itself. As a result many of these missions use custom spacecraft systems which are focused on robust operation instead of performance [9]. However robust systems which utilize NMR result in high power draw. On the other hand many nano-satellites utilize COTS systems which may not have significant fault tolerance by creating a NMR interface between the hardware and the rest of the system survival can be increased.

NMR is a methodology which provides fault masking as long as half plus one modules are operating correctly. Due to the module requirement however this is a

resource intensive method which imposes significant power constraints for both FPGA and multi-core processing units. For satellites which implement higher than TMR tolerance schemes, power draw becomes a significant issue for thermal and computational resource management. One method of countering this is an online/offline energy management system. In this process half of the tasks are computed and compared by the voters. If all results are within tolerance of each other, then the second phase does not occur. If there is a distinction between various outputs, then a second cycle computes the other half of the tasked process and compares them [10]. Combining this method with the dynamic tolerance scheme can provide a significant increase in system resource reserves and minimize power draw. This is a significant advantage for deep space missions when extra power is required for communication and system life support.

Another fault recognition framework was developed which also takes into account mission objectives and policy requirements [11]. In this approach an adaptive decision process was created which balances bus safety and mission objectives as potential for handling detected faults and determining the best course of action. This process provides the option for spacecraft to delay in flight reconfiguration if there is an achievable mission objective which will not affect the long term health of the spacecraft, promoting autonomous decision making which is necessary for periods when the satellite is out of communication with ground networks.

Traditionally functions for a spacecraft have been passed down to specific subsystems and rarely have the ability to overlap due to size, weight and power requirements. A vector modeling approach of modularity mapping has been proposed which allows the mission designers to implement a satellite which provides little overlap of system function, or multiple levels of redundancy through the use of

modular systems which can contain various functions [2]. In either case, the ability for the system as a whole to recover from failure remains a necessity. While micro-controllers and processors have very little ability to recover without a system restart, FPGAs have the ability to reconfigure in flight. This unique feature allows the use of subsystems to recover in the event of SEUs. For this reason FPGAs are used for core system functions, health checks and with the addition of TMR and scrubbing are used for full system recovery operating modes. Another event in the case of subsystem controller failure is the use of a secondary FPGA taking over the unusable FPGA. This can be done by use of a linear bus which uses a data bus structure which allows all distributed FPGAs communicate with all other hardware when necessary [12]. Previous attempts at this has been seen with the development of the X2000 at NASAs Jet Propulsion Lab. In the work done on the X2000 multiple levels of hardware and software fault protection implications were developed to integrate COTS into use for deep space missions. The X2000 team found that by implementing multiple levels of redundancy they were able to get comparable fault protection as specifically design hardware [9].

Another supporting technology was developed in conjunction with the SPA standard. Murray et. al developed an adaptive wiring manifold which replaced the custom wiring harness used for connecting satellites [13]. The design of these wiring panels provided a scalable interface which provided a way to connect arbitrary modules as well as provide a switchable pathway between them. This concept allows the ability to switch between failing hardware and potential reserves in flight. The second is the ability to add on additional hardware in flight. Combined with a self-describing framework this can provide true plug-and-play functionality.

1.2.3 Standardization

There have been two significant advances for the OA/PNP model since the early 2000s. The first is the introduction of the SPA developed by the AFRL and OSR, and the release of the NASA core Flight Executive (cFE). Both of these provide frameworks for the core mission software, firmware, and the hardware interfaces. The SPA standard has further developed into the modular open network architecture (MONARCH) which provided a scaled framework for large satellites over 1000 kg [14]. While many communication protocols have been standardized, there is still some room left for the engineers to design the system for minimizing negative performance interactions. The purpose of MONARCH was to compile the engineering efforts into a best-practice, and further specify the interfacing protocols. This removed work which would be lost on a system to system basis. It also further enhanced SPAs self-description and specification of data.

The second framework is the Goddard cFE. NASA Goddard Space Flight Center developed the framework as a way to reduce their internal development timelines and reduce mission cost. The software framework provides a majority of the necessary functions for the command and data handling (C&DH) subsystem and interfaces with various real time operating systems [15]. The cFE package is a scalable flight qualified software environment which is used for flight as well as ground testing and mission simulation. The release to the general public for this software reduces the amount of the custom flight software which is required for the system designers, leading to reduced development cycle time [15].

1.2.4 Companies

Several companies have also begun implementing modular systems which are semi-open modules which can interface more readily with other systems. One such system is the Space Information Laboratories (SIL) Intelli-Avionics system [16]. This system is designed around minimizing the number system black boxes as a way to minimize overall system cost. The integration of similar systems into full system on modules reduces the complexity of dealing with multiple different hardware frameworks as well as having a single point of contact for a set of sub functions.

Similarly some companies are providing full turnkey platforms such as the Clyde Space CubeSat platforms [17]. By providing the interface requirements a customer can design and build a singular payload and integrate it into a fulling functional bus. Although it provides a convenient package it is not a one-size fits all open framework which can be modified by the customer.

WIP Some material is protected by NDA, working on what can still be shared.

1.3 Proposal

The purpose of this project is to develop a baseline nanosatellite design using design space exploration, optimization methods, and analysis using models in a simulation environment.

1.4 Methodologies

The general method for this project is as follows:

- Choose a set of nano-satellite missions and identify a bound of system and subsystem requirements based on common mission parameters.

- Using analytical design equations and estimations, coupled with regression of current hardware develop a sizing model for each core subsystem
- Perform a factorial analysis on the tradespace of each subsystem to define the key performance drivers.
- Optimize and simulation the design to perform a first order analysis of the feasibility of design capabilities.

Chapter 2

SPACE MISSION BACKGROUND THEORY

This chapter will overview the core concepts of the theory necessary to understand, simulate, and implement a general model for a nano-satellite. By generating a nano-satellite model, it is possible to develop a computational test-bench for emerging technologies and methods for use in space missions. This section will briefly overview the critical components necessary to generate the nano-satellite mission model, including the following modules:

- (1) Orbit Mechanics and Numerical Techniques
- (2) Space Environment Forces and Effects
- (3) Subsystem Functionality
- (4) Design Space Exploration

2.1 Orbital Mechanics and Numerical Techniques

In order to determine the environmental influences which would act as inputs to the general nano-satellite model, it is first necessary to determine the position in space that spacecraft is in. In order to determine the position and attitude, a simulation module will need to be constructed which provides accurate time, space, and orientation parameters. For conciseness only the general mechanics equations and numerical techniques will be dealt with in this section. Specific maneuver details and methods used for designing and analyzing missions are described in Appendix A to maintain focus on the governing mechanics for orbital mechanics.

2.1.1 Orbital Mechanics

There are three fundamental laws which describe the motion of planets around the Sun. The first two laws were discovered by Johannes Kepler 1609 and the third by Kepler again in 1619. They are as follows [18]:

- (1) The orbit of a planet is an ellipse with the Sun as its focus.
- (2) The line joining the planet to the sun sweeps out equal areas in equal time.
- (3) The square of the period of a planet is proportional to the cube of its mean distance from the sun.

To describe the orbit shape and orientation the use of six Keplerian elements is needed. Keplerian elements are typically given to describe the shape of the orbiting body and include the eccentricity, semi-major axis, inclination, longitude of ascending node, argument of periapsis, and true anomaly.

- Eccentricity e is derived from the mathematical property of conic sections. Eccentricities from zero to less than one are ellipses. An eccentricity of one indicates a parabola, while anything higher than one is a hyperbolic conic section. The shape of the conic section defines the shape of the orbit.
- The semi major axis a is the length between the apoapsis and periapsis of the ellipse.
- Inclination i is the experienced tilt of the orbit plane about the ascending node with respect to the main body plane of reference.
- Longitude of the ascending node Ω orients the ascending node of the ellipse to where the orbit passes upwards through the reference plane. It is referenced against the vernal point of the main body.

- The argument of periapsis ω aligns the periapsis with respect to the ascending node of the orbit.
- True anomaly θ shows the angular position from periapsis of the orbiting body on the ellipse.

The elements are shown in figure 2.1. These elements can be mapped to the Cartesian grid and from the Cartesian grid to the Keplerian elements as shown in appendix A.

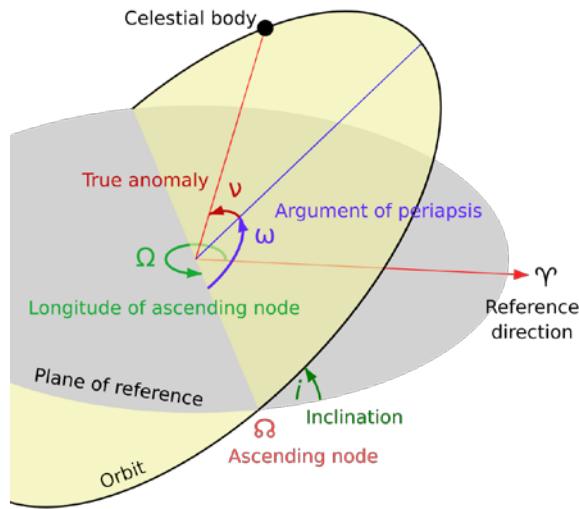


Figure 2.1: Keplerian Elements from Lasunncy / Wikimedia Commons CC-BY-SA-3.0

Using Newton's second law we can find the acceleration of the satellite in the reference inertial frame. There are a variety of forces which act on the satellite at any given time, however the focus of the gravitational forces will be discussed here. Perturbations such as thrust burns, atmospheric drag, solar pressure, and non-idealized gravity will be discussed in section 2.2. Assuming the satellite as a point mass we can separate the general equation of the satellite into the following

equation.

$$\mathbf{F}_{\text{total}} = m_{sc} \mathbf{a}_{sc} \quad (2.1)$$

Due to the large impact of the gravitational force on the orbit compared to all others, the total force will be separated into $\mathbf{F}_{\text{grav}} + \mathbf{F}_{\text{other}}$. Equation 2.1 can also be rewritten more generally for any body in the reference frame. The general form of the equation is useful as it improves the accuracy of your spacecraft position due to taking into account changing mass.

$$\ddot{\mathbf{r}}_i = \frac{\mathbf{F}_{\text{tot}}}{m_i} - \dot{\mathbf{r}}_i \frac{\dot{m}_i}{m_i} \quad (2.2)$$

To find the gravitational force of all bodies on the spacecraft the following equation is used.

$$\mathbf{F}_g = -Gm^i \sum_{j=1, j \neq i}^n \frac{m_j}{r_{ji}^3} (\mathbf{r}_{ji}) \quad (2.3)$$

By neglecting non-gravitational forces and combining equations 2.2 and 2.3, a general orbit path can be found. As the mission design moves further into completion, higher fidelity can be found by adding in the necessary perturbations and expanding the number of bodies in the reference system. For the initial iteration of the orbit propagation multiple assumptions were made, these include:

- Only two bodies are involved in the problem.
- There are no significant forces on the spacecraft outside of gravity.
- All bodies are rigid and have a point mass at the center of gravity of the object.
- All burns (ΔV) are instantaneous and do not significantly change the mass of the spacecraft.

Further iterations will improve the fidelity of the model to include other perturbations such as multiple bodies, propulsive burns, drag, solar pressure, non-spherical gravity, and other significant environmental factors.

2.1.2 Reference Frames

Due to the complexity of the spacecraft dynamics it is important to define which reference frame we are working in and how they relate to one another. For Earth based orbits, the starting point for all equations of motion is the Earth-Centered Inertial (ECI) frame. This is the reference non rotating frame from which all other frames can be further found for our purposes.

The ECI frame is a Cartesian grid space which is defined by using $\hat{\mathbf{e}_x}$, $\hat{\mathbf{e}_y}$, $\hat{\mathbf{e}_z}$. The $\hat{\mathbf{e}_x}$ direction is bound by the intersection nodal vector of Earth's equator and the orbital plane of Earth around the sun (the ecliptic) and is positive in the direction of the Vernal Equinox. Due to the precession of the Earth, the actual direction of the Vernal Equinox changes very slightly from year to year. The constant changing of this nodal vector creates a problem when standardizing the reference planes, as such the ECI frame is referenced against a specific epoch such as J2000 which was defined by the mean equator and equinox at the JD 2451548.0 $\hat{\mathbf{e}_z}$ is the vector which moves through the North Pole, while $\hat{\mathbf{e}_y}$ is defined simply by crossing $\hat{\mathbf{e}_z}$ and $\hat{\mathbf{e}_x}$ [19]. This frame is not entirely inertial however, but is non-rotating with respect to the stars, and has negligible amounts of acceleration allowing use as an inertial frame [20].

The Perifocal frame is effectively another inertial frame for Earth based satellites. Similar to the ECI frame it is a Cartesian grid space utilizing the vectors $\hat{\mathbf{P}}$, $\hat{\mathbf{W}}$, $\hat{\mathbf{Q}}$. In this frame $\hat{\mathbf{P}}$ is located in the direction of the periapsis of the orbit from the center of the orbiting body. The $\hat{\mathbf{W}}$ is perpendicular to the plane of orbit,

which is the direction of the angular momentum vector $\hat{\mathbf{h}}$. $\hat{\mathbf{Q}}$ lies on the orbital plane with $\hat{\mathbf{P}}$ and completes the orthogonal basis for the reference frame. This frame allows use of the simplified orbit mechanics models such as the two body problem, as well as simplifying the transform from the Keplerian elements to the Cartesian grid space used for equations of motion.

There are also a variety of non-Newtonian reference frames which are used in order to help determine the attitude of the spacecraft. The first is the orbital reference frame which is found as a set of vectors originating from the point of the spacecraft. The $\hat{\mathbf{O}}_x$ axis is in the direction of the spacecrafts velocity vector while $\hat{\mathbf{O}}_z$ vector is in the direction of the central body. A third vector, $\hat{\mathbf{O}}_y$ is the orthogonal cross product between the $\hat{\mathbf{O}}_z$ and $\hat{\mathbf{O}}_x$ vectors. The spacecraft roll, pitch, and yaw angles can then be found by the rotation of the spacecraft reference frame about the orbital reference frame. The spacecrafts reference frame is based on the geometry of the spacecraft and can be arbitrarily decided. Further reference frames for any deployed satellite structures can be found by referencing from the spacecraft main body frame. For the purpose of this project all body frames will be referenced as \mathbf{SC}_x , \mathbf{SC}_y , \mathbf{SC}_z with appropriate reference to the specific deployed structure.

Earth also has two more useful reference frames which are the Earth Centered Earth Fixed (ECEF) and East, North, Up (ENU). ECEF has X,Y,Z axis which are set at the center of mass of the earth and point to the 0° latitude, 0° longitude, and true north respectively. The ENU frames are based at the surface of the Earth at a local ground station and have the X,Y,Z axis defined by East, North, and directly upward respectively. The combination of these inertial and non-Newtonian reference frames allows for relative ease for determining spacecraft attitude, ground station tracking, and adjusting for time delays based off the rotation of the Earth.

2.1.3 Numerical Integration Techniques

The equations of the orbiting bodies are governed by gravitational attraction with minor perturbations from external forces and the space environment. Due to their transient nature, it is necessary to numerically solve them. There are many choices for methods when it comes to numerical integration, only three of the common families will be covered.

Runge-Kutta

A commonly used technique is the Runge-Kutta method due to a combination of its ease of use and adaptive step sizing [18]. Generally speaking the algorithm is as follows [19]:

$$\text{For } \dot{y} = f(t, y) \text{ with initial condition } y(t_0) = y_0 \quad (2.4)$$

A step size (h) greater than zero is then chosen and implemented in the following process.

$$y_{n+1} = y_n + h \sum_{i=1}^s b_i k_i \quad (2.5)$$

$$k_s = f(t_n + c_s h, y_n + h(a_{s1} k_1 + a_{s2} k_2 + \dots + a_{s,s-1} k_{s-1})) \quad (2.6)$$

For a general embedded Runge-Kutta method, the Butcher Tableau contains the coefficients for the above equation and is of the form shown in table 2.1.

In these tables the bottom b^* row is the higher order coefficients used for the error estimator. In adaptive methods the error is determined by the equation 2.7.

This is used to change the step size based on the user defined tolerance.

$$e_{n+1} = y_{n+1} - \hat{y}_{n+1}^* = h \sum_{i=1}^s (b_i - b_i^*) k_i \quad (2.7)$$

Adams-Basforth

Table 2.1: Butcher Tableau general form

	0				
c_2	a_{21}				
c_3	a_{31}	a_{32}			
.	.	.	\dots		
c_s	a_{s1}	a_{s2}	\dots	$a_{s,s-1}$	
	b_1	b_2	\dots	b_{s-1}	b_s
	b_1^*	b_2^*	\dots	b_{s-1}^*	b_s^*

It can be seen that the Runge-Kutta method is a single-step process which evaluates the function f multiple times per step in the solution, this typically leads to a longer computational time as it can not take advantage of previous steps history. Other methods for orbit propagation can be found in families of numerical techniques which use predictor-corrector schemes. These methods attempt to find a solution using a multiple previous steps to approximate a time step solution and then correct it using a corrector. By requiring multiple historical steps, it is not always convenient to use the predictor-corrector schemes, one solution is to propagate the necessary steps using a one-step method such as Runge-Kutta, and then move forward in the solution with the multi-step method. One of the best known predictor-corrector methods is the Adams-Moulton method which uses the Adams-Basforth predictor and the Moulton corrector formula. Equations 2.8, 2.9, and 2.10 show the predictor, corrector and estimated error formulas for stepping from time n to $n+1$. Note that the term $h^5 \frac{d^5x(\delta)}{dt^5}$ is the truncation error term and is generally omitted due to not knowing the truncation error [18].

$$P \quad h \quad \frac{251}{24} \frac{5}{5} d^5 x(\delta) \\ x_{n+1} = x_n + \frac{24}{24} (55f_n - 59f_{n-1} + 37f_{n-2} - 9f_{n-3}) + \frac{720}{720} h \frac{19}{5} \frac{d^5 x(\delta)}{dt^5} \quad (2.8)$$

$$C \quad h \quad P \quad \frac{19}{24} \frac{5}{5} d^5 x(\delta) \\ x_{n+1} = x_n + \frac{19}{24} (9f(t_{n+1}, x_{n+1}) + 19f_n - 5f_{n-1} + f_{n-2}) + \frac{720}{720} h \frac{19}{5} \frac{d^5 x(\delta)}{dt^5} \quad (2.9)$$

$$\frac{270}{270} |x_{n+1} - x_{n+1}| \quad (2.10)$$

Gauss Jackson

The Gauss-Jackson method is a multistep predictor corrector which has been used since the 1960s to estimate the position of tracked objects in space. The drawback of this method is that for an estimation of the N^{th} order, $N + 1$ points must be known before hand. Like the Adams-Bashforth method this can be initiated using a small time step Runge-Kutta variation and then propagated using this method [21, 22, 23]. It has been shown that the Gauss Jackson method has a lower global error than traditional Runge-Kutta 4 for near circular orbits, however RK4 has a lower global error than highly elliptical orbits [24]. Implementation of the Gauss-Jackson method can be found in [22].

2.2 Space Environment and Perturbing Forces

Many assumptions made above will not work as a mission is planned out in detail. In reality, burns to change and maintain orbits take time and expel mass from the spacecraft. Atmosphere imparts drag when in low earth orbit, the sun is a constant source of solar pressure which affects trajectory, and the main body of orbit is usually not a perfect sphere. General methods for including these perturbations in the orbit model will be found in the subsequent subsections and will be used in conjunction with equation 2.2 to improve the fidelity of space mission modeling.

2.2.1 Finite Burns

Most satellites which require long term orbit maintenance use some form of chemical propulsion or electric propulsion. In these cases the satellites propulsion system expels some amount of propellant in order to adjust its course. The thrust generated by the propulsion systems is assumed to be on axis with the direction of

travel and can be modeled adding the following equations to equation 2.2[25]:

$$\mathbf{F}_{\text{Thrust}} = T \frac{R_0 \mathbf{V}^{SC}}{|R_0 \mathbf{V}^{SC}|} \quad (2.11)$$

$$\dot{m} = \frac{-T}{I_{sp}g_0} \quad (2.12)$$

2.2.2 Atmospheric Drag

While in low earth orbits, the atmosphere still imparts some forces on the spacecraft. While very small, it can add up over time depending on the altitude of the spacecraft. The general method to include this force inside of perturbations is to use the satellites coefficient of drag (C_D), cross sectional area perpendicular to the velocity vector, and density from the chosen atmospheric model in order to calculate the drag. NRLMSISE-00 is an empirical model of earths atmosphere which is an extension of MSISE-90 which expanded the previous data set to include satellite drag [26]. Other models exist for the atmospheric density, such as: 1988 MET model, COSPAR International Reference Atmosphere 1986 (CIRA), and U.S. Standard Atmosphere. For the simulations purpose, the NRLMSISE-00 model was chosen in order due to including empirical data from satellites. Similar to thrust, drag is along the direction axis of travel, allowing us to formulate the equation for aerodynamic drag the same way as thrust. The following equations can be added to the perturbation forces in order to add in atmospheric drag. The model used to estimate density for our cases can be found in Appendix A.

$$\mathbf{F}_D = -\frac{1}{2\rho} |ATM\mathbf{V}^{SC}|^2 C_D A \frac{ATM\mathbf{V}^{SC}}{|ATM\mathbf{V}^{SC}|} \quad (2.13)$$

$$ATM\mathbf{V}^{SC} = {}^{EC}\mathbf{V}^{SC} - {}^{EC}\mathbf{V}^{ATM} = {}^{EC}\mathbf{V}^{SC} - ({}^{EC}\boldsymbol{\omega}^{Earth} \times {}^{EC}\mathbf{r}^Q) \quad (2.14)$$

2.2.3 Solar Radiation Pressure

Solar pressure is a force which is negligible compared to other perturbation forces under 800km altitude [1]. The following formula can be used to find the force caused by solar pressure. A is the cross sectional area exposed to the sun, r is an empirical reflection factor. An r value of 0 completely absorbs, while a value of 1 represents total reflection.

$$\mathbf{F}_{SP} = -4.5 \times 10^{-6}(1 + r)A \quad (2.15)$$

2.2.4 Oblate Earth

The original assumption under the first implementation of the gravitational force was a center mass point. However because the mass of the central body is usually non uniform, adjustments must be made. The well defined gravitational potential function, Φ , uses geopotential coefficients in order to modify the point mass gravitational force on the spacecraft. The general potential function is given as:

$$\Phi = \frac{\mu}{r} \left(1 - \sum_{n=2}^{\infty} J_n \frac{R_E^n}{r^n} P_n(\sin(\psi)) \right) \quad (2.16)$$

Where J_n is the geopotential coefficient, ψ is the geodetic latitude, P_n is the Legendre polynomials [1, 19]. In the Cartesian system this can be re-written using equation 2.17 [27].

$$\begin{aligned} P_x &= \frac{P_x}{\sqrt{5Z^2 - X(X^2 + Y^2 + Z^2)}} \\ P_y &= \frac{3J_2\mu R_s^2}{2R_s^7} \cdot \frac{5Z^2 - Y(X^2 + Y^2 + Z^2)}{5Z^2 - 3Z(X^2 + Y^2 + Z^2)} \\ P_z &= \end{aligned} \quad (2.17)$$

2.2.5 Magnetic Sphere and Ionizing Radiation

The geomagnetic field for Earth can be calculated using the world magnetic model (WMM) which is distributed by NOAA's National Centers for Environmental Information. Updated coefficients are updated every five years, and can be assumed to be linearly time varying across the coefficients five year lifespan. The magnetic model can be used to assist the attitude determination system to determine the current pointing of the spacecraft. Due to time limitations this will not be implemented in this project, however suitable sources for this model can be found from NOAA's NCEI website. By knowing the satellite's latitude, longitude, altitude and date the WMM software can predict the components of the magnetic field [28].

CREME96 is a suite of programs which can be used to model the ionizing radiation environment of near Earth orbits. Similar to the magnetic sphere, the inclusion of this model will not be implemented for the initial simulation due to the time constraints. In future work it will be used to model the chance of single event upsets to create a realistic SEU test for redundancy models.

Chapter 3

SUBSYSTEM BASELINE DESIGN

This section will cover the principle design equations that will be used in the design exploration, optimization and models simulation. Each section has a set of design methods which provide general sizing and performance rates, a set of possible objectives to optimize around, as well as a variety of system and mission variables which influence the output of the design equation sets. For the example mission we have a nanosatellite at some altitude and inclination in a circular orbit. The objective is to provide short wave infrared imagery for analysis of identifying geological material.

3.1 Attitude Determination and Control System

For the attitude determination and control system (ADCS) model to work the initial state, mass moment of inertia, inertia, external torques, and desired pointing angle must be known. For each time iteration through the ADCS model will determine the power required to point to the correct position, and produce any updated variables that it has changed. For the purpose of design exploration and sizing a set of equations will be used to determine the estimated torques on a nanosatellite and a regression analysis of ADCS hardware will be performed in order to estimate the size, weight, and power draw for this subsystem. Due to time limitations only the system sizing and optimization will be performed for this subsystem. The system model in the simulation will only support power draw as a way to estimate battery state of charge over the course of the satellites life. Future

work will be needed to incorporate multiple control modes and the required six degree of freedom model to simulate realistic satellite behavior. That is outside the scope of this project.

3.1.1 Estimated Torques

Estimating the total worst-case disturbance torques allow the system designer to get basic information on the size and complexity of the ADCS. In this case there are four main components of the torques: gravity, solar, magnetic and aerodynamic. The following equations allow the estimated torques (in $N \cdot m$) to be calculated. The angle, θ , is the maximum deviation of the z-axis from the local vertical in radians. The angle, i , is the incidence angle of the sun on the spacecraft. The moments of inertia are in $kg \cdot m^2$. All length units in this subsection are meters. The reflectance factor, q , lies between 0 and 1 and can be estimated as 0.6 [1]

$$T_{gravity} = \frac{3\mu}{2R^3} |Iz - Iy| \sin(2\theta) \quad (3.1)$$

$$T_{solar} = \frac{W_f}{c_s} A (1 + q) \cos(i) (c_{pressure} - c_{gravity}) \quad (3.2)$$

$$T_{mag} = \frac{2DM_e}{R^3} \quad (3.3)$$

Note that D is the residual dipole (in $A \cdot m^2$) of the spacecraft, and M_e is the magnetic moment of earth ($7.96 * 10^{15}$ tesla \cdot m^3).

$$T_{aero} = \frac{1}{2} \rho V^2 A_s C_d (c_{pressure} - c_{gravity}) \quad (3.4)$$

3.1.2 Regression Analysis of ADCS Systems

The output report of the ADCS code has been included at the end of this report. In it the regression model figures to analyze data can be seen, as well as R^2

values and residuals plotted against fitted values. A quick summary of the results includes the following findings:

- Mass of reaction wheels is related to total momentum capacity, power is related to wheels maximum torque.
- For wheels there is little correlation between the Z dimension and either max torque or momentum capacity due to the range of models selected.
- The X and Y dimensions of reaction wheels are related to the momentum capacity of the wheel. This is due to increasing the inertia of the wheels directly increases the total momentum capacity.
- Mass and power of magnetic torque rods average to a constant. The physical dimensions are correlated to the rods dipole however.
- IMUs and Magnetometers have a wide variety of power, weight and size. More models should be gathered before a reasonable estimate can be made.

3.1.3 Physical Parameter Estimation Models

H_{max} is given as maximum momentum capacity in $N \cdot m \cdot s$. τ_{max} is the maximum torque of the wheel in $N \cdot m$

$$M_{Wheel}(kg) = 1.666 \cdot H_{max} + 0.1216 \quad (3.5)$$

$$P_{Wheel}(W) = 0.466 \cdot H_{max} + 0.5106 \quad (3.6)$$

$$X_{Wheel}(mm) = 20.55 \cdot \ln(H_{max}) + 120.4 \quad (3.7)$$

$$Y_{Wheel}(mm) = 20.21 \cdot \ln(H_{max}) + 118.0 \quad (3.8)$$

$$Z_{Wheel}(mm) = 23.61 \cdot \ln(H_{max}) + 100.2 \quad (3.9)$$

Dipole is given as $A \cdot m^2$

$$M_{Mgtqr}(kg) = 0.001 \cdot Dipole + 0.3457 \quad (3.10)$$

$$P_{Mgtqr}(W) = 0.0502 \cdot Dipole + 0.399 \quad (3.11)$$

$$X_{Mgtqr}(mm) = 1.087 \cdot Dipole + 17.65 \quad (3.12)$$

$$Y_{Mgtqr}(mm) = 0.8574 \cdot Dipole + 14.47 \quad (3.13)$$

$$Z_{Mgtqr}(mm) = 29.18 \cdot Dipole + 87.24 \quad (3.14)$$

The pointing knowledge, ${}^\circ_k$, is in degrees.

$$M_{ST}(kg) = -7296 \cdot {}^\circ_k^2 + 31.79 \cdot {}^\circ_k + 2.735 \quad (3.15)$$

$$P_{ST}(W) = -4592e4 \cdot {}^\circ_k^2 + 750 \cdot {}^\circ_k + 5 \quad (3.16)$$

$$X_{ST}(mm) = -6071 \cdot {}^\circ_k + 196.3 \quad (3.17)$$

$$Y_{ST}(mm) = -6500 \cdot {}^\circ_k + 200.3 \quad (3.18)$$

$$Z_{ST}(mm) = -1.536e4 \cdot {}^\circ_k + 387 \quad (3.19)$$

No reasonable estimation models could be found with the IMUs or magnetometers. Because of this the overall margin of the ACDS should be increased in the baseline to allow for the inclusion of these items if necessary.

3.2 Command and Data Handling

The command and data handling (CDH) subsystem is the most critical component of nanosatellites as it controls the timing for functions for all on-board operations as well as communication between the end user and the satellite in orbit. This subsystem can not be adequately sized using parametric equations due the complexity of processing components, board formats, and rapid miniaturization of hardware for space. To provide an adequate estimate of size, power and weight for

this subsystem a regression analysis was performed. The selection process shown in Space Mission Design and Analysis provide a method to estimate the complexity of the system which is a possible candidate for the sizing estimate variable. The adapted table is shown in table 3.1.

3.2.1 OBC Requirements Sizing

The on-board computer (OBC) is a complex system which lies outside the scope of this project. As such a down select process is required in order to meet the OBC requirements. The performance requirements are based on the software requirements, which are outlined in this section. It is assumed that NASAs core flight software suit will be the base of the nanosatellite software and that additional modules will double the total logical lines of code. This results in a total SLOC count of 78.6K lines [29], with the language assumption of C. The underlying operating system, FreeRTOS is around roughly 10k SLOC. Using the tables from SMAD we can safely estimate the instructions per second as

$$IP\ S = 28 \cdot SLOC \quad (3.20)$$

3.3 Communications

The communications subsystem is the only interface that the satellite has with the ground facility and is used for tracking, telemetry, command, mission data transfer and ranging. The design of the communications architecture is based on the combination of satellite, relays, and ground station resources which are available in the mission design. The current architecture chosen is a single ground station located in San Jose, with a single low altitude nanosatellite placed in an orbit which

passes overhead. This was chosen due to the simplicity of the architecture and to minimize the overall cost of the proposed design. All of the design equations for the communications subsystem and the communications architecture are from the Space Mission Analysis and Design book unless otherwise noted [1].

3.3.1 Data Transmitted

In order to ensure that as much data gathered by a scientific satellite is capable of being transferred back to Earth, it is important to ensure that the communications links have a sufficient received energy-per-bit to noise density ratio. This ratio is typically design around for a value between five and ten for most missions [1]. This ratio is used to predict the bit error rate depending on modulation technique and can increase (or decrease) the number of passes required for a complete data download. As many nanosatellites do not have the ability to perform orbit maintenance it is important to ensure as much data is sent back to Earth in each pass as the satellite will eventually burn up in the planets atmosphere, resulting in permanent loss of any data not transmitted. The total data downloaded can be estimated from equation 3.21.

$$D = \frac{R(F T_{max} - T_{init})}{M} \quad (3.21)$$

Where the fractional reduction in viewing time, F, is defined by the orbit geometry in equation 3.22

$$F \stackrel{\text{def}}{=} \frac{1}{\lambda_{max}} \arccos \left(\frac{\cos(\lambda_{max})}{\cos(\lambda_{min})} \right) \quad (3.22)$$

3.3.2 Received Energy per Bit to Noise Density

$$\frac{E_b}{N_o} = \frac{P L_t G_t L_s L_a G_r}{k T_s R} \quad (3.23)$$

At first glance the ratio terms are not intuitive of the underlying design variables so a derivation and example calculation of this is performance parameter is provided in the appendices. This is used to determine which modulation scheme to use to satisfy a bit error rate requirement.

3.3.3 Communication Size

The pointing loss, L_θ , in dB can be calculated as a function of pointing error and beam width.

$$L_\theta = -12 \frac{\text{err}^2}{\theta} \quad (3.24)$$

Where θ is the half power beam width. The estimated size of the helix antenna can then be found using

$$\theta = \frac{52}{(\pi D)^2 L / \lambda^3} \quad (3.25)$$

Where D and L are in meters and λ is in GHz. It should be noted that for the best gain the following inequality should be followed.

$$0.8 \leq \frac{\pi D}{\lambda} \leq 1.2 \quad (3.26)$$

Another option for the microwave frequency is the patch antenna which has a design region given as follows [30]

$$\{0.003\lambda < t < 0.05\lambda\} \cap \frac{\lambda}{3} < h < \frac{\lambda}{2} \quad (3.27)$$

3.3.4 Design Variables for subsystem

From the architecture design and communication subsystem sizing equations we have the following input variables which will be analyzed for cause-effect relations to determine which design choices will make the largest impact. There are design variables from the hardware side, as well as the missions orbit. The following hardware design variables have been identified based on the preceding design equations and will first be analyzed in design of experiments to determine which will become parameters and which will remain variables for optimization.

- Data rate R
- Antenna max rotation (Θ_{tx})
- Transmission antenna power (P)
- Trans/Receiver gains (G_i)
- System Noise temperature(T_s)
- Frequency (f)
- Modulation technique

The following variables have been identified as factors in the sizing of the communication subsystems but are more closely related with other subsystem, mission and environmental variables. As such their effect will be analyzed however their respective size drivers will be based on the subsystem or mission parameter in question.

- Altitude
- Ground station location

- Weather losses (for worst case scenarios)

Hardware variables include transmitter power antenna gains, system temperature, line loss, and bit rate.

3.3.5 Data Transmitted

Data rate of the system (bps), Time in view, and fractional viewing time are the variables in play. The hardware component is simply bps and transmitting antenna rotation (power, time in view). The mission orbit selection and ground station location will determine time in view, fractional viewing time.

3.4 Electrical Power System (EPS)

The EPS needs to have knowledge of the solar cell position, battery position, and current draw. If the current draw is too high the EPS must reset the entire system to prevent hardware failure. If the charge of the batteries needs to increase, the solar panels will need to be adjusted and a new output of their position must be had for the ADCS. This section is divided into two parts, power generation and power storage.

3.4.1 Solar Power Generation

Determining the solar array size is dependent on the time the satellites time in different power modes, time in sunlight, and solar cell type. The cell type determines both the efficiency of the satellite panels as well as the degradation percentage per year due to environment and usage. The selected cell material was GaAs due to superior performance towards end of life. It is assumed that the solar array incidence angle is at worse within 30 degrees of the sun light. Estimating the

total power of the solar array for generation can be found using equation 3.28.

$$P_{sa} = \frac{\frac{P_e T_e}{X_e} + \frac{P_d T_d}{X_d}}{T_d} \quad (3.28)$$

The power in the eclipse orbit and daylight orbit are dependent on the satellites mission objectives and should be worst case scenarios. The efficiencies X_i are dependent on the power regulation type but range from 60% to 85% typically [1]. The beginning of life power is cell and manufacturing/integration dependent. This is estimated as

$$P_{BOL} = P_0 \cdot I_d \quad (3.29)$$

For a typical GaAs cell this estimated at $181 \frac{W}{m^2}$. The end of life power can be found by extrapolating the estimated degradation per year over the lifetime of the satellite, assuming no failures in the solar cell this is give as follows:

$$P_{EOL} = P_{BOL} \cdot \left(1 - \frac{\text{degradation}}{\text{yr}}\right)^{\text{lifetime}} \quad (3.30)$$

From the end of life power we can size the solar array such that it will generate enough power at the last year of its life and is given as the ratio $\frac{P_{sa}}{P_{EOL}}$. The estimated mass is can be estimated as

$$M_{sa} = \frac{P_{EOL}}{M_{sp}} \quad (3.31)$$

typically the specific mass is around 14 to $47 \frac{W}{kg}$ at the end of life.

3.4.2 Power Storage

The batteries must be charged in the daylight period and used during the eclipsed period which leads. The estimated necessary battery capacity can be found with equation 3.32.

$$B_{cap} = \frac{P_{ecl} T_{ecl}}{(DOD) N n} \quad (3.32)$$

Where DOD is the estimated depth of discharge, N is the number of batteries and n is the transmission efficiency of the battery. The mass of the batteries can be estimated from the power density of the battery material type and some margin for cabling. It is assumed that anything less than 30 Amps for the total system draw can be around 0.05kg for the total connections [1].

3.5 Payload

For this satellite mission an infrared imager was chosen as the optical payload. Because the payload drives the requirements for the satellite bus it is important to find a locally optimal baseline payload before evaluating the design of the bus. In this case the sizing process for a passive optical payload was adapted from the SMAD Firesat example. The scaling ratios and constants provided by the design equation were applied to the Argus 1000 Infrared spectrometer to compare to modern small satellite remote sensor payloads.

3.5.1 Payload Design Size Estimates

The initial baseline payload can be estimated by estimating eight design variables based off of mission requirements, trade studies and historical data. The design variables and typical levels are discussed in the next subsection. For the preliminary investigation it is assumed that the satellite in question has a near circular orbit ($e \approx 0$). The baseline design estimate is provided from SMAD.

After the orbit has been decided the payload can begin being designed. For the preliminary design we can assume a circular orbit and a spherical Earth. We begin by determining the orbit period, in minutes, for the circular orbit which can be

found with equation 3.33.

$$P \text{ (min)} = 1.658669e-04 \cdot \frac{R_E}{R_E + \text{Altitude}} \quad (3.33)$$

It will be useful later on to determine the ground velocity of the spacecraft over the Earth. In our case we can simply the ground velocity to be constant (assuming no perturbations for our orbit) and simplifies to the following.

$$V_G = \frac{2\pi}{P \text{ (sec)}} \frac{R_E}{R_E} \quad (3.34)$$

The angular radius, ρ , seen from the satellite to the target is the angle from the satellite which goes from the subsatellite point to the outer horizon of the Earth.

This can be calculated for with equation 3.35

$$\rho = \sin \frac{R_E}{R_E + \text{Altitude}} \quad (3.35)$$

The Earth central angle, λ is the angular radius as seen from the center of the earth between the subsatellite point and the target. The region viewable by the spacecraft can also be defined from the center of the earth as λ_0 . The sum of λ_0 and the satellites angular radius is equal to 90° .

$$90^\circ = \lambda_0 + \rho \quad (3.36)$$

The distance between the satellite and the outer horizon of the earth can now be calculated.

$$D_{max} = R_E \cdot \tan(\lambda_0) \quad (3.37)$$

The elevation, E , from the observer on the ground to the satellite is the angle from the target to the satellite in space. The incidence angle is the angle from the normal of the targets surface to the satellite. The sum of the incidence angle and elevation angle is 90° . By defining a maximum incidence angle (or minimum elevation angle),

we can compute the maximum angle in view and the maximum earth central angle for the satellite using equations 3.38 and 3.39 respectively. It is important to see that the swath width is simply twice the maximum earth central angle.

$$\eta_{max} = \sin^{-1} (\cos(90^\circ - IA_{max}) \cdot \sin(\rho)) \quad (3.38)$$

$$\lambda_{max} = 90^\circ - (90^\circ - IA_{max}) - \eta_{max} \quad (3.39)$$

Using the calculated values the slant range to the target can be calculated using equation 3.40

$$R_S = R_E \cdot \frac{\sin(\lambda_{max})}{\sin(\eta_{max})} \quad (3.40)$$

The maximum along track ground sampling distance, Y_{max} , is a design variable which is a spatial resolution parameter. This is the worst ground sample distance at the edge of the swath. Using this design parameter we can find the instantaneous FOV for a single pixel using equation 3.41.

$$IFOV = \frac{Y_{max}}{R_S} \cdot \frac{180^\circ}{\pi} \quad (3.41)$$

From Y_{max} it is possible to also determine the across track max ground sample distance through a simple trigonometric expressions.

$$X_{max} = \frac{Y_{max}}{\cos(IA_{max})} \quad (3.42)$$

The best spatial resolution of the optical payload (viewing the target directly under the satellite) can be found as well using right triangles.

$$X, Y_{min} = IFOV \cdot Altitude \cdot \frac{\pi}{180^\circ} = 2 \cdot Altitude \cdot \tan \frac{IFOV}{2} \quad (3.43)$$

Data rates can now be found by determining the number of pixels that are along the track (this is highest when the optical sensor has the highest nadir angle), the

number of swaths recorded in one second, the number of pixels. These can be found in equations 3.44, 3.45, and 3.46 respectively.

$$Z = \frac{2 \cdot \eta_{max}}{IFOV}^C \quad (3.44)$$

$$Z_A = \frac{V_g}{Y} \cdot 1sec \quad (3.45)$$

$$Z = Z_C \cdot Z_A \quad (3.46)$$

The encoding bits per pixel is a design parameter based on your dynamic range necessary for data acquisition. After this is decided the data rate may be found as shown in equation 3.47

$$DR = Z \cdot \frac{Bit}{Pixel} \quad (3.47)$$

There are two other key objectives for the payload design, sensor dwell time and aperture diameter. The dwell time can be increased or decreased based on the number of pixels the instrument has, however the dwell time must remain above the detection time constant of the payload. The estimated integration period for the pixel can be found in 3.48, where N_m is the number of pixels on the instrument scanner along the track.

$$T_i = \frac{Y_{max} \cdot N_m}{V_g \cdot Z_C} \quad (3.48)$$

The aperture diameter can be estimated from the pixel width (d), image quality factor (Q), focal length (f), and operating wavelength (λ_{op}). The focal length can be estimated with equation 3.49 and the payload aperture diameter by equation 3.50

$$f = \frac{\text{Altitude} \cdot d}{X_{min}} \quad (3.49)$$

$$D_{aperture} = \frac{2.44\lambda_{op} \cdot f \cdot Q}{d} \quad (3.50)$$

The ratio of the aperture diameter of the payload and a previously flown instrument can be compared and used or estimating the size. The ratio, R_{AD} , is also used to

determining the scaling parameter K for the instrument. If the ratio is less than 0.5, the scaling parameter is 2. Otherwise the scaling parameter can be left as 1. If X_o, Y_o, Z_o denote the linear dimensions of the previous hardware, and variables kg_o and W_o denote the mass and power as well. The estimated physical parameters can be found using the following five equations:

$$X_{new} = R_{AD} \cdot X_o \quad (3.51)$$

$$Y_{new} = R_{AD} \cdot Y_o \quad (3.52)$$

$$Z_{new} = R_{AD} \cdot Z_o \quad (3.53)$$

$$kg_{new} = K \cdot R_{AD} \cdot kg_o \quad (3.54)$$

$$W_{new} = K \cdot R_{AD} \cdot W_o \quad (3.55)$$

The five physical parameters, data rate, ground sample distance, and image quality factors are all possible objectives for payload optimization.

3.5.2 Design and Optimization Variables

The following design variables are used in the design space exploration and optimization routines.

- Altitude (km)
- Maximum Incidence Angle (θ)
- Maximum Along Track Ground Sample Distance (m)
- Bit Per Pixel (Integer ≥ 1)
- Pixels for Instrument (Integer)
- Width of Square Detector (μm)

- Image Quality Factor (0.5 to 2)
- Operating Wavelength (λ)

Typical altitudes for altitude lie between 300 and 700 km for typical nanosatellites. The maximum incidence angle is the maximum angle expected for which the payload will be used. It is relative to the normal of the local ground at the target sight. The incidence angle and the spacecraft elevation angle (from the ground station) sum to 90 degrees. The maximum along track ground sample distance is the spatial requirement at the maximum earth central angle (i.e. maximum off nadir coverage). This can be visualized the ground sample distance at the edge of the swath, with the ground sample distance decreasing as you get close to nadir. Bit per pixel is an integer for the number of bits for the pixel data.

The pixels for instrument variable is the number of pixels along one dimension (along track) in the optical payload for whisk broom type scanners. Width of square detector is the physical dimensions for an individual pixel in the optical system. In the case of CMOS sensors this can be as small as $2\mu m$. Larger pixel sizes such as those on the Lunar Image Spectrometer on the SELENE mission are $40\mu m$ also exist. The image quality factor is a scaling function to reduce the image quality or due multiple samples. It directly influences the data rate by scaling the total number of bits in the image. It is suggested that a factor of 1.1 be used as the nominal good image quality factor [1]. Finally the operating wavelength is the wavelength chosen for the optical payload. In our case it is para-metricized at $3\mu m$, the short infrared band.

3.6 Redundancy Model

The triple module redundancy (TMR) model is comprised of three majority voters, three minority voters, and three inverted tri-state models, and an error detection phase. The three inputs are sent to the three majority voters in parallel. These three majority voters then provide the most common input based on the following truth table shown in table 3.2. Similarly the minority voter (truth table in table 3.3) provides the least common output as an output which is used by the tri-state buffer which is used to suppress erroneous outputs.

The majority voters output (Y) is sent as the primary channel (P) input for the minority voter. R1 and R2 are from the other respective channels. If the primary input (P) is part of the majority then the inverted tri-state (an active low) is active and the data is allowed to pass through. If the primary channel is not part of the majority then the tri-state buffer prevents the data from being passed through allowing all outputs to be the correct input as long as two faults have not occurred in the logic module. The fault detection block is a combination of gates which will generate a high signal in order to send a reset command to the FPGA. This is a combination of XOR and OR gates based in the incoming signals before and after the majority voters as simple use for the current design. The test of the TMR module as well as the TMR module setup is shown in Appendix C. A switching algorithm has been developed to move data between failed modules in a predetermined time frame however the specifics can not be shown due to it being intellectual property. The redundancy test setup can be viewed in Appendix C as well.

Table 3.1: Adapted system complexity table from [1]

Requirement or Constraint	System Complexity		
	Simple	Typical	Complex
Processing Commands:			
Command Rates	50 CMD/s	50 CMD/s	≥ 50 CMD/s
Computer Interface	None	Computer or Stored Commands	Yes
Stored Commands	None		Not Needed
Number of Channels	<200	300-500	>500
Processing of Telemetry Data			
TLM Rates	<4 Kbps	4-64 Kbps	64 - 256 Kbps
Payload Data	None	1-200 kbps	10 Kbps - 10 MBps
Computer Interface	None	None	Yes
Number of Channels	<200	400-700	>500
Other			
Mission Time Clock	None	Included	Included
Watchdog	None	Included if OBC chosen	Yes
ADCS Function	None	None	Yes
Bus Constraints	Single Unit	Up to multiple units	Integrated or Distributed
Total Ionizing Dose	<2kRads	2-50 kRads	50kRads - 1MRad

Table 3.2: Majority Voter Table

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

Table 3.3: Minority Voter Truth Table

P	R1	R2	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0

Chapter 4

SYSTEM EXPLORATION, DESIGN OF EXPERIMENTS AND SIMULATION MODELS

4.1 Requirements Generation

Each nanosatellite has a set of design and mission requirements which must be fulfilled in order to be considered a successful mission. The generation of these requirements are based on inputs from a combination of stakeholders including designers, researchers, launching companies, and regulatory agencies. For the purpose of this project two documents will be created. The first is the Certification Acceptance Requirements Documents, which is a physical document detailing the traceability of all system and mission requirements. The second is an internal requirements module which can be used to provide quick checks on system level designs and will eventually be combined into the simultaneous analysis and design optimization process. The requirements module is integrated with other system and subsystem models and provide some amount of traceability as well as automatic documentation for theoretical designs. The module will provide a quick check for the feasibility of the design but are not a substitute of actual verification and validation of the physical hardware which is to be flown. The major limitation of the requirement module is the fidelity of the subsystem modules.

4.1.1 Certification Acceptance Requirements Document

The requirements created for this project have been developed based on input from John Hines, Reine Ntome, and Tyler Woods. They have been collected into a

certification and acceptance requirements document (CARD) located at the end of Appendix 2. The CARD is a single integrated document which provides all necessary requirements and objectives necessary for mission completion. It also provides a breakdown of which party is responsible for the completion of the requirement, the verification method, and any necessary verification documents. The CARD for the proposed mission is provided in the appendices.

The CARD is a table of requirements which shows the requirement I.D., a description, traceability (documents, etc.), dictates what party is responsible, how the verification will be shown, what documents are linked to the verification, and any comments the requirement may pose to the subsystem teams, systems engineers, management, or customers. Verification of requirements being met are done through testing (T), review of design (D), analysis / memo (A), and inspection (I).

4.2 Design Space Exploration and Optimization

This section will cover design space exploration techniques and possible methods of analysis in order to determine which variables will have the most effect.

4.2.1 Design Space Exploration and Design of Experiments

Spacecraft system designs complex and difficult to design due to the large set of design variables that are needed to find near optimal solutions. Typically the design variable inputs are in a range of $O(10^5 \sim 10^7)$ and are coupled with other design variables [31]. Due to time limitations and the inability to validate against hardware, we will focus on the smaller set, $O(10^1)$ set of variables in the baseline design. The goal of these large data set optimizations is not to find a global optimum, but rather converge towards the optimal solution in order for designers to

effectively move the end design towards their specific goal. In order to minimize the time of the optimization routines in OpenMDAO a design of experiment analysis is performed in order to set variables with little effect on the system design to a single parameter based on historical data and designer intuition. Using OpenMDAOs design of experiment (DoE) driver, parametric models of each subsystem have been created and were analyzed for a full factorial statistical analysis. The full factorial statistical analysis is a method which analyzes each variable (a factor) at multiple values (levels) in order to understand how the outcome (response variable) changes. The benefit of a full factorial analysis is the ability to detect interaction between multiple design variables with respect to the outcome. Design variables which have limited effect on the outcome or have limited options to begin with may be set to specified values based on the reality of the situation. For example there are only so many ground stations which the designer may have to choose from, or the payload may already exist and the designer is then required to make as little modifications to it as possible to minimize performance loss of the payload.

4.2.2 Design of Experiments Analysis

When first analyzing a DoE, it is important to code the data into a useful format. For our purpose a linear transform is used to map the different levels of each factor into a range of -1 to 1. This has two benefits when analyzing the data. The first is that there is no change to the shape of the distribution of independent variables which is important when you need to verify assumptions for statistical models such as analysis of variance (ANOVA). Secondly the transformed factors in full factorial design matrix has all orthogonal columns [32]. This is important as any experimental design which is orthogonal allows each factor to be evaluated independently of each other. It has bonus effect which makes interaction plots

significantly more readable, but that has no analytical benefit. The linear transform applied is given in equation 4.3 and its inverse function in 4.4. Let \mathbf{U}_i be the vector of the i -th factor which has the level for each experiment. $X_{i,H}$ and $X_{i,L}$ represent the highest and lowest level respectively. We can then define the scaling constants for the transform as follows:

$$a_i = \frac{X_{i,H} + X_{i,L}}{2} \quad (4.1)$$

$$b_i = \frac{X_{i,H} - X_{i,L}}{2} \quad (4.2)$$

$$\mathbf{Y}_i = \frac{\mathbf{U}_i - a_i}{b_i} \quad (4.3)$$

$$\mathbf{U}_i = \mathbf{Y}_i * b_i + a_i \quad (4.4)$$

By ensuring orthogonality using statistical methods such as ANOVA and graphical methods such as matrix scatter plots, we can analyze the main and interaction effects between design variables on each response output. The main graphical methods that were used were the main effect and interaction effect scatter plots, response distribution histograms and box plots. In most cases this showed immediate results of what design factor impacted the response outputs as main effects, which set of design variables had two-factor interaction, and in some cases that the response variable was indifferent to the factor. Using this knowledge, trade studies for specific design variables (e.g. operational wavelength), and general intuition specific factors were set to parameters based on historical data or constants taken from the SMAD book. This reduced the number of iterations for the optimizer function and reduced the overall optimization time.

For design spaces which do not have clear results from graphical techniques, an ANOVA test can be performed. For this test to be applied there are six assumptions which must be met. While some assumptions are robust to how well

your data fits to it, assumption 5 is required to be able to substantiate any claim from this test. The assumptions are listed as follows:

- (1) Response variable is continuous
- (2) Independent variable should have two or more categorical independent groups
- (3) There should be independence of observations
- (4) No significant outliers
- (5) Response variable (residuals) should be normally distributed for each category of the independent variable
- (6) Homogeneity of variances. (Variances of response groups should be within 2 times the lowest)

The general model applied to the data set (in this case two factors (i and j) is given as

$$Y_{ijk} = \mu + \alpha_i + \beta_j + E_{ijk} \quad (4.5)$$

Where for response value at (i,j), $Y_{i,j,k}$ the mean value, a factor effect is found (e.g. the i-th factor has the overall effect α_i), and some error term, E_{ijk} is computed. The predicted values for each observation then becomes:

$$\hat{Y}^{ijk} = \hat{\mu} + \hat{\alpha}_i + \hat{\beta}_j, \text{ with residual } R_{ijk} = Y_{ijk} - \hat{\mu} - \hat{\alpha}_i - \hat{\beta}_j \quad (4.6)$$

For a design of experiment with no replication, (i.e. $Y_{ijk} = \mu_{ij} + E_{ijk}, \quad k = 1$) there are some small things to make note of. The validity of an N-Way ANOVA with no replication significantly decreases and are listed below [33]. For assumptions that there may be significant interaction effect.

- For fixed factors ($i,j = 1,\dots,n$)
 - * Model 1 n-ANOVA can be performed with caution
 - * Model 2 n-ANOVA can be performed with higher type II error
 - * Interaction effects can not be tested
- For random factors ($i,j = 1,\dots,n$)
 - * Factors A and B can be tested as factor I MS / remained MS
 - * Interactions can not be tested
- For mixed models (A is fixed and B is random)
 - * Factor A can be tested
 - * Factor B can not be tested
 - * There is no interaction test available.

In the case of correctly assuming that there is no interaction effect, all factors may be tested for Factor (I) MS / remainder MS. The ANOVA process is fairly lengthy to describe in this report and sufficient examples may be found online or in engineering statistics textbooks. For the purpose of this study, the ANOVA process was handled by MATLABs statistical toolbox. Model validation can be performed by analyzing the normal probability plot and run sequence plot of residuals, as well as a scatter plot of the predicted values against the residuals [32]

4.2.3 Optimization

While there are many optimization methods they can be broadly categorized into methods which use gradients and those that do not. Gradient free optimizer

suffer computational performance as the number of design variables increase due to the the use of design variables across the entire range of the design space [34]. Gradient optimization methods allow for designers to assess the system sensitivity to various design variables and select a range for design options. For the purpose of this project the OpenMDAO tools will be used. OpenMDAO is a set of optimization methods implemented in Python to allow researchers to analyze complex (high design variable sets) systems by grouping separate components into processes which can be run in parallel to satisfy a set of constraints.

The OpenMDAO approach assigns each variable a residual which is then grouped to form a set of nonlinear system of equations [35]. Hwang has shown that by driving the residuals to zero that a system of nonlinear equations can be formed which allow the computation of total derivatives. The unifying derivatives equations is shown in equation 4.7.

$$\frac{\partial R}{\partial u} \frac{du}{dr} = I = \frac{\partial R}{\partial u} {}^T \frac{du}{dr} \quad (4.7)$$

Using the computed total derivatives it is possible then to use the methods in OpenMDAO to either explore the design space or to optimize a chosen initial design to find a local optimal solution. The use of the optimizer is to find locally optimal solutions to use as a baseline design for nanosatellites. Future work is required to perform a simultaneous analysis and design to find optimal solutions for an end product, that is beyond the scope of this project. To find a good design compromise with the variety of objectives and constraints, the Kriesselmeier-Steinhauser function will be used to aggregate all constraints into a single criteria which will allow the optimizer to find a local compromise from possible solutions [31, 36]. This function is shown in equation 4.8.

$$KS(x) = \sum_{i=1}^{n_{max}} \frac{1}{\rho} \ln \left(\frac{e^{-\rho(f_i(x) - f_{i,max}(x))}}{\rho} \right) \quad (4.8)$$

4.3 Simulation Models

The simulation models are used to take analyze designs from the design space exploration and optimization routines and evaluate their feasibility for normal operations. They are not full detailed modes as the level of fidelity is not something that can be done by one person in the time constraints imposed currently. Each section lists the model levels needed to perform at the very basic level a data and power draw test for analyzing some mission requirements. Note that due to time constraints some of these modules may not be implemented.

4.3.1 Orbit Model

The orbit model must provide the position, sunlight line of sight, target line of sight, and environmental disturbances to the spacecraft.

4.3.2 Attitude Determination and Control System

The ADCS module will only saturate momentum and then dump it via magnetic torque rods. This will be used to exercise the battery modules.

4.3.3 Electrical Power Subsystem

The electrical subsystem must include the solar arrays, batteries, and estimated mass of power regulators and connections. The model must be able to estimate the state of charge based on system draw. The temperature of the solar array also reduces the efficiency of power generation by about 0.5% per degree above 28 ° C.

4.3.4 Communications

The communications systems will be able to measure the ideal data rate and power draw on the system when over specified locations in orbit relative the the ground targets and stations.

4.3.5 Payload

The payload must be able to warm up, operate, and gather data based on the LOS of the target. It is expected that the data will simply be randomly generated binary data as it is too difficult to replicate performance data for the payload system.

4.4 Benchmarks for Design of Experiment analysis and Optimization

Due to the large amount of space required to perform and demonstrate DoE techniques it is recommended that the reader understand the relevant sections from the NIST e-handbook of Statistical Methods [32]. An optimization benchmark for a multi-objective constrained problem can be found in the following section. It is important to note that using the K-S optimization routine provided by the pyOpt package that it is possible to initiate a optimization problem outside of the design region and it will automatically move towards to closest locally optimal design point. The benchmark case will showcase the ability of the technique in an easy to view two dimensional problem.

4.4.1 Optimization with Combined Constraints

The following benchmark case comes from the Multi-Objective Optimization Using Evolutionary Algorithms book by K. Deb [37]. The simple optimization

problem is only in the \mathbf{R}^2 domain which allows it to be easily visualized for both the feasible search space. Similarly with only two objective functions it is possible to graphically show the intersection of f_1 and f_2 .

$$\begin{aligned} \text{Minimize } & \quad \square f_1(x, y) = x \\ \text{s.t. } & \quad \exists f_2(x, y) = \frac{1+y}{x} \end{aligned} \tag{4.9}$$

In the region $0.1 \leq x \leq 1$ and $0 \leq y \leq 5$ with the following objective constraints

$$\begin{aligned} \text{s.t. } & \quad \square \exists g_1(x, y) = y + 9x \geq 6 \\ & \quad \exists g_2(x, y) = -y + 9x \geq 1 \end{aligned} \tag{4.10}$$

From the constraint functions g_1 and g_2 we can see that there is only a subset of the design space has been allowed for a feasible output. The design space is shown in figure C.7 in the appendix. Because of the objective functions are designed to be minimized it helps to view the response surface so that we can see how the design variables x and y change each objective. The responses for each function can be seen in figures 4.1 and 4.2. From both the f_1 and the output response, we see than the lowest possible value of x is desired. However from f_2 we see that a larger value of x is desired. This requires a tradeoff between x and y design variables in order to find compromise between these functions. The relationship between the two output functions can be seen in the Pareto efficiency graph in figure 4.4. In this case we can see that the minimum value of f_1 occurs when f_2 is almost nine. On the other hand we see that f_2 is minimum when f_1 is at its peak. Any combination of design variables which results in a solution of response variables which land on this Pareto front are considered to be optimal solutions as there is no longer a point where you can decrease the output of one response without increasing the response of another. The relation between the two objective functions can be see in figure 4.3 This is a useful tool as it minimizes the possible Pareto-optimal options for a set of given

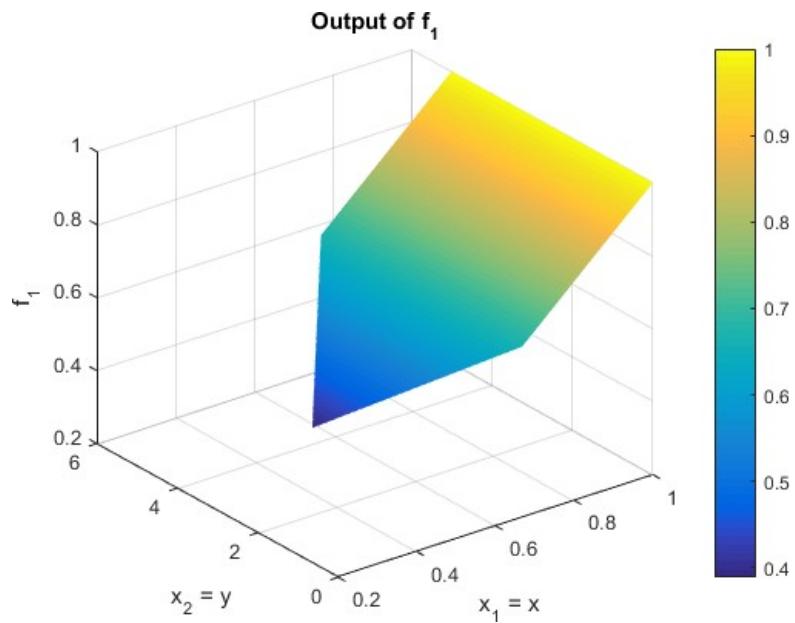


Figure 4.1: Response of output variable f_1 based on design space.

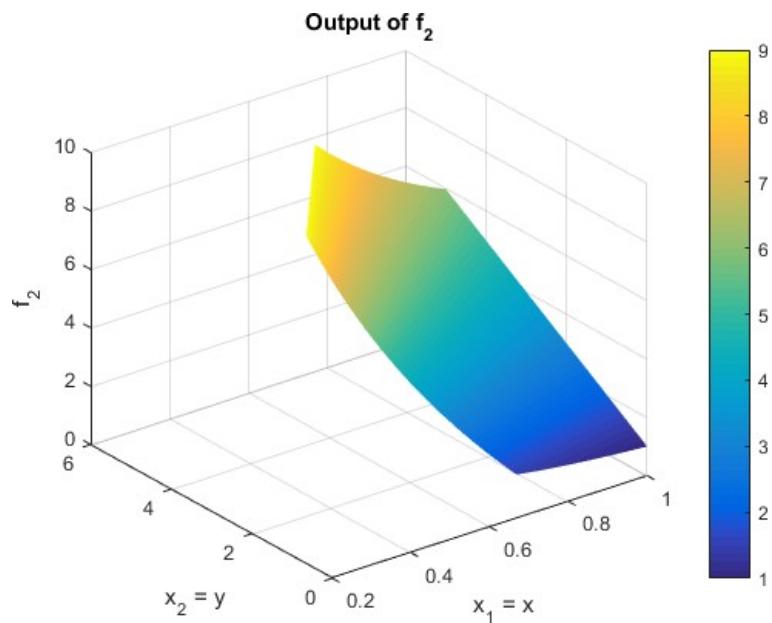


Figure 4.2: Output of the secondary objective function f_2 .

constraints and objective functions. When running the optimizer it is expected to get a local solution that is on or very close to the Pareto front.

For the optimization in choice the KS function is used to consolidate the objectives and constraints into a singular unconstrained minimization function which we can then solve for. For this example we need to rewrite the constraints in the form $Ax + B \leq 0$ and scale the objective functions f_1 and f_2 . This can be shown below in the equations 4.13, 4.14, 4.11 and 4.12. The scaled objective function is simply the value of the objective function divided by the value of the objective function at the start of each KS iteration, subtracting the maximum constraint value at the start of an iteration plus one. The initial value for the starting iteration is shown below for the initialization values of $x = 0.35$ and $y = 2.5$.

$$F_1 = \frac{f_1(x)}{f_1(x_0)} - 1 - \max(g_{i,o}) = \frac{0.35}{0.35} - 1 - \max(11.25, 1.65) = -11.25 \quad (4.11)$$

$$F_2 = \frac{f_2(x)}{f_2(x_0)} - 1 - \max(g_{i,o}) = \frac{10}{10} - 1 - \max(11.25, 1.65) = -11.25 \quad (4.12)$$

$$F_3 = -9x - y + 6 \leq 0 \quad (4.13)$$

$$F_4 = -9x + y + 1 \leq 0 \quad (4.14)$$

This can then be combined to create the KS function which will be used in the KS optimization routine. This function is evaluated and its optimization envelope minimized while the optimization routine searches the design space. This composite KS function for this benchmark problem is shown below in equation 4.15.

$$KS(x) = \max(F_1, F_2, F_3, F_4) + \frac{1}{\rho} \ln \prod_{i=1}^4 e^{\rho F_i - \max(F_1, F_2, F_3, F_4)} \quad (4.15)$$

From the From equations 4.11 and 4.12 it is immediately apparent that the initialization is actually outside of the design space based on the constraints, however this does not pose a problem for the KS optimization algorithm. While the

function may not converge to a global minimum, it will provide a solution which is a local compromise between the objective functions and within the feasible design space. This is illustrated in figure C.8, located in the appendix, where the found minimum value of the constructed KS function is on the Pareto front and is a feasible solution. Due to the simplicity of this problem only a small portion of the OpenMDAO framework was needed. The benchmark example was ran through the pyOpt package utilizing the builtin KSOPT functionality. This routine was originally shown by Wrenn but has been added to the pyOpt package by Perez [36, 34]. From this optimization benchmark we can see that it is possible to find solutions which provide compromise from multiple objectives. The process used in this section will be performed for each individual subsystem and mission design for the nanosatellite mission in order to look for a valid design in the satellites design space.

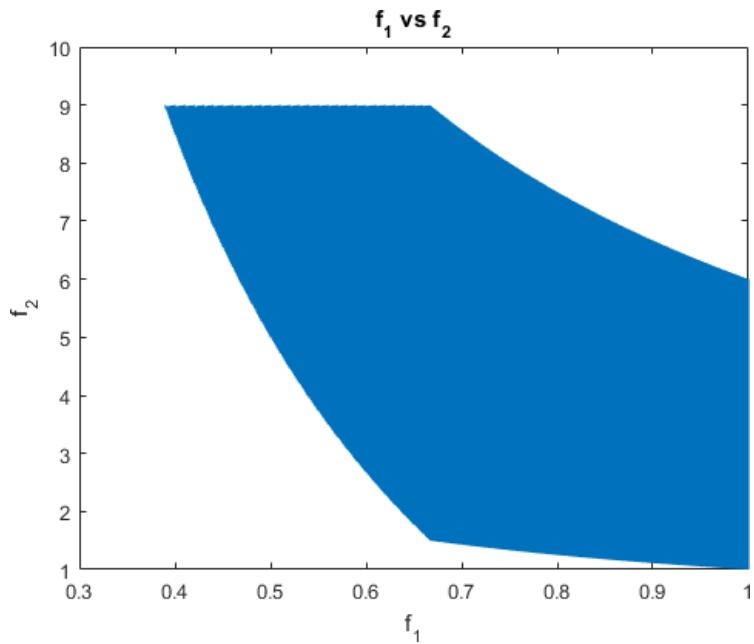


Figure 4.3: Output of f_1 and f_2 for the same input variables x and y .

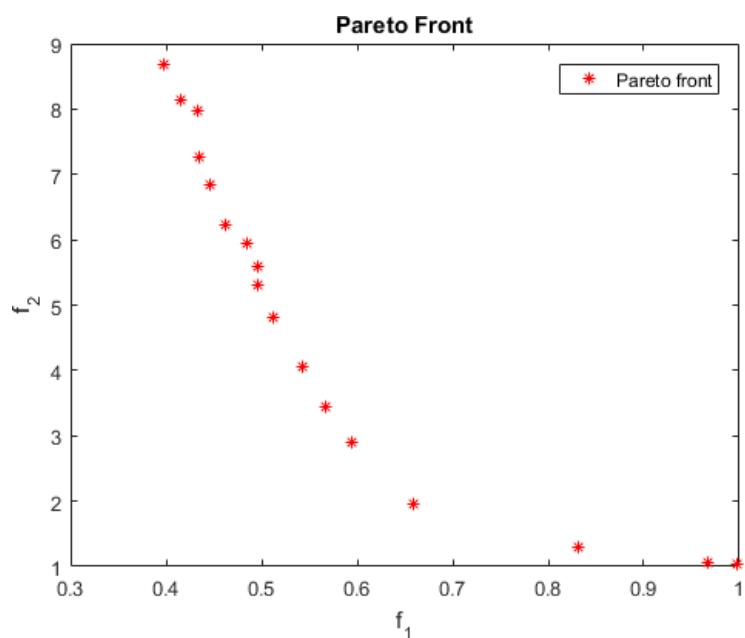


Figure 4.4: Pareto front of benchmark response variables f_1 and f_2 .

Chapter 5

DESIGN OF EXPERIMENT AND OPTIMIZATION ANALYSIS

The following subsection give an overview of the DoE analysis as well as the results from the optimization codes.

5.1 Payload

By using the design equations for a passive optical payload, a design space exploration was done using reasonable extreme values to see the interaction of factors at their most extreme. In this case a 5^8 full factorial DoE was performed in order to see the extremes as well as the median values. All DoE plots are scaled to their orthogonal coded factor level. For all plots along the diagonal, -1 represents the lowest value in the design space and +1 represents the highest value in the design space. For all interactions plots ($j \times i$) the far left value of negative one consists of factors at their extreme opposite ends (i.e. the highest from i and the lowest from j), while the values on the far left (i.e. the highest i and highest j) represent the extreme ends on the upper or lower bounds. This can be understood more clearly in the table below. The outside bounds (top row and first column) are the factor levels. The interaction effect ($i \cdot j$) is plotted against the response variable in question. For this case only the aperture diameter interaction is shown here. The rest of the DoE scatter plots may be found in Appendix C. The optimization technique has provided the following system sizes. $0.136 \times 0.477 \times 0.0613$ m dimensions in X,Y,Z respectively. An estimated power use of 0.18W and a mass of 0.15 kg. The geometric diffraction limited ground sample distance at nadir = 0° is 88m between

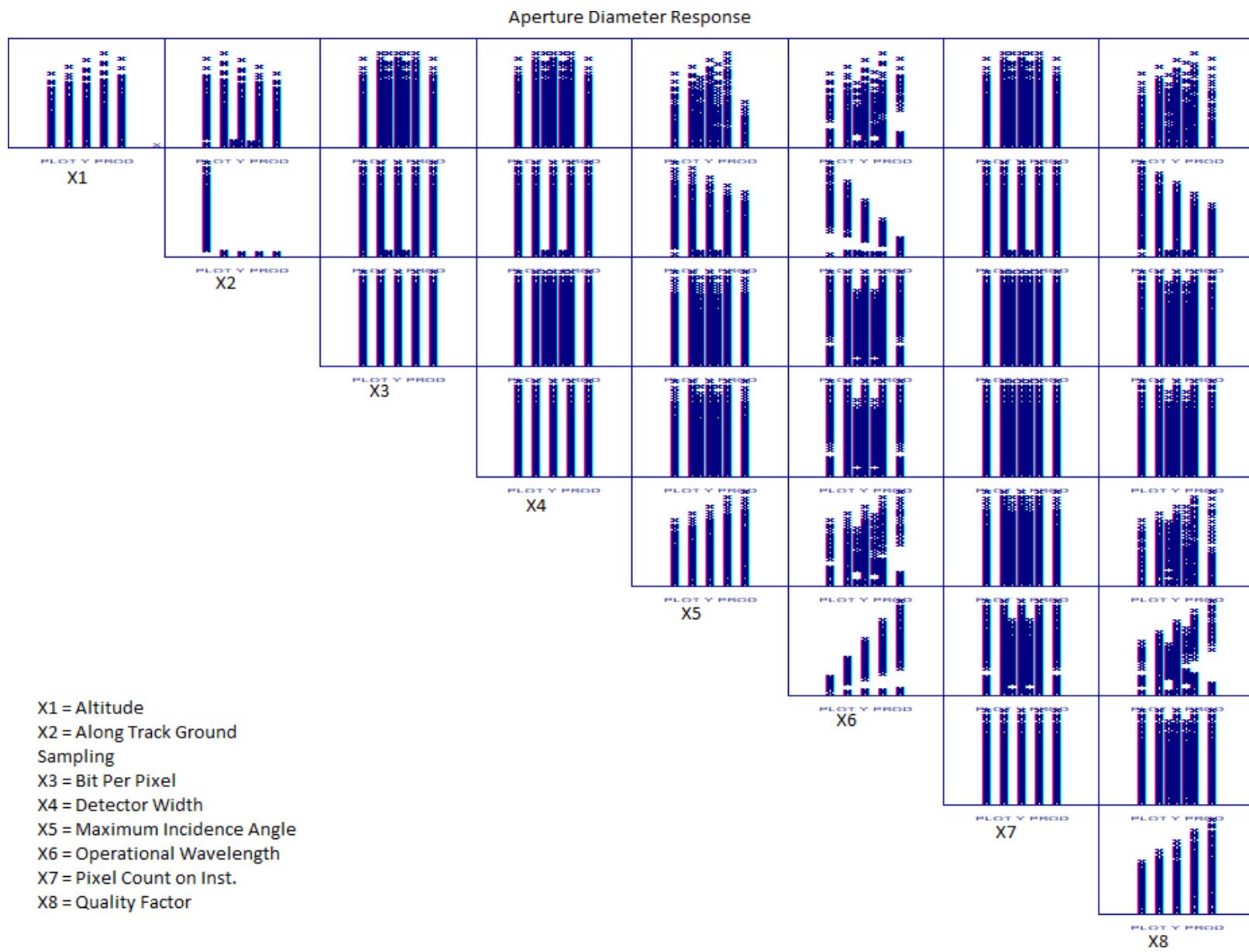


Figure 5.1: DoE scatter plot of Aperture Diameter

Table 5.1: Factor Interaction Chart

Factor Level	-1	-0.5	0	0.5	1
-1	1	0.5	0	-0.5	1
-0.5	0.5	0.25	0	-0.25	-0.5
0	0	0	0	0	0
0.5	0.5	-0.25	0	0.25	0.5
1	-1	-0.5	0	0.5	1

center pixels. The estimated data rate is 2.4 Mbps and the field of view is 0.5 degrees.

5.2 Bus

The following subsections describe the design of experiment and optimizations. DOE scatter plots are provided in Appendix C.

5.2.1 ADCS

The nano-satellite control system can be easily oversized due to the small disturbance torques seen near the launch altitude. In this scenario an altitude of 250 km was selected as a way to determine the sizing for a satellite near the end of its life. The aerodynamic drag and magnetic fields produced the largest amounts of torque which was compensated by small reaction wheels (on the order of 10mm in the z axis and covering the face of 1U. The sizing of reaction wheels and torque rods are dependent on performance requirements for slew rates and momentum saturation and the interaction between the two was not considered. In the case of the star tracker the mass and power were a function of the square of the pointing knowledge, while the physical dimensions scaled linearly. An integrated unit was not considered for this subsystem. The integrated units can provide significantly better results compared to individual products.

Each reaction wheel had an estimated volume of $1180\ mm^3$. The torque rods were approximately $17 \times 17 \times 135\ mm$ (overestimated) with a high magnetic dipole required ($1.5\ A \cdot m^2$). The Star tracker had the largest volume required at $279560\ mm^3$, slightly under 1/3U. The overall estimated power was 1.464 watts for steady operations. The peak power was not considered but can reach in the order of 10 watts per wheel based on data sheets from models chosen in the regression model. The total mass is estimated at 0.672 kg.

5.2.2 C&DH

Most flight qualified hardware is more than capable of running the bare minimum software requirements that is estimated. Using the selection of models from the NASA state of the art technologies report the largest form factor, weight, and typical power was chosen. This resulted in a size of $96 \times 90 \times 12.4\ mm$ and a weight of 0.094 kg. Objective constrained design size:

Chapter 6

MODEL AND SIMULATION ANALYSIS

The current model level is seen in figure 6.1. Only the orbit and line of sight modules have been implemented as of the time of this writing.

6.1 Orbit

Current levels for orbit dynamics include NBodySimulation using the Sun, Earth, Moon, and Juptier. Solar, J2, and atmospheric perturbations have not yet been added. A simulation of the ISS from March 25th 2018 based on data from JPL Horizons has shown good ($\pm 0.0014\%$ difference) agreement for the satellite over the simulation period of one day, a plot of the distances from the center of the earth can be seen in figure 6.2. Solar line of sight and estimated power generation has been recorded but not yet validated.

6.2 Redundancy and Error Detection

The TMR model has been shown to detect discrepancies as long as all three modules have not yet failed. A switching algorithm has been developed to move the failed peripherals from one FPGA to a second FPGA in a reasonable manner however validation of the model on hardware has in progress.

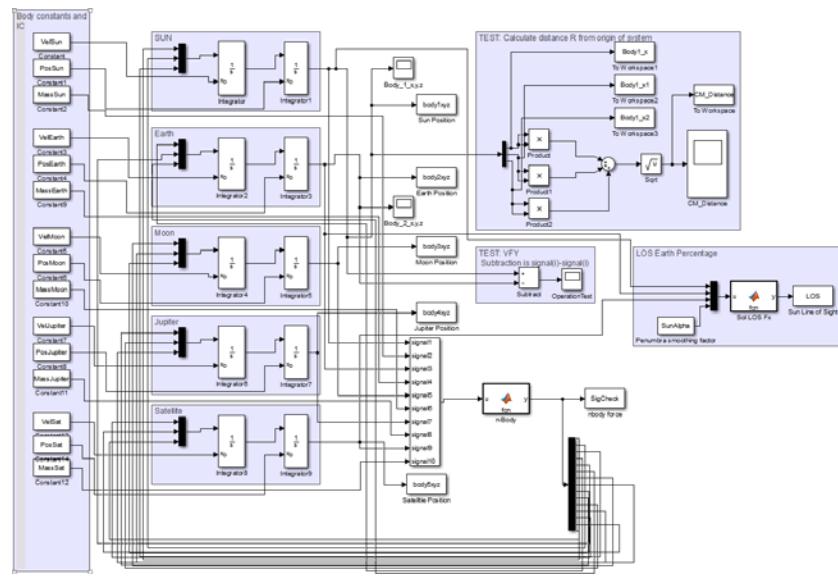


Figure 6.1: Current Simulink Model

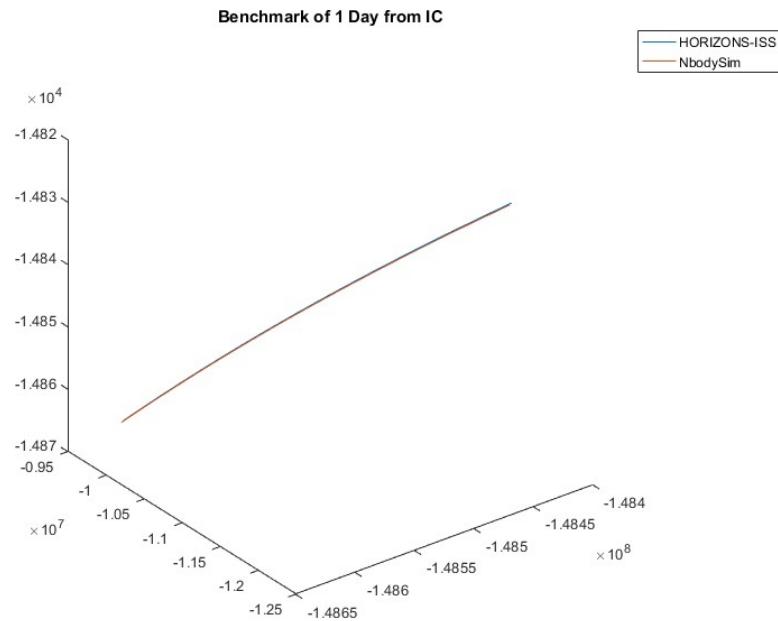


Figure 6.2: ISS Orbit from N-Body sim compared to JPL Horizons log, i.c. March 25, 2018

Chapter 7

PATH FORWARD

High fidelity models of individual subsystems should be integrated into the orbit model. The core of each subsystem model interfaces with the orbit and environmental model and the mission script acts as the OBC controlling the dataflow between the models. The ADCS module will require multiple operating states including detumbling, payload maneuvering, and internal tracking of momentum. The EPS model will consist of power and storage sub modules which will manage electrical states and estimated power draw assuming no faults in the system. The payload simulation model and communication model will require operation when certain objectives are within line of sight. The estimated data (random binary) will need to be stored, fed through the redundancy module too test the fault scheme, and then sent through the communication model to estimate the performance of the communication system. Thermal properties should be monitored in all subsystem modules as small nanosatellites have a small surface area and will be at a higher risk of operating too hot for the stable operating envelope.

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Appendix A

ORBITAL MECHANICS, MANEUVERS, AND MISSION DESIGN

A.1 Cartesian to Keplerian

For any spacecraft which is some distance, ${}^{E_0}\mathbf{r}^{E_0}$, and moving at some speed, ${}^{E_0}\mathbf{v}^{E_0}$ from the central body with gravitational parameter μ , the following method can be used to determine its Keplerian elements. The following vector with Keplerian elements can be calculated using only position, velocity, and central body gravitational variables $[a, e, i, \Omega, \omega, \theta]^T = f(X, Y, Z, v_x, v_y, v_z, \mu)$ using the following set of equations.

$$r = \sqrt{\mathbf{r} \cdot \mathbf{r}} = \sqrt{X^2 + Y^2 + Z^2}$$

$$v = \sqrt{\mathbf{v} \cdot \mathbf{v}} = \sqrt{v_x^2 + v_y^2 + v_z^2}$$

$$\text{Radial velocity } v_r = \frac{\mathbf{r} \cdot \mathbf{v}}{r}$$

$$1 \hat{\mathbf{i}} \quad \hat{\mathbf{j}} \quad \hat{\mathbf{k}}_1$$

$$\hat{\mathbf{h}} = \mathbf{r} \times \mathbf{v} = 1 X \quad Y \quad Z 1$$

$$h = \frac{1 v_x \quad v_y \quad v_z 1}{\hat{\mathbf{h}} \cdot \hat{\mathbf{h}}}$$

$$1 \hat{\mathbf{i}} \quad \hat{\mathbf{j}} \quad \hat{\mathbf{k}}_1$$

$$\hat{\mathbf{N}} = \hat{\mathbf{k}} \times \hat{\mathbf{h}} = 1 0 \quad 0 \quad 1 1$$

$$N = \frac{1 h_x \quad h_y \quad h_z 1}{\hat{\mathbf{N}} \cdot \hat{\mathbf{N}}}$$

$$\mathbf{e} = \frac{1}{\mu} v^2 - \frac{\mu}{r} \mathbf{r} - r v \mathbf{v}$$

$$\begin{aligned}
e &= \sqrt{\mathbf{e} \cdot \mathbf{e}} \\
i &= \cos^{-1} \frac{h_z}{h} \\
\Omega &= \begin{cases} \Omega & (N \geq 0) \\ 360^\circ - \cos^{-1} \frac{N_x}{N} & (N_Y < 0) \end{cases} \\
\omega &= \begin{cases} \omega & (e_z \geq 0) \\ 360^\circ - \cos^{-1} \frac{\hat{\mathbf{N}} \cdot \mathbf{e}}{Ne} & (e_z < 0) \end{cases} \\
\theta &= \begin{cases} \theta & (v \geq 0) \\ v - 360^\circ & (v < 0) \end{cases} \\
a &= \frac{(v - \Omega) + e \cos(\theta)}{1 - e^2}
\end{aligned}$$

A.2 Keplerian to Cartesian

Similarly from the transformation from Cartesian to Keplerian, the reverse is also true. In this case we can also take advantage of the Perifocal frame in order to simplify the transformations. In this case we will go from the planets grid and apply rotation matrices for the Ω , i , and ω using rotational matrices ${}^{EC} \omega^{EC^I}$, ${}^{EC^I} \omega^{EC^{II}}$, and ${}^{EC^{II}} \omega^P$ respectively.

$$\begin{aligned}
{}^{EC} \omega^{EC^I} &= \begin{pmatrix} 0 & -\sin(\Omega) & \cos(\Omega) \\ \cos(\Omega) & 0 & \sin(\Omega) \\ \sin(\Omega) & -\cos(\Omega) & 0 \end{pmatrix} \\
{}^{EC^I} \omega^{EC^{II}} &= \begin{pmatrix} 0 & \cos(i) & \sin(i) \\ 0 & \sin(i) & -\cos(i) \\ -\sin(i) & \cos(i) & 0 \end{pmatrix}
\end{aligned}$$

$$\begin{matrix} & & & \\ & \cos(\omega) & \sin(\omega) & 0 \\ \begin{matrix} & -\sin(\omega) \\ & \cos(\omega) \end{matrix} & 0 & 1 \end{matrix}$$

$${}^{EC}{}^I \boldsymbol{\omega}^P = \begin{bmatrix} & & \\ & 0 & \\ & 0 & 1 \end{bmatrix}$$

We now multiply through the rotations matrices from ECI to P (Ω, i, ω) in order to obtain the full transform for ECI to P, ${}^{EC}\boldsymbol{\omega}^P$. Because all three rotational matrices are orthogonal we can take the transpose of the full transformation matrix to obtain

P to ECI.

$$\begin{matrix} & & & \\ & \cos(\Omega) \cos(\omega) - \sin(\Omega) \cos(i) \sin(\omega) & \sin(\Omega) \cos(\omega) + \cos(\Omega) \cos(i) \sin(\omega) & \sin(i) \sin(\omega) \\ \begin{matrix} & -\cos(\Omega) \sin(\omega) - \sin(\Omega) \cos(i) \cos(\omega) \\ & \sin(\Omega) \sin(i) \end{matrix} & \begin{matrix} \cos(\Omega) \cos(i) \cos(\omega) - \sin(\Omega) \sin(\omega) \cos(\omega) \sin(i) \\ -\cos(\Omega) \sin(i) \end{matrix} & \begin{matrix} \cos(i) \\ \cos(\omega) \sin(i) \\ \cos(\omega) \sin(i) \end{matrix} \\ & & \\ & \cos(\Omega) \cos(\omega) - \sin(\Omega) \cos(i) \sin(\omega) & -\cos(\Omega) \sin(\omega) - \sin(\Omega) \cos(i) \cos(\omega) & \sin(\Omega) \sin(i) \\ {}^P\boldsymbol{\omega}^{EC} = \begin{matrix} & \sin(\Omega) \cos(\omega) + \cos(\Omega) \cos(i) \sin(\omega) \\ & \sin(i) \sin(\omega) \end{matrix} & \begin{matrix} \cos(\Omega) \cos(i) \cos(\omega) - \sin(\Omega) \sin(\omega) \\ \cos(\omega) \sin(i) \end{matrix} & \begin{matrix} -\cos(\Omega) \sin(i) \\ \cos(i) \end{matrix} \end{matrix}$$

At this point it is now necessary to find the ${}^P_0\mathbf{r}^{SC}$ and ${}^P_0\mathbf{v}^{SC}$ vectors in the Perifocal frame, and then we can use the transform matrix ${}^P\boldsymbol{\omega}^{ECI}$ to find the reference system Cartesian coordinates and velocity.

$$\begin{matrix} & & & \\ & \cos(\theta) & & \\ \begin{matrix} h^2 \\ \mu 1 + e \cos(\theta) \\ \sin(\theta) \end{matrix} & & & \\ & & 0 & \\ & -\sin(\theta) & & \\ \begin{matrix} \mu \\ h \\ e + \cos(\theta) \end{matrix} & & & \\ & 0 & & \end{matrix}$$

$$[r_{EC}, v_{EC}]^T = [{}^P\boldsymbol{\omega}^{EC}][\mathbf{r}]^T, [{}^P\boldsymbol{\omega}^{EC}][\mathbf{v}]^T]^T$$

A.3 Lambert's Problem

Lambert's problem is an important orbital mechanics problem which determines the orbit from two position vectors and a time of flight between points ${}^{EC_0}\mathbf{R}^A$ and ${}^{EC_0}\mathbf{R}^B$. The method for solving the problem is important in mission design, specifically in areas regarding targeting and fuel use optimization, due to finding necessary impulses to change trajectories to the target point in space. This is solved for our problem using the universal variable method.

A.4 Atmospheric Drag - Density

Density calculated from table below from [38]. The expected values are a reasonable comparison relatively well with the 1976 standard atmospheric model and provide an estimate for the density. This method was used in the design space exploration due to the ease of implementation, however will be replaced by a more numerically intensive model in the simulation model. The simple atmospheric model can calculate the estimated density by finding the correct base altitude, density and scale height and placing the correct values into equation A.1.

$$\rho_{altitude} = \rho_0 \cdot e^{\frac{h_0 - Z}{H}} \quad (A.1)$$

A.5 E_bN_o Derivation

$$\frac{E_b}{N_o} = \frac{P L_l G_t L_s L_a G_r}{k T_s R} \quad (A.2)$$

Power flux of a sphere for an isotropic antenna can be found as

$$W_f = \frac{PL_l}{4\pi r}$$

Table A.1: Simple Atmospheric Model Data from [38]

Altitude Z (km)	Base Altitude h_0 (km)	Density $\rho_0(\frac{\text{kg}}{\text{m}^3})$	Scale Height H (km)
0	0.00	1.23	7.25
25	25.00	3.899e-2	6.35
30	30.00	1.774e-2	6.68
40	40.00	3.972e-3	7.55
50	50.00	1.057e-3	8.38
60	60.00	3.206e-4	7.71
70	70.00	8.770e-5	6.55
80	80.00	1.905e-5	5.80
90	90.00	3.396e-6	5.38
100	100.00	5.297e-7	5.88
110	110.00	9.661e-8	7.26
120	120.00	2.438e-8	9.47
130	130.00	8.484e-9	12.64
140	140.00	3.845e-9	16.15
150	150.00	2.070e-9	22.52
180	180.00	5.464e-10	29.74
200	200.00	2.789e-10	37.11
250	250.00	7.248e-11	45.55
300	300.00	2.418e-11	53.63
350	350.00	9.518e-12	53.30
400	400.00	3.725e-12	58.52
450	450.00	1.585e-12	60.83
500	500.00	6.967e-13	63.82
600	600.00	1.454e-13	71.84
700	700.00	3.614e-14	88.67
800	800.00	1.170e-14	124.64
900	900.00	5.245e-15	181.05
1000	1000.00	3.019e-15	268.00

The transmitter gain is defined as the ratio of power at the center of the antenna coverage area compared to the theoretical omnidirectional antenna. Effective isotropic radiated power (EIRP) in watts is used to state the effective power of the antenna and is defined as

$$EIRP \stackrel{\text{def}}{=} PL_l G$$

which results in the effective power flux density of the antenna as

$$W_f = \frac{(EIRP)L_a}{4\pi R_r^2}$$

The received power is power flux of the transmitting antenna times the cross sectional area of the receiving antenna and the antenna efficiency.

$$C = W_f \frac{\pi D^2}{4r} \eta_r = \frac{PL_l G_t L_a D^2 \eta_r}{16r^2}$$

The receiving antenna also has a gain for a given wavelength, λ , which can be defined as

$$G_r = \frac{\pi D^2 \eta_r}{4} \frac{4\pi}{\lambda^2} = \frac{\pi^2 D^2 \eta}{\lambda^2}$$

The free space path loss (FSPL) is a loss value which is expressed as the reciprocal of gain and defined as

$$\frac{4\pi R_r^2}{\lambda^2}$$

This allows us to define space loss, L_s , as the inverse of FSPL and integrate it into the received power equation and now we see

$$C = P L_t G_t L_a G_r = (EIRP) L_s L_a G_r$$

In dB form the energy per bit to noise density ratio can be written as

$$\frac{E_b}{N_o} = P + L_t + G_t + L_{pt} + L_{pr} + L_s + L_a + G_r + 228.6 - 10 \log T_s - 10 \log R$$

with P in dBW, T_s in K, R in bps, and $10 \log k = -228.6 \text{ dBW}/(\text{Hz} \cdot \text{K})$, and the rest of the terms in dB.

Appendix B

REQUIREMENTS DOCUMENT

26-Oct-17

Requirements are grouped by WBS level and contained in separate tab sheets below. The Program Level 1 requirements are also provided in a separate tab for reference. Trac, allocation and V&V method is shown for each requirement. V&V methods are:
T=Test, D=Demonstration, A=Analysis, I=Inspection

RQMT ID	REQUIREMENT	TRACEABILITY	ALLOCATION				Verification Method		Verification Document(s)	Rationale/Comment
			T	D	A	I				
1.0	GEN SAT MISSION OBJECTIVE									
L1-PTD-01	The purpose of the GenSat is to demonstrate a semi-reconfigurable satellite which can demonstrate new MMR technologies.	Project-wide								
RQMT ID	REQUIREMENT	TRACEABILITY	ALLOCATION	Verification				Verification Document(s)	Rationale/Comment	
2.0	Mission and Technology Requirements			T	D	A	I			
2.1	Mission Hardware									
2.2	Mission Operations									
2.3	Environmental Requirements and Launch Provisions									
2.4	Mission and Satellite Reliability									
2.5	Payload and Spacecraft Disposal Orbit Debris, Re-entry Limits									
RQMT ID	REQUIREMENT	TRACEABILITY	ALLOCATION	Verification				Verification Document(s)	Rationale/Comment	
3.0	Payload Requirements			T	D	A	I			
3.1	Payload Requirements									
3.1.1	The Payload shall not exceed the total volume defined in the Spacecraft to Payload ICD.	Payload			X	X			The exact volume and locations will be negotiated at formation of the ICD.	
3.1.2	The Payload developer shall document the measured thrust direction, variability, and location of thrust relative to reference system as documented in the Spacecraft to Payload ICD.	Payload		X		X			Document forces that will be produced by the Payload thrust.	
3.1.3	The Payload shall conform to CG and total mass limits specified in the Spacecraft to Payload ICD.	Payload			X	X			Payload mass allocation and CG issues will be negotiated at ICD formation	
3.1.4	The Payload shall be capable of operating from spacecraft-supplied power as specified in the Spacecraft to Payload ICD.	Payload		X		X			The exact voltage and whether unregulated or regulated will be negotiated at formation of the ICD.	
3.1.5	The Payload shall be configured to communicate signals and data to the Flight System as specified in the Spacecraft to Payload ICD.	Payload		X		X			Most likely RS-422 asynchronous	
3.1.6	The Payload shall support a 180 day mission lifetime on orbit.	Payload				X			Operation on orbit could be as long as 180 days. Not meant to infer a 180 day continuous firing capability, but that the payload could be utilized off and on during a 180 day period.	
3.1.7	The Payload shall be thermally controlled as specified in the Spacecraft to Payload ICD.	Payload		X		X			The intent of this requirement is to have the Flight system provide some thermal control support for the Payload.	
3.1.9	The Payload shall be capable of being powered off for launch and powered on by the Spacecraft at any time during the flight.	Payload				X			Power supply interface from Payload will be switched	
3.1.10	The Payload shall provide harnesses and cabling for the Payload System as specified in the Spacecraft to Payload ICD.	Payload		X					The definition of the exact cable/harness interface, as well as cable routing, will be negotiated in the Spacecraft to Payload ICD	
3.1.11	The Payload shall be responsible for supplying mounting structures as specified in the Spacecraft to Payload ICD.	Payload				X			Exact interface definition will be negotiated and documented in a Spacecraft to Payload ICD.	
3.1.12	The Payload shall provide a simulator of the Payload to support System Integration testing.	Payload		X		X			Support electrical, command and control interfaces to allow for integration testing .	
3.1.13	The Payload shall be able to acquire Health and Status information from its instruments.	Payload		X					Necessary to monitor status of subsystem and for diagnostics.	
3.1.14	The Payload shall be able to provide Health and Status information for the Payload to the Spacecraft as specified in the Spacecraft to Payload ICD.	Payload, Vendor			X				Necessary to send H&S information to the GDS for analysis and review.	
3.1.15	The Payload shall provide engineering telemetry sufficient for MOC to determine the quantity of propellant remaining to within 5% (TBR).	Payload, Vendor, MOC				X			Provide data to determine propellant level, e.g. firing times that can be correlated with lookup tables on the ground.	
3.1.16	The Payload shall provide engineering telemetry sufficient for MOC to determine the thruster performance ISP within 5% (TBR).	Payload, Vendor				X			Provide data to model thruster performance to calculate future thrust command durations. The Spacecraft provides engineering telemetry to measure orbit change. Engineering telemetry may be combined with lookup tables or ground analysis to determine actual ISP, the requirement is to make sure whatever data is needed on thruster operation is provided	

3.1.17	The Payload shall provide a safe plug to inhibit unsafe operation on the ground per the electrical interface in the Spacecraft to Payload ICD.	Payload, Vendor	X	X	S&MA safety requirement (and probably also the LV) to physically prohibit a thruster being activated.
3.1.18	Payload bus solution shall provide Payload electrical interfaces as specified in the Spacecraft to Payload ICD.	Payload, Vendor	X	X	
3.1.19	Payload bus solution shall provide Payload mechanical interfaces as specified in the Spacecraft to Payload ICD.	Payload, Vendor	X	X	
3.1.20	Payload bus solution shall provide Payload thermal interfaces as specified in the Spacecraft to Payload ICD.	Payload, Vendor	X	X	
3.1.21	Payload bus solution shall provide Payload communication interfaces as specified in the Spacecraft to Payload ICD.	Payload, Vendor	X	X	
3.1.22	Payload shall provide and EIDP upon delivery containing: •Propulsion System Specs •Propulsion System Drawings (MICD/EICD) •Propulsion Assembly/Handling Procedures •Propulsion System Limits/Constraints •Propulsion System Test Data and Scripts •Propulsion System CMD/TLM Requirements •Propulsion System Acceptance Test Procedures	Payload		X	
3.1.23	The Payload shall provide EMI/EMC test data and analysis (TBD).		X	X	Need to define specifics. Looking for self-compatible, measured output provided to SC vendor, and documenting any particular sensitivities that may disrupt thruster operation.
3.1.24	The Payload shall be shipped to the spacecraft vendor appropriately packaged in a shipping container.	Payload		X	
3.1.25	The Payload developer will provide any required GSE necessary for I&T and/or LV integration of the Payload.	Payload		X	

RQMT ID	REQUIREMENT	TRACEABILITY	ALLOCATION	T	D	A	I	Verification Document(s)	Rationale/Comment
4.0	Bus Functional Requirements								
4.1	Attitude Determination and Control								
4.1.1	GenSat shall be capable of producing tracking and ephemeris solutions based on collected GPS telemetry from the spacecraft.	MOC		X	X				Use of GPS locations and timestamps from sub MEO altitudes in orbit can be used to determine the orbital elements of the satellite.
4.1.2	GenSat shall be capable of selectively transmitting stored telemetry upon command of the MOC.	Vendor			X				
4.2	Propulsion Management and Control								
4.2.1	The GenSat project team shall provide a flatsat demonstration unit with the ability to demonstrate MMR technologies at the hardware, data bus, and software levels	Project-wide			X	X			
4.3	Command and Data Handling								
4.3.1	GenSat bus shall provide bidirectional communication with the Payload	Vendor							
4.3.2	GenSat shall be capable of providing telemetry defining the state of any quantity or function monitored or capable of being updated by the FSW.	Vendor				X			
4.3.3	GenSat shall monitor SC elements necessary for the MOC to assess the state of the spacecraft.	Vendor				X			
4.3.4	GenSat shall be capable of transmitting any or all of its memory contents on command by MOC.	Vendor		X		X			
4.3.5	All clocks shall be synchronized within less than TBD seconds. Time slips and timestamp errors due to CPU interrupts or other sources shall be corrected or prohibited by design.	Vendor			X				
4.4	Condition Sampling and Reporting Functions								
4.4.1	GenSat shall monitor temperatures of critical subsystem components throughout the mission. Temperature sampling and storage shall occur at least once per hour following on-orbit deployment.				X				
4.4.2	Current from the Payload, Main Transponder, and Beacon Transmitter subsystems shall be recorded at least 3 times per orbit				X				
4.4.3	Accuracy current of recording shall be no less than 1/50 the expected peak value.				X				
4.4.4	The voltage of the satellite's batteries shall be recorded at least once per minute following deployment for both sunlight and eclipse phases and during any pre-launch checkout operations.				X				
4.5	Communications								
4.5.1	The Spacecraft shall be capable of radiating telemetry to the ground at a rate and duration able to downlink 250Mbps per day.	Vendor			X	X			

4.5.2	The Spacecraft shall be capable of radiating telemetry to the ground with greater than 3db link margin.	Vendor	X	X
4.5.3	GenSat shall radiate telemetry on a specified S-band frequency.	Vendor	X	
4.5.4	The Spacecraft shall be capable of maintaining TLM transmission while performing payload system characterization.	Vendor		X
4.5.5	The Spacecraft shall be capable of operating payload and transmitting data at full rate during eclipses up to 20min.	Vendor	X	X

4.6 Fault Detection Isolation and Recovery				
4.6.1	After a power outage and restart, the PharmaSat Bus shall be capable of returning to its previous operating state and resuming normal operations without loss of previously stored mission data.	Project-wide		X
4.6.2	Spacecraft subsystem shall be capable of isolating subsystems from controllable critical faults (CCF) in a single subsystem are resetable faults in orbit and have potentially catastrophic effects on system performance	Project-wide		X
4.6.3	Single Event Upsets of dynamic memories (RAM) shall be detected and corrected. Memory errors shall be removed and any related system function should be fully recoverable.	Project-wide	X	
4.6.4	GenSat shall use an error-correcting memory solution to help ensure memory integrity.	Vendor	X	X

4.7 Power Management Functions				
4.7.1	The power generation function shall be capable of providing one-time system power surge of up to 5 watts during the eclipse time of the first orbit.	Vendor	X	X
4.7.2	The GenSat shall provide protection, battery charging and conditioning, and temperature control for the batteries to ensure acceptable battery charging and discharging cycle life throughout the mission timeline.	Vendor	X	X

4.8 Thermal Control				
4.8.1	The GenSat project team shall provide a flatsat demonstration unit with the ability to demonstrate MMR technologies at the hardware, data bus, and software levels	Project-wide	X	X

Appendix c

**BACKUP GRAPHS, CHARTS AND IMAGES, AND MATLAB
PUBLISHED CODE**

Contents

- Define Custom Fit Functions
- Max Torque Data Scatter
- Max Momentum Capacity & Regression
- RxWheel Regression
- RxWheel Torque Regression Models
- RxWheel Momentum Regression Models
- Magnetorquer Data
- Magnetorquer Graphs (All Linear)
- Magnetorquer Regression
- Star Tracker Data
- Star Tracker Regression
- Magnetometer Data
- Magnetometer Regression
- IMU Data
- IMU Regression
- Regression Functions and Goodness of Fit

```
clc; clear all; close all;
%RXWHEEL DATA: Mass      Power    Xdim     Ydim     Zdim     Peak Torque   Momentum Capacity   Peak Power
RxWheel = [0.96 0.65    109      109      101      0.011    0.42    10;
2.6     1.2      131      131      120      0.11     1.5      113;
0.185   0.3      50       50       40       0.002    0.04     1.8;
0.13    0.6      42       42       19       0.004    0.015    1;
0.24    0.5      58       58       25       0.007    0.05     1;
0.35    0.5      70       70       7        0.007    0.1      1;
0.226   0.9      77       65       38       0.02     0.18     23.4];
```

Define Custom Fit Functions

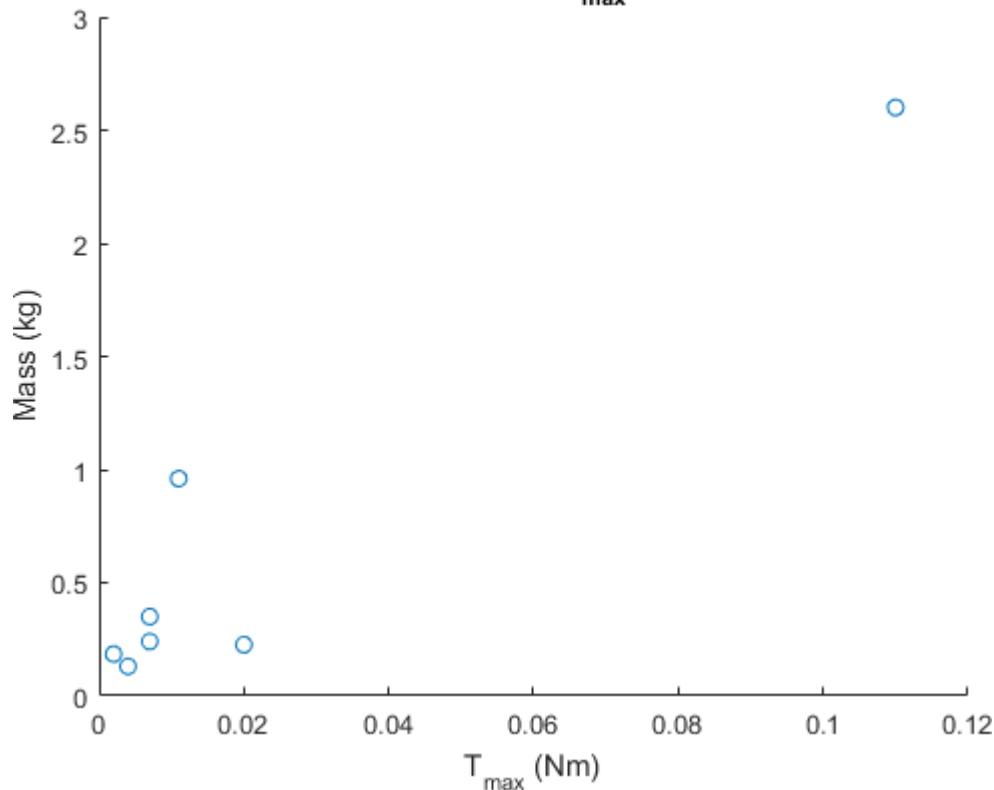
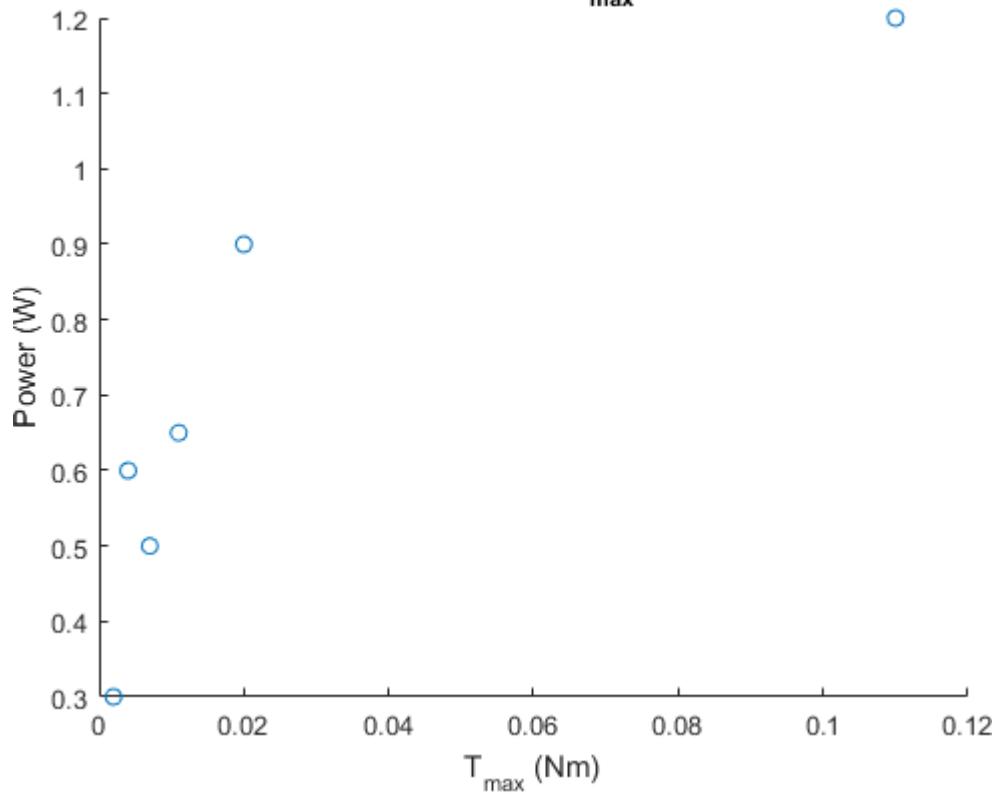
```
LogFit = fittype('a*log(x) + b','dependent',{'y'},'independent',{'x'},...
    'coefficients',{'a','b'})
ExpFit = fittype('a*exp(b*x)', 'dependent',{'y'}, 'independent',{'x'},...
    'coefficients',{'a','b'})
% poly1 = linear
% poly2 = quadratic
```

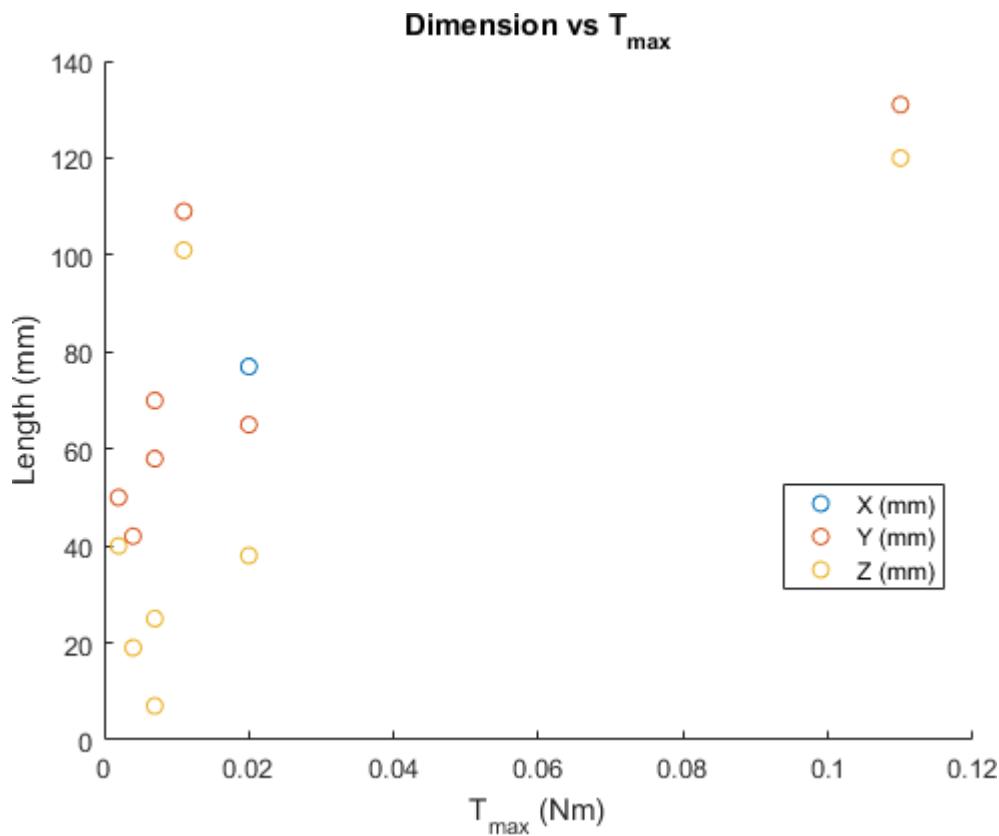
```
LogFit =
General model:
LogFit(a,b,x) = a*log(x) + b
```

```
ExpFit =
General model:
ExpFit(a,b,x) = a*exp(b*x)
```

Max Torque Data Scatter

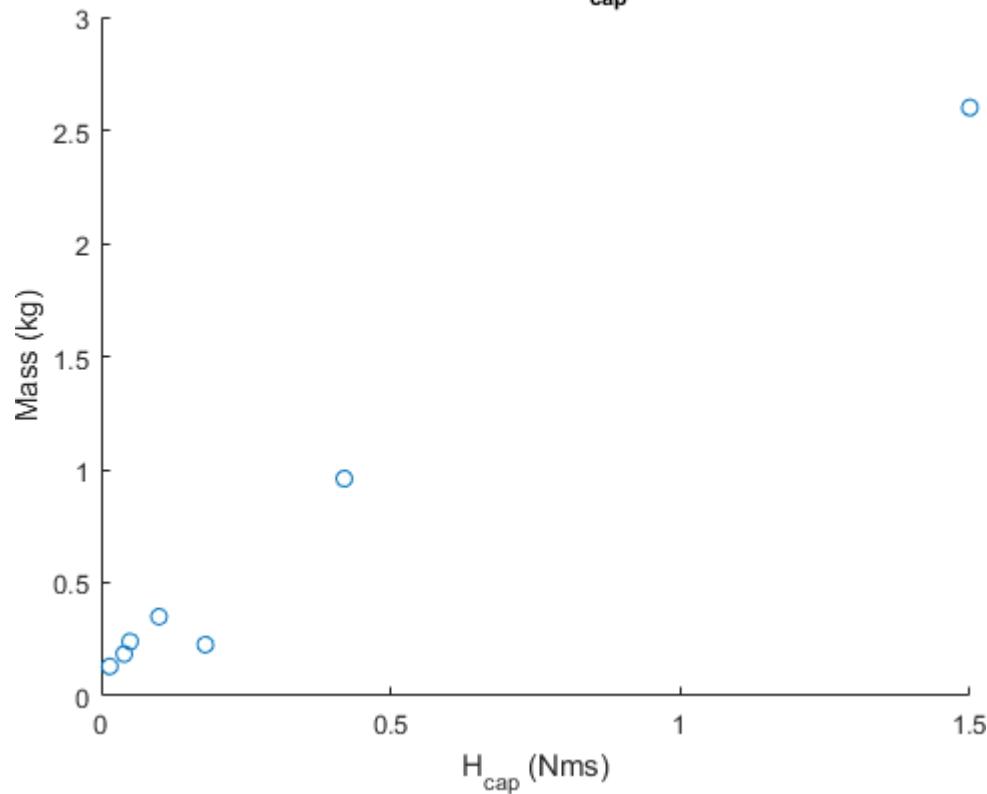
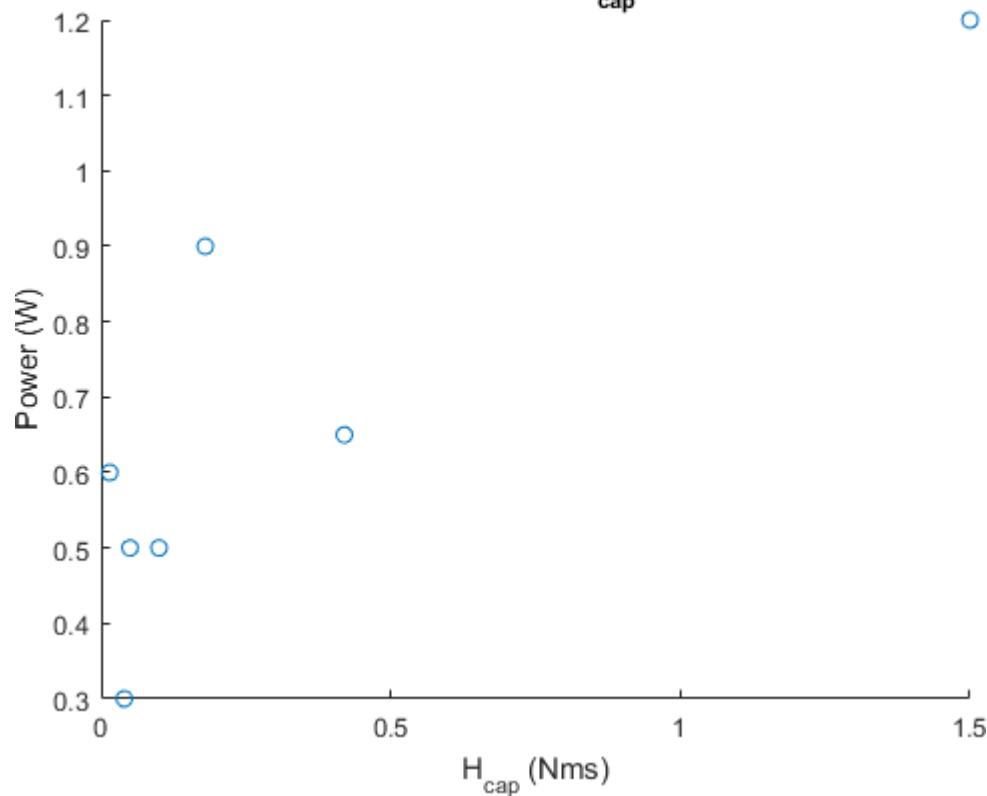
```
%Plot Response vs Independent Variables
%Mass
figure
scatter(RxWheel(:,6),RxWheel(:,1))
title('Mass vs T_{max}')
xlabel('T_{max} (Nm)')
ylabel('Mass (kg)')
%Power
figure
scatter(RxWheel(:,6),RxWheel(:,2))
title('Power vs T_{max}')
xlabel('T_{max} (Nm)')
ylabel('Power (W)')
%Dimensions
figure
hold on
scatter(RxWheel(:,6),RxWheel(:,3))
scatter(RxWheel(:,6),RxWheel(:,4))
scatter(RxWheel(:,6),RxWheel(:,5))
title('Dimension vs T_{max}')
xlabel('T_{max} (Nm)')
ylabel('Length (mm)')
legend('X (mm)', 'Y (mm)', 'Z (mm)', 'location', 'best')
```

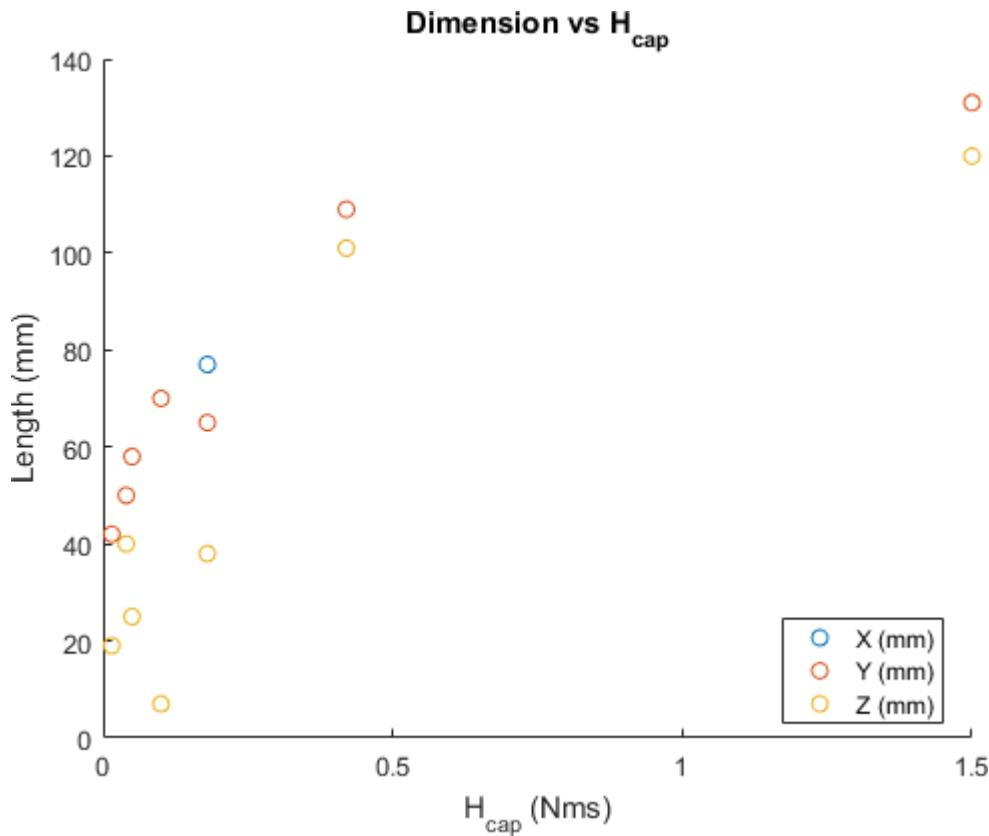
Mass vs T_{max} **Power vs T_{max}** 



Max Momentum Capacity & Regression

```
%Mass
figure
scatter(RxWheel(:,7),RxWheel(:,1))
title('Mass vs H_{cap}')
xlabel('H_{cap} (Nms)')
ylabel('Mass (kg)')
%Power
figure
scatter(RxWheel(:,7),RxWheel(:,2))
title('Power vs H_{cap}')
xlabel('H_{cap} (Nms)')
ylabel('Power (W)')
%Dimesions
figure
hold on
scatter(RxWheel(:,7),RxWheel(:,3))
scatter(RxWheel(:,7),RxWheel(:,4))
scatter(RxWheel(:,7),RxWheel(:,5))
title('Dimension vs H_{cap}')
xlabel('H_{cap} (Nms)')
ylabel('Length (mm)')
legend('X (mm)', 'Y (mm)', 'Z (mm)', 'location', 'best')
```

Mass vs H_{cap} **Power vs H_{cap}** 



RxWheel Regression

From the above graphs we see that the linear dimensions are logarithmic and the power and mass may or may not be linear or exponential.

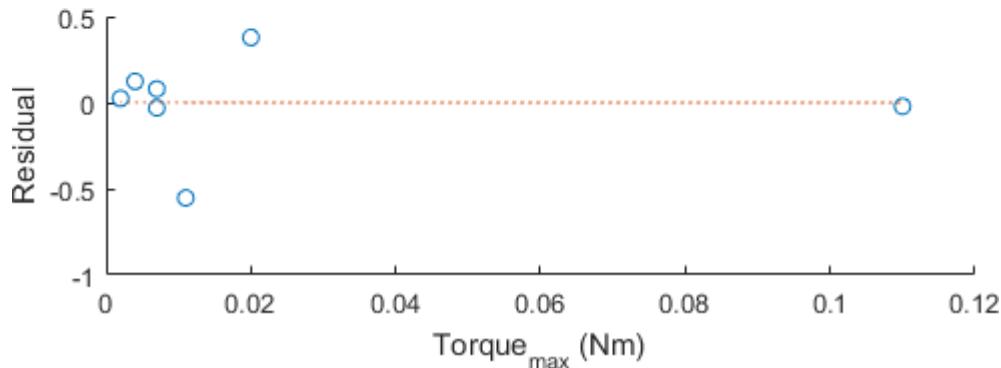
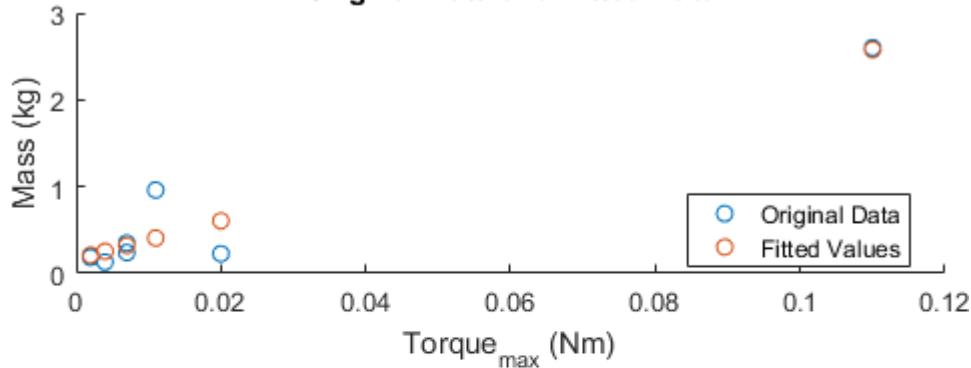
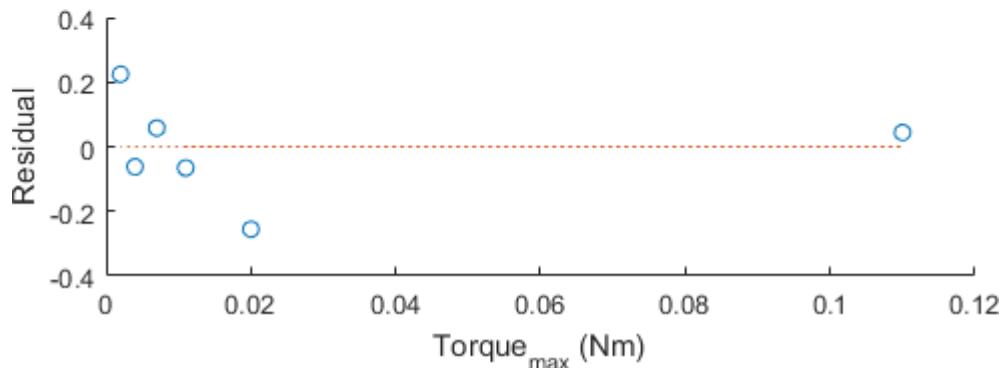
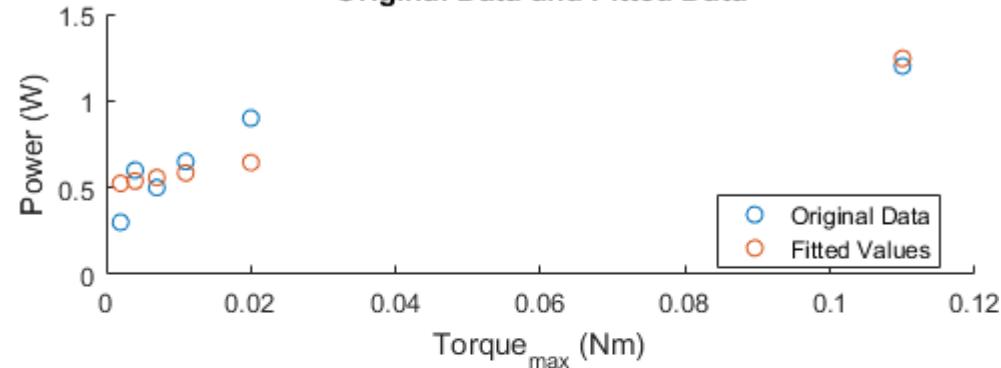
RxWheel Torque Regression Models

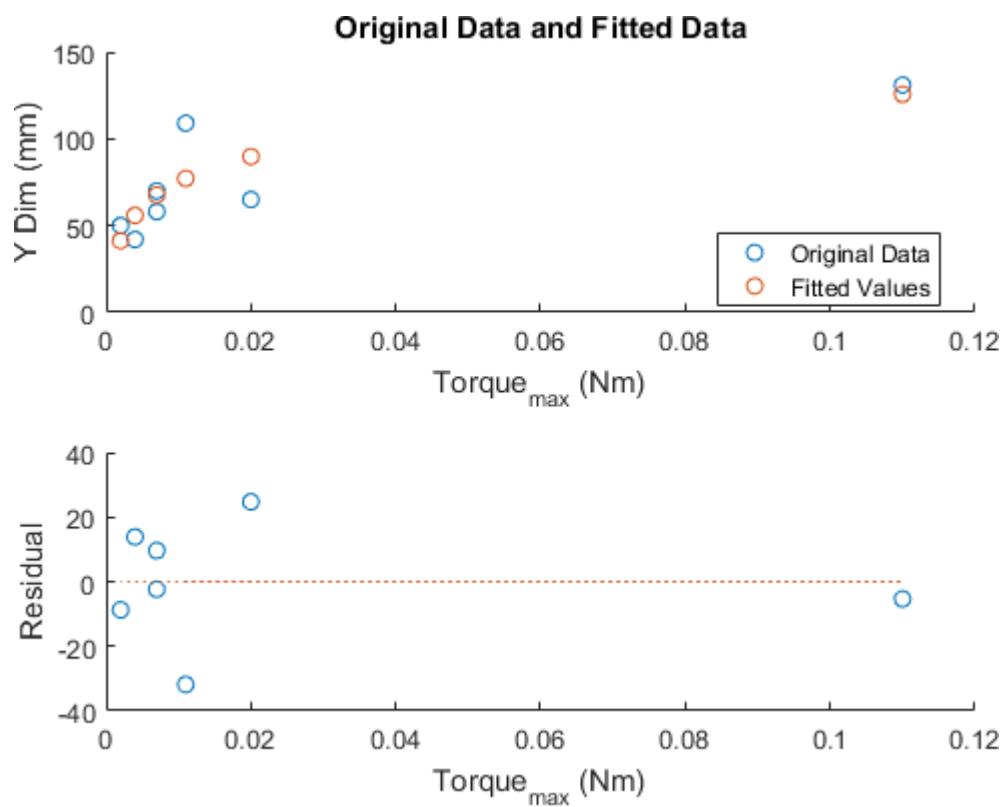
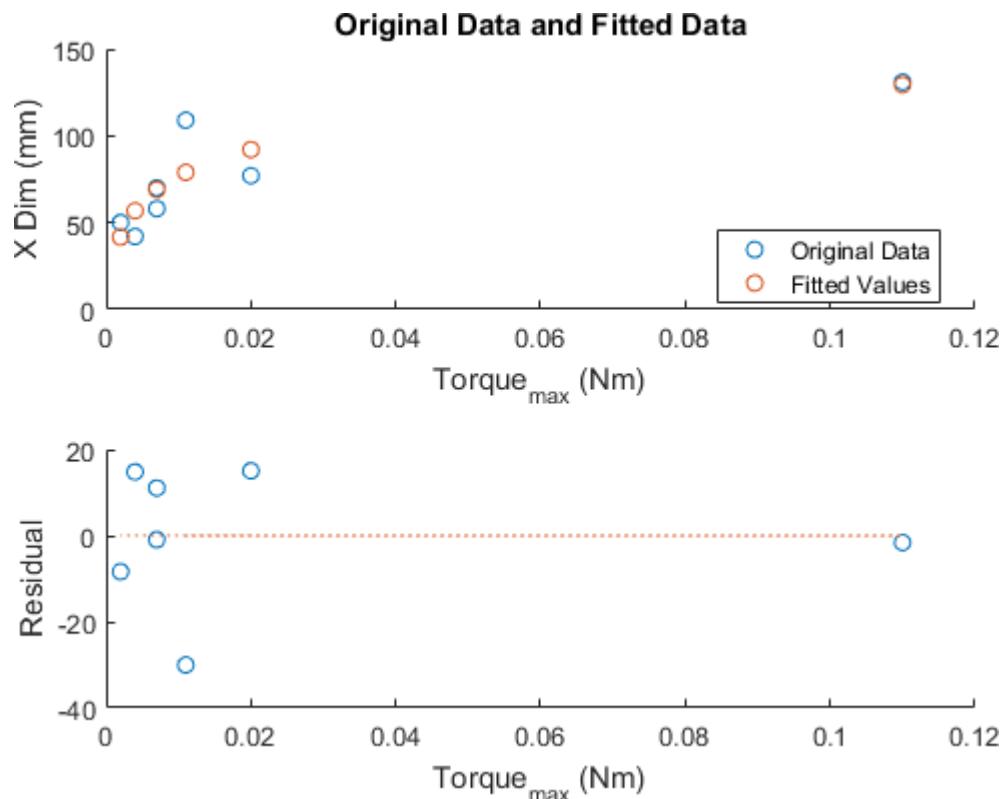
```
[MassT,MassTGOF] = fit(RxWheel(:,6),RxWheel(:,1),'poly1');
[PowerT, PowerTGOF] = fit(RxWheel(:,6),RxWheel(:,2),'poly1');
[XDimFitT, XDimGof] = fit(RxWheel(:,6),RxWheel(:,3),LogFit);
[YDimFitT, YDimGof] = fit(RxWheel(:,6),RxWheel(:,4),LogFit);
[ZDimFitT, ZDimGof] = fit(RxWheel(:,6),RxWheel(:,5),LogFit);
FittedValuesT = [MassT(RxWheel(:,6)), PowerT(RxWheel(:,6)),...
    XDimFitT(RxWheel(:,6)), YDimFitT(RxWheel(:,6)) ZDimFitT(RxWheel(:,6))];
Residuals = FittedValuesT - RxWheel(:,1:5);
FitResiduals(RxWheel(:,6),RxWheel(:,1),FittedValuesT(:,1),Residuals(:,1),...
    'title','Torque_{max} (Nm)','Mass (kg)')
FitResiduals(RxWheel(:,6),RxWheel(:,2),FittedValuesT(:,2),Residuals(:,2),...
    'title','Torque_{max} (Nm)','Power (W)')
FitResiduals(RxWheel(:,6),RxWheel(:,3),FittedValuesT(:,3),Residuals(:,3),...
    'title','Torque_{max} (Nm)','X Dim (mm)')
FitResiduals(RxWheel(:,6),RxWheel(:,4),FittedValuesT(:,4),Residuals(:,4),...
    'title','Torque_{max} (Nm)','Y Dim (mm)')
FitResiduals(RxWheel(:,6),RxWheel(:,5),FittedValuesT(:,5),Residuals(:,5),...
    'title','Torque_{max} (Nm)','Z Dim (mm)')
```

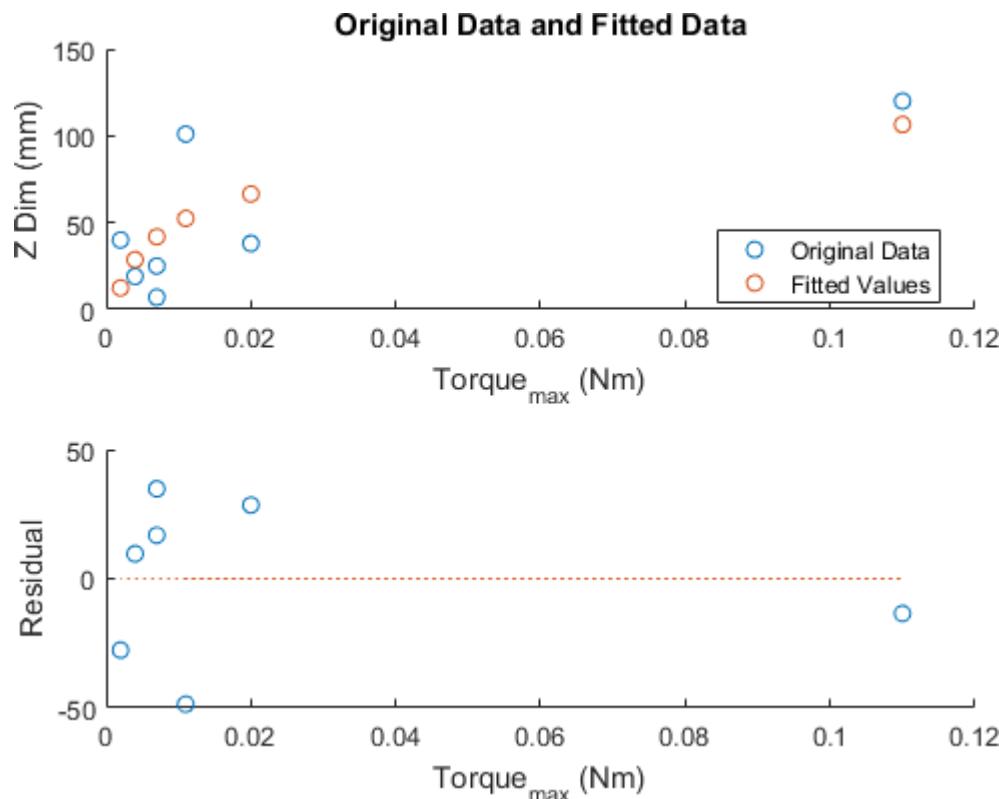
Warning: Start point not provided, choosing random start point.

Warning: Start point not provided, choosing random start point.

Warning: Start point not provided, choosing random start point.

Original Data and Fitted Data**Original Data and Fitted Data**





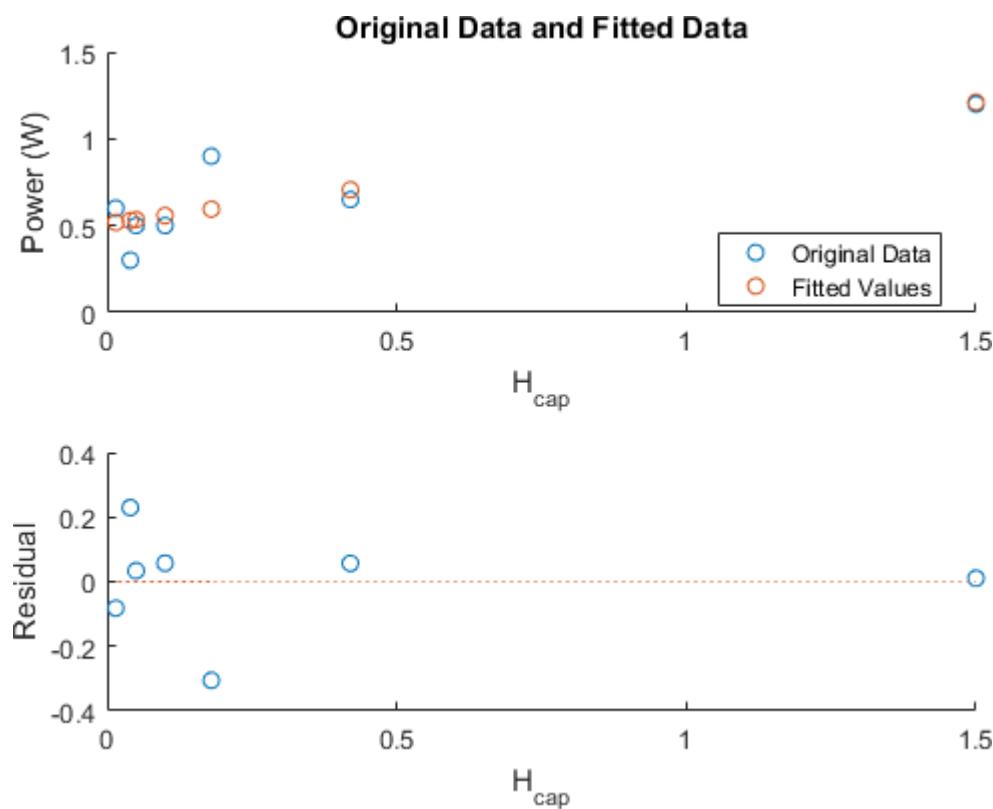
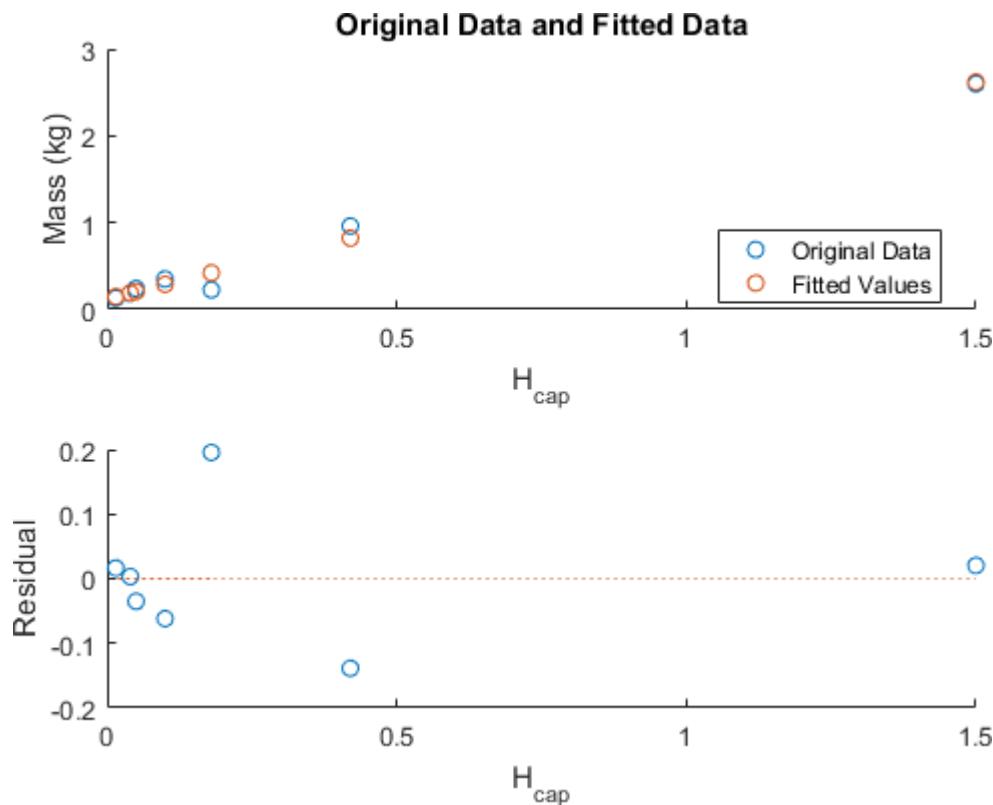
RxWheel Momentum Regression Models

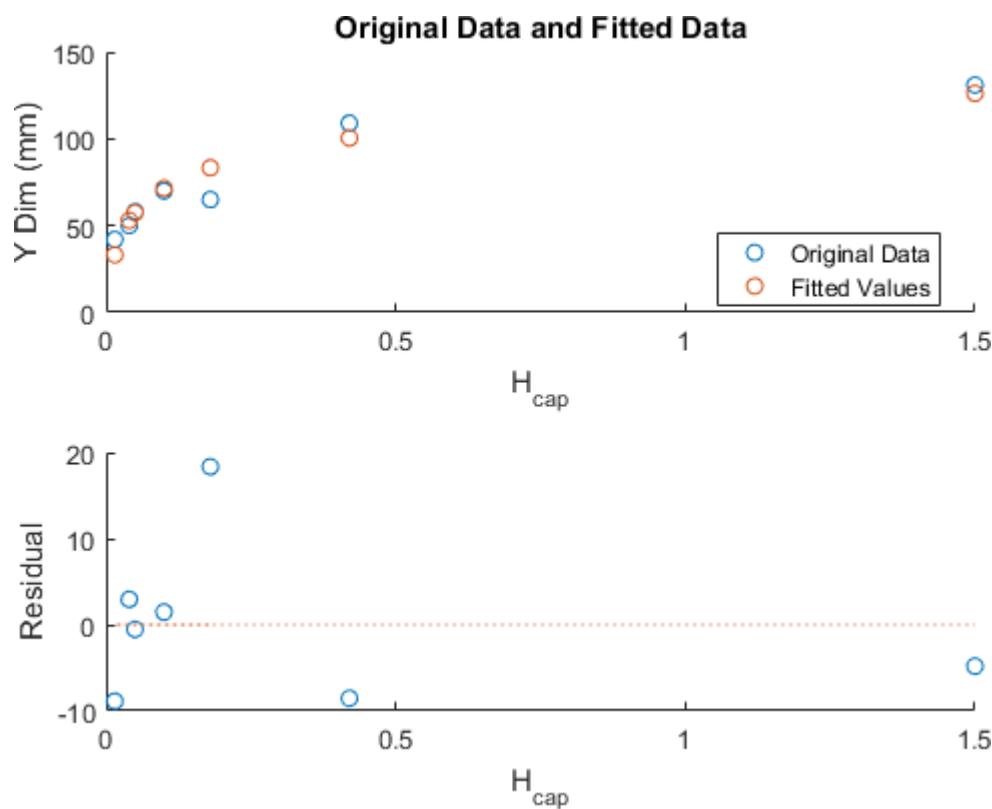
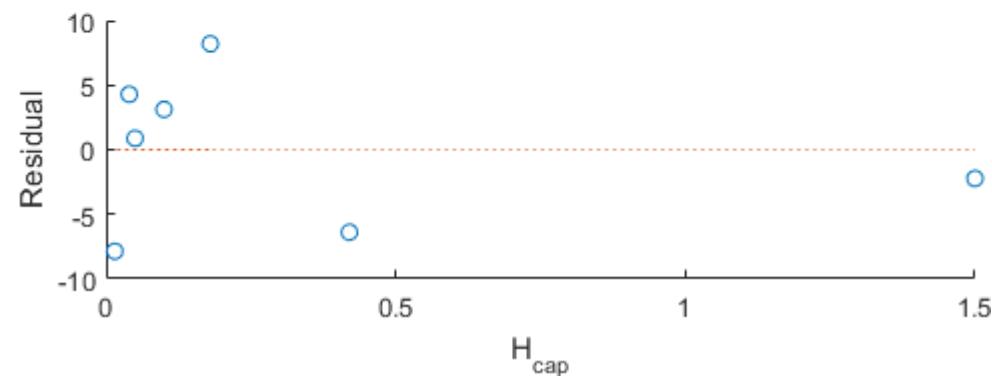
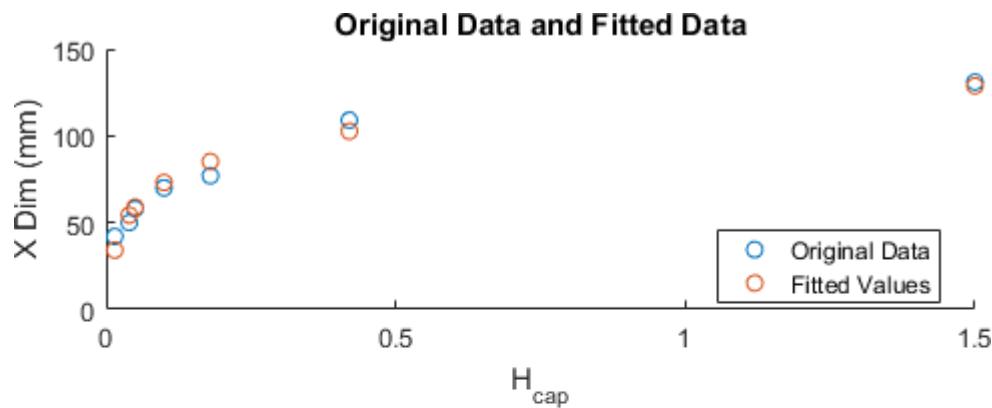
```
[MassH,MassTGOFH] = fit(RxWheel(:,7),RxWheel(:,1),'poly1');
[PowerH, PowerTGOF] = fit(RxWheel(:,7),RxWheel(:,2),'poly1');
[XDimFitH, XDimGOFH] = fit(RxWheel(:,7),RxWheel(:,3),LogFit);
[YDimFitH, YDimGOFH] = fit(RxWheel(:,7),RxWheel(:,4),LogFit);
[ZDimFitH, ZDimGOFH] = fit(RxWheel(:,7),RxWheel(:,5),LogFit);
FittedValuesT = [MassH(RxWheel(:,7)), PowerH(RxWheel(:,7)),...
    XDimFitH(RxWheel(:,7)), YDimFitH(RxWheel(:,7)) ZDimFitH(RxWheel(:,7))];
Residuals = FittedValuesT - RxWheel(:,1:5);
FitResiduals(RxWheel(:,7),RxWheel(:,1),FittedValuesT(:,1),Residuals(:,1),...
    'title','H_{cap}', 'Mass (kg)')
FitResiduals(RxWheel(:,7),RxWheel(:,2),FittedValuesT(:,2),Residuals(:,2),...
    'title','H_{cap}', 'Power (W)')
FitResiduals(RxWheel(:,7),RxWheel(:,3),FittedValuesT(:,3),Residuals(:,3),...
    'title','H_{cap}', 'X Dim (mm)')
FitResiduals(RxWheel(:,7),RxWheel(:,4),FittedValuesT(:,4),Residuals(:,4),...
    'title','H_{cap}', 'Y Dim (mm)')
FitResiduals(RxWheel(:,7),RxWheel(:,5),FittedValuesT(:,5),Residuals(:,5),...
    'title','H_{cap}', 'Z Dim (mm)')
```

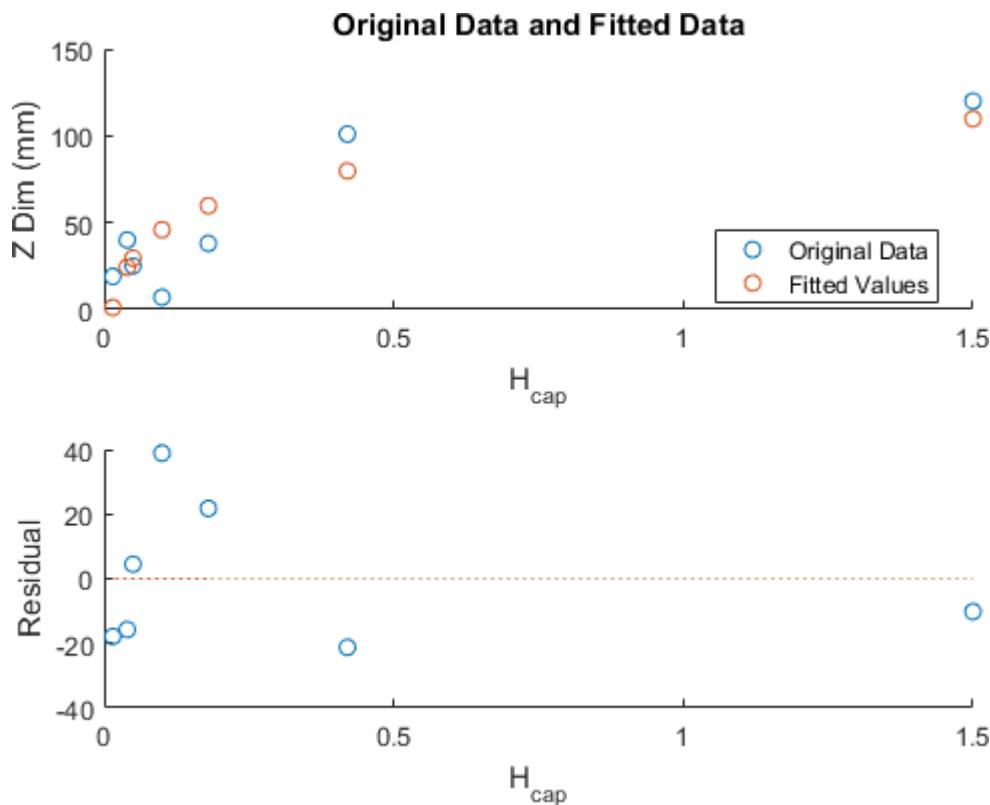
Warning: Start point not provided, choosing random start point.

Warning: Start point not provided, choosing random start point.

Warning: Start point not provided, choosing random start point.







Magnetorquer Data

mass power x y z Dipole (A \cdot m^2)

```

MGTQR = [0.5    0.5    66    252    39    5;
0.2    0.5    15    15    157.5   2;
0.3    0.77   18    18    240    5;
0.3    0.5    14.5   14.5   325    6;
0.35   1      17    17    330    10;
0.3    0.2    10  10  70    0.2;
0.5    0.8  15  13    94    1.2];

```

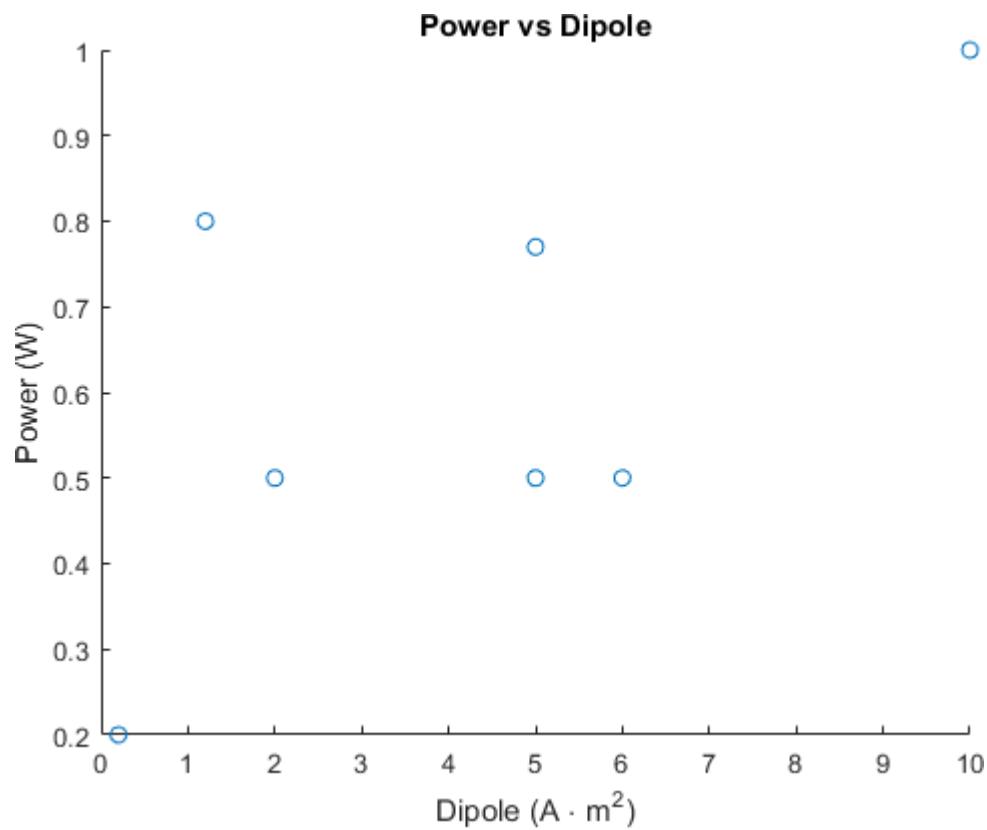
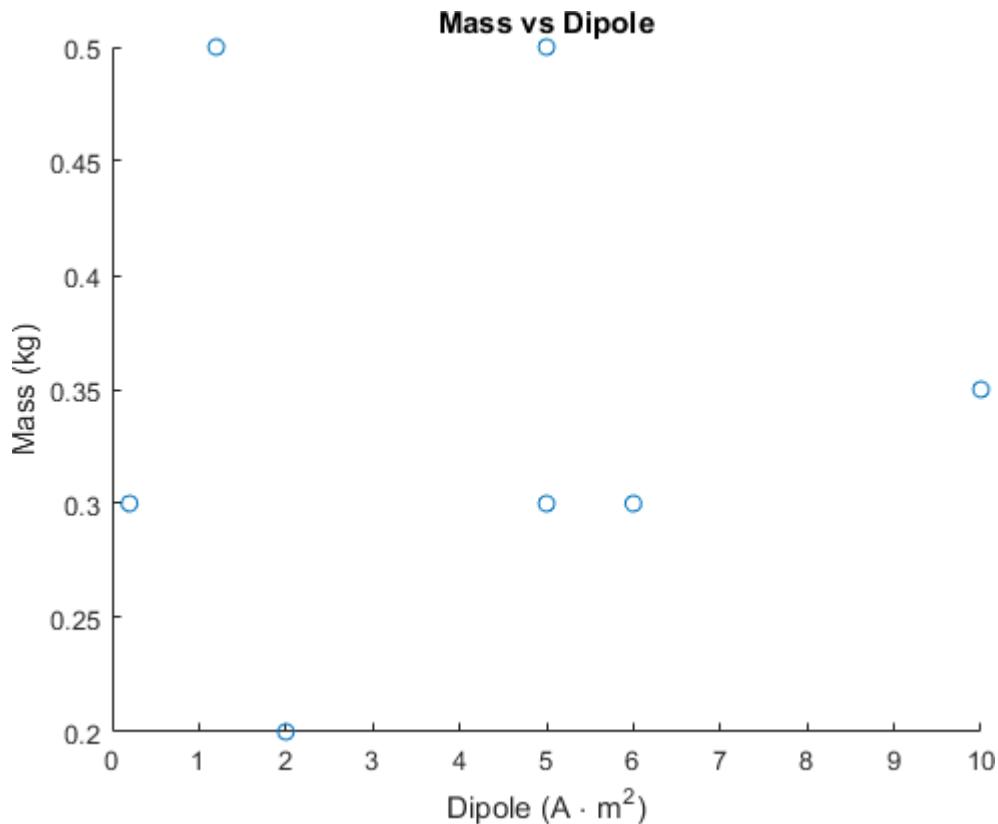
Magnetorquer Graphs (All Linear)

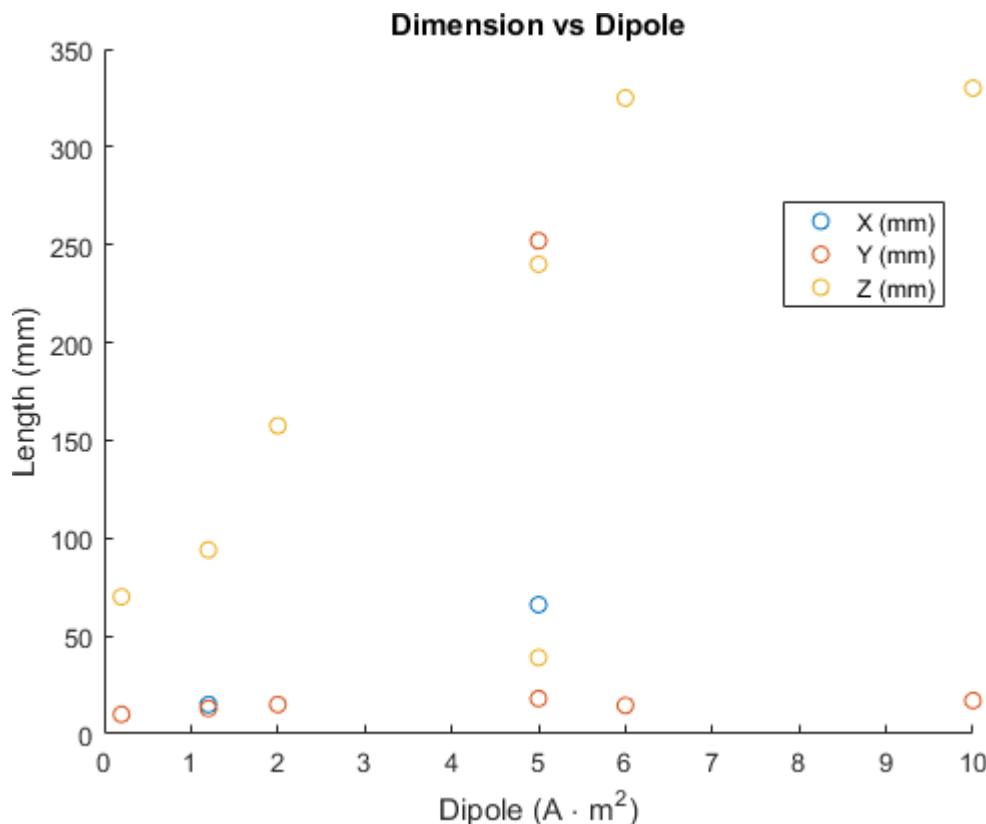
```

%Mass
figure
scatter(MGTQR(:,6),MGTQR(:,1))
title('Mass vs Dipole')
xlabel('Dipole (A \cdot m^2)')
ylabel('Mass (kg)')
%Power
figure
scatter(MGTQR(:,6),MGTQR(:,2))
title('Power vs Dipole')
xlabel('Dipole (A \cdot m^2)')
ylabel('Power (W)')
%Dimesions
figure
hold on
scatter(MGTQR(:,6),MGTQR(:,3))
scatter(MGTQR(:,6),MGTQR(:,4))

```

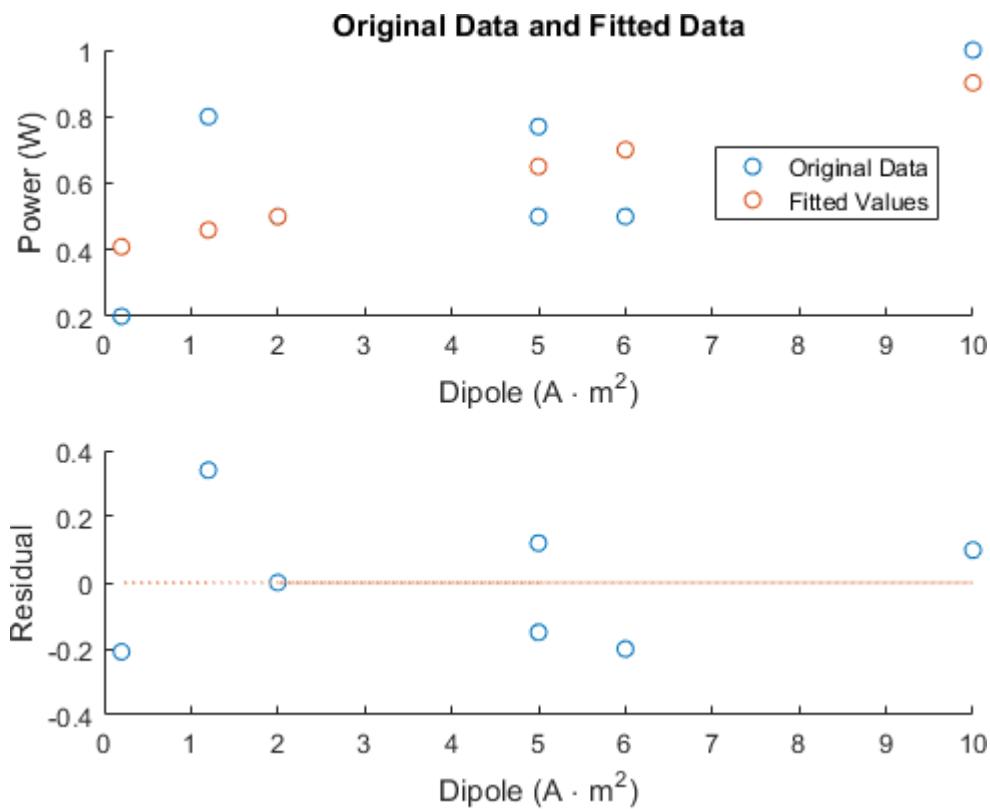
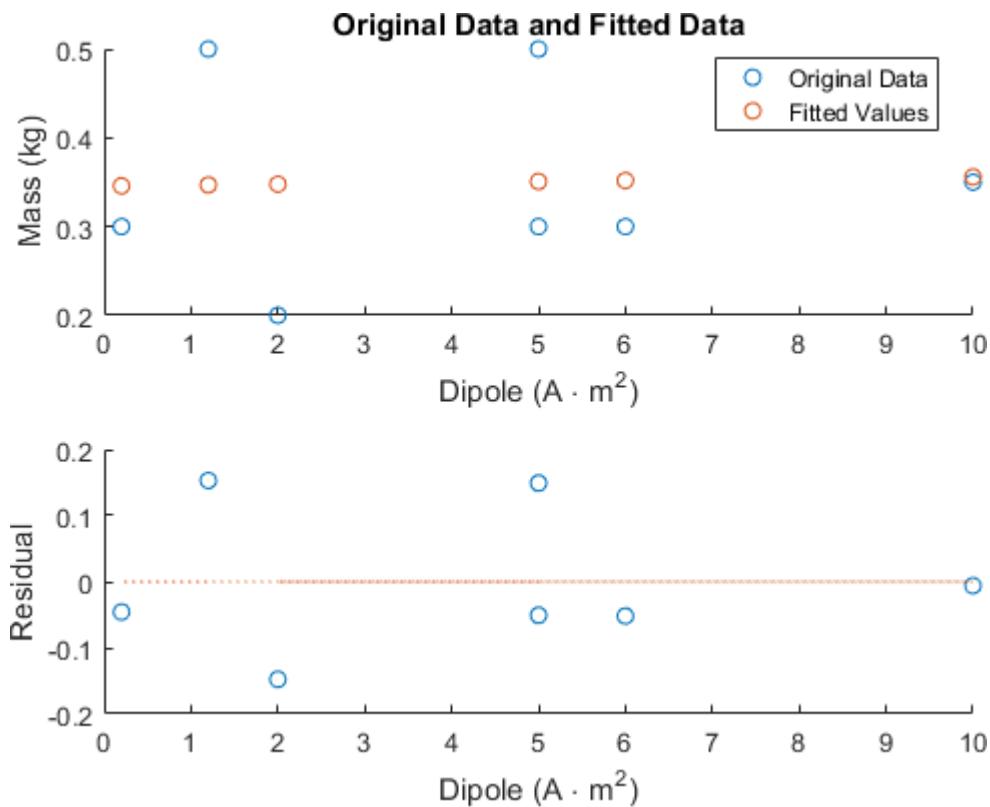
```
scatter(MGTQR(:,6),MGTQR(:,5))
title('Dimension vs Dipole')
xlabel('Dipole (A \cdot m^2)')
ylabel('Length (mm)')
legend('X (mm)', 'Y (mm)', 'Z (mm)', 'location', 'best')
```

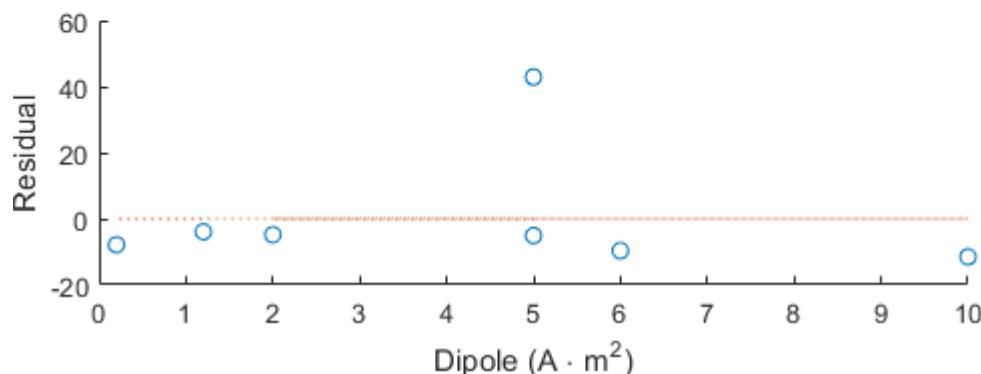
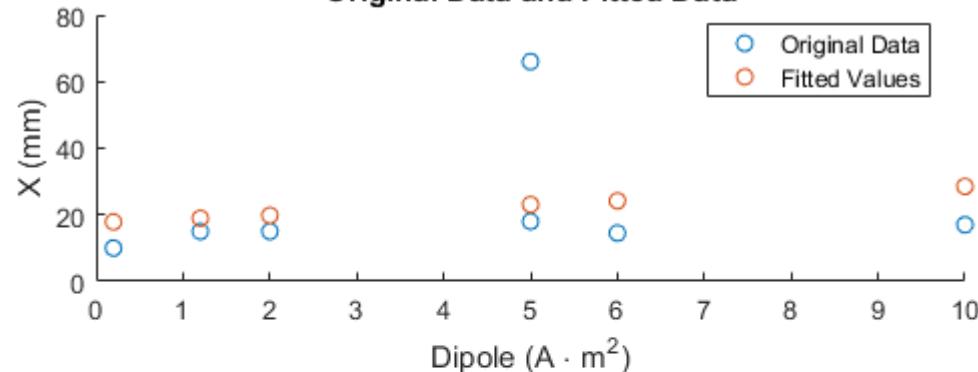
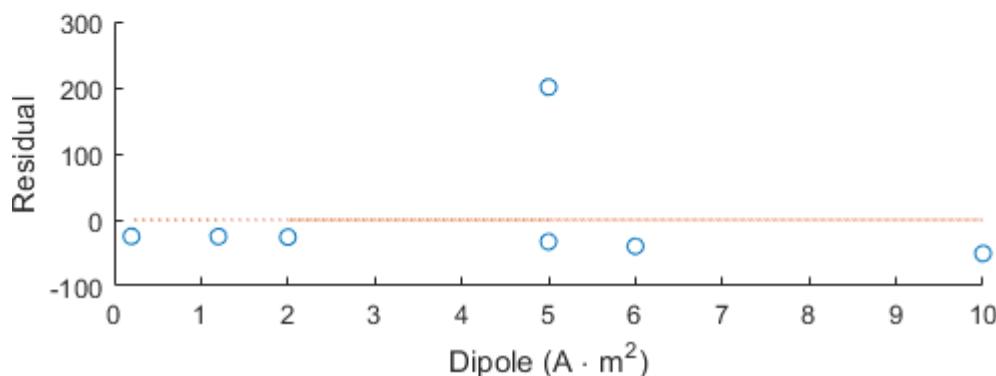
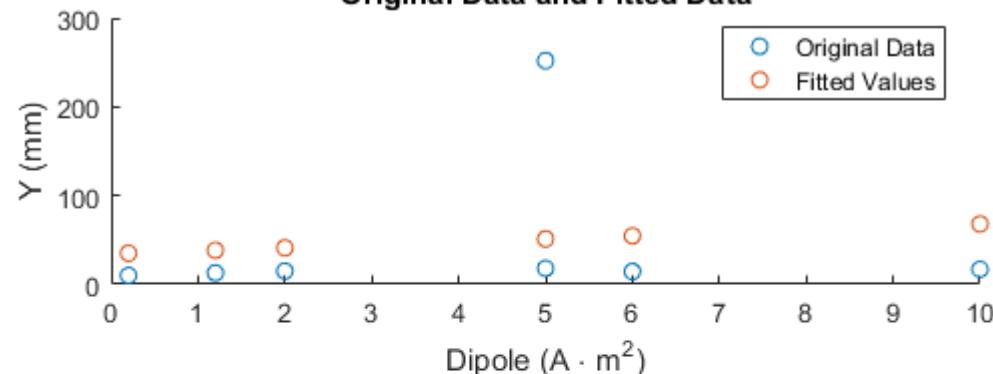


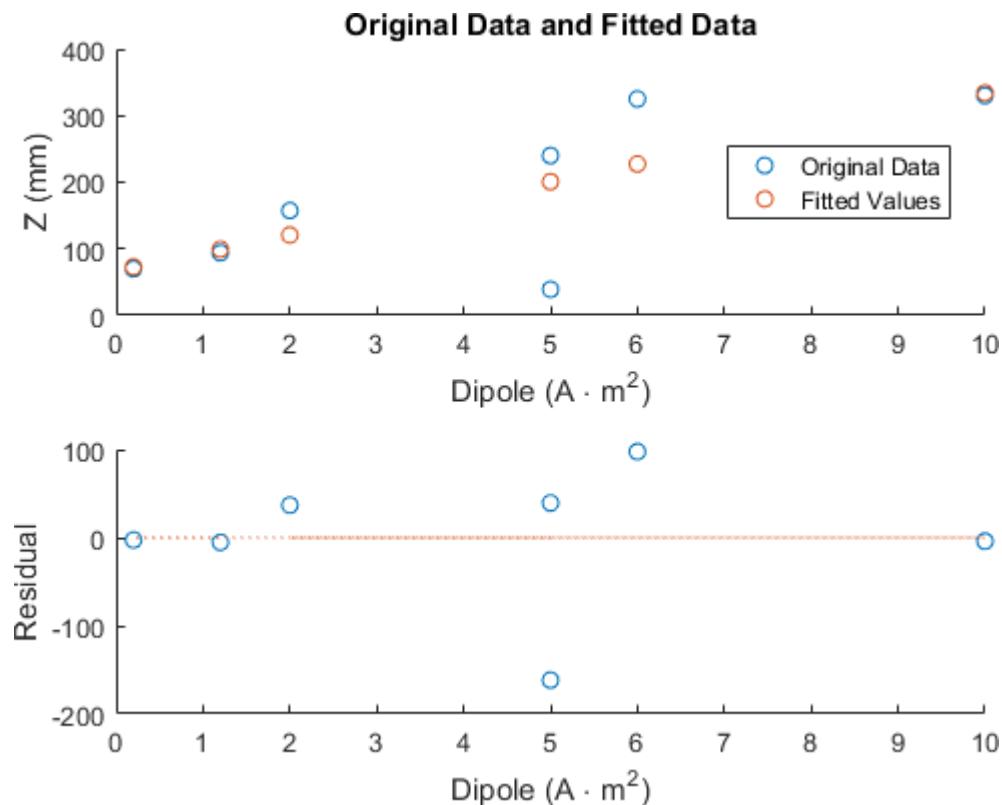


Magnetorquer Regression

```
[MtqDFit, MtqDGOF] = fit(MGTQR(:,6), MGTQR(:,1), 'poly1');
[MtqPFit, MtqPGOF] = fit(MGTQR(:,6), MGTQR(:,2), 'poly1');
[MtqXFit, MtqXGOF] = fit(MGTQR(:,6), MGTQR(:,3), 'poly1');
[MtqYFit, MtqYGOF] = fit(MGTQR(:,6), MGTQR(:,4), 'poly1');
[MtqZFit, MtqZGOF] = fit(MGTQR(:,6), MGTQR(:,5), 'poly1');
MDFitted = [MtqDFit(MGTQR(:,6)), MtqPFit(MGTQR(:,6)), MtqXFit(MGTQR(:,6)), ...
    MtqYFit(MGTQR(:,6)), MtqZFit(MGTQR(:,6))];
MDResiduals = MGTQR(:,1:5)-MDFitted;
FitResiduals(MGTQR(:,6), MGTQR(:,1), MDFitted(:,1), MDResiduals(:,1), ...
    'title', 'Dipole (A \cdot m^2)', 'Mass (kg)')
FitResiduals(MGTQR(:,6), MGTQR(:,2), MDFitted(:,2), MDResiduals(:,2), ...
    'title', 'Dipole (A \cdot m^2)', 'Power (W)')
FitResiduals(MGTQR(:,6), MGTQR(:,3), MDFitted(:,3), MDResiduals(:,3), ...
    'title', 'Dipole (A \cdot m^2)', 'X (mm)')
FitResiduals(MGTQR(:,6), MGTQR(:,4), MDFitted(:,4), MDResiduals(:,4), ...
    'title', 'Dipole (A \cdot m^2)', 'Y (mm)')
FitResiduals(MGTQR(:,6), MGTQR(:,5), MDFitted(:,5), MDResiduals(:,5), ...
    'title', 'Dipole (A \cdot m^2)', 'Z (mm)')
```



Original Data and Fitted Data**Original Data and Fitted Data**

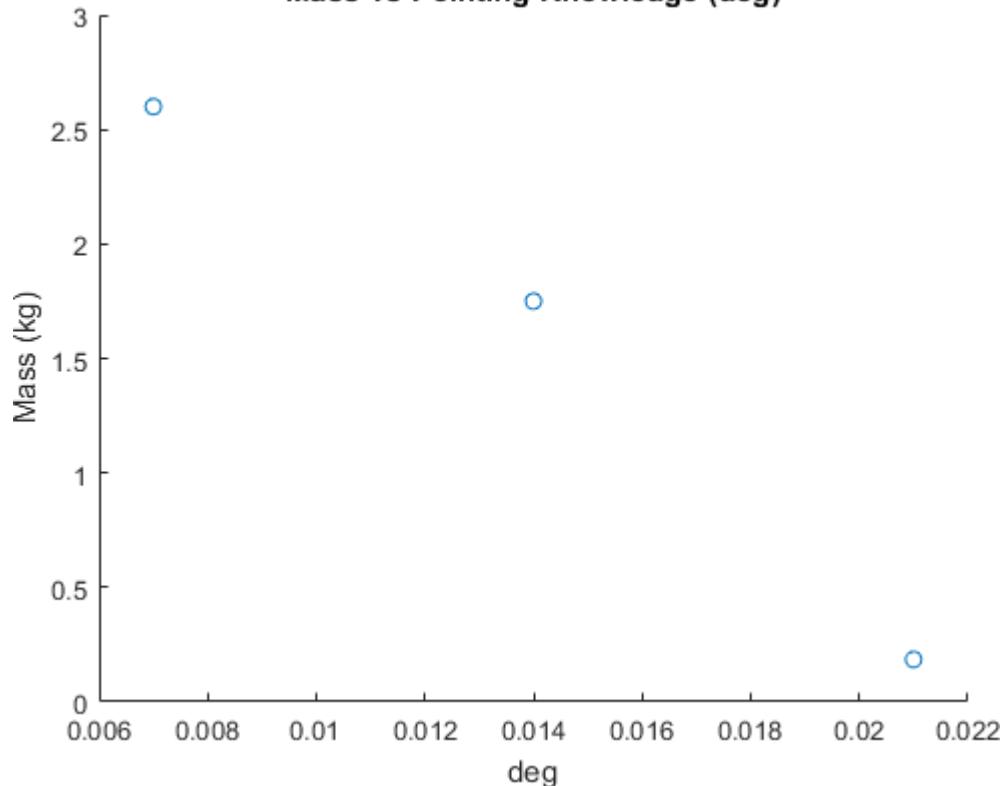
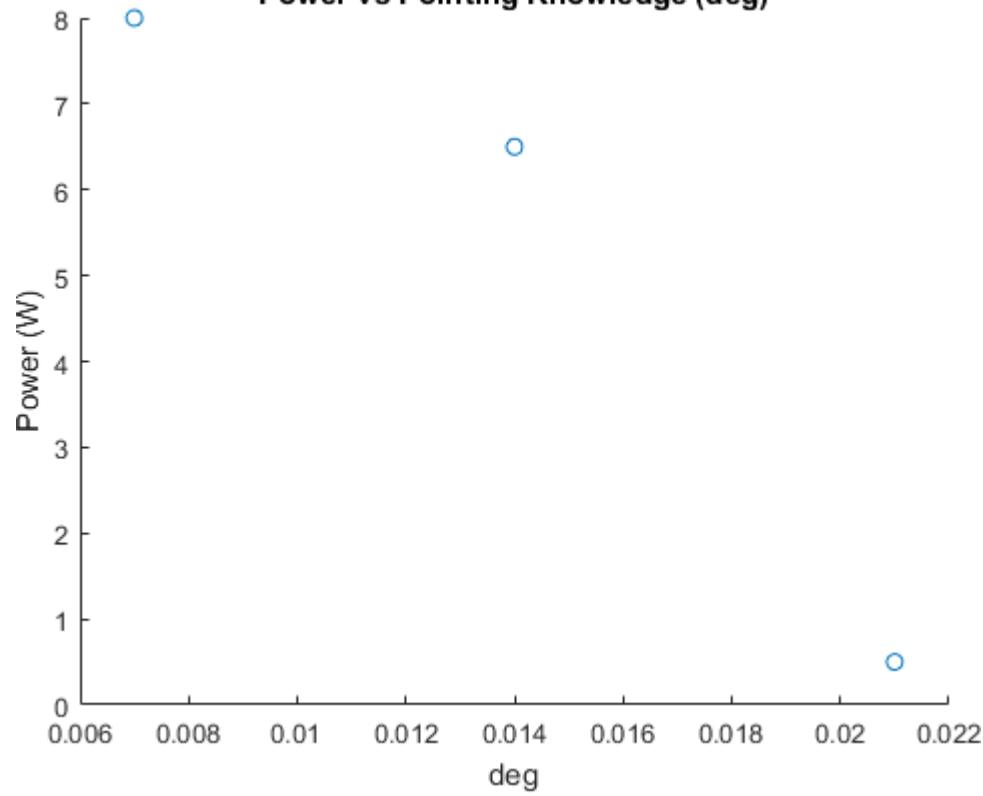


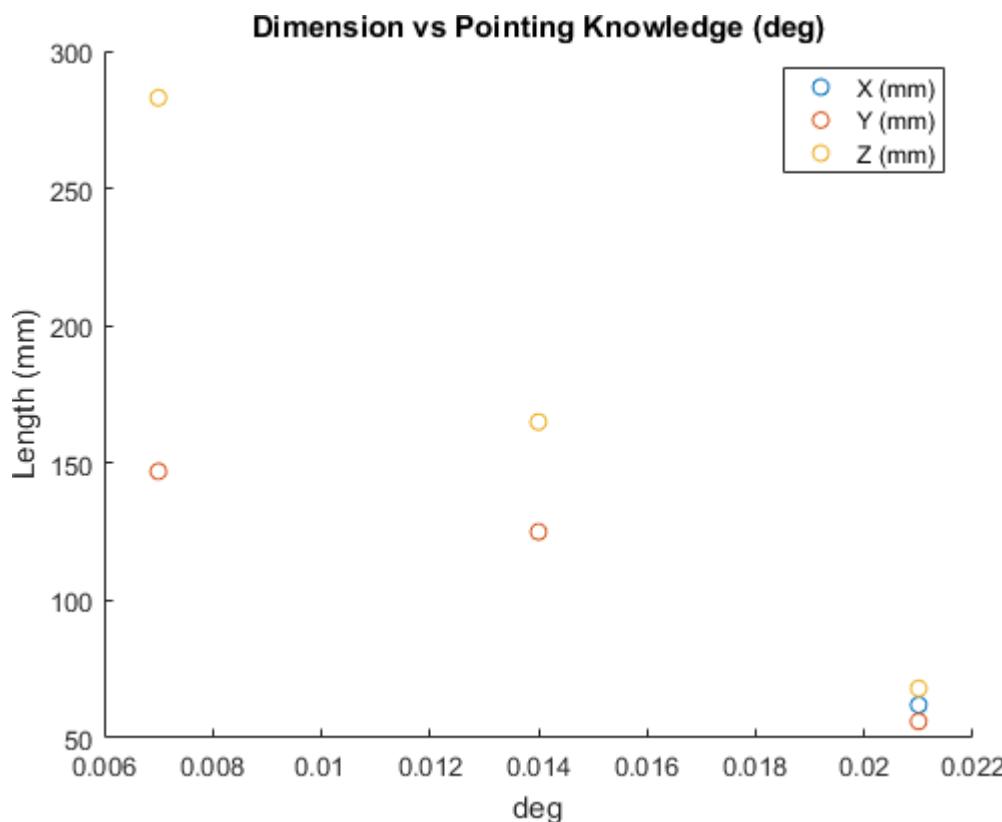
Star Tracker Data

```

STDATA = [2.6    8       147     147     283     0.007;
1.75   6.5    125     125     165     0.014;
0.185  0.5    62      56      68      0.021];
%Mass
figure
scatter(STDATA(:,6),STDATA(:,1))
title('Mass vs Pointing Knowledge (deg)')
xlabel('deg')
ylabel('Mass (kg)')
%Power
figure
scatter(STDATA(:,6),STDATA(:,2))
title('Power vs Pointing Knowledge (deg)')
xlabel('deg')
ylabel('Power (W)')
%Dimensions
figure
hold on
scatter(STDATA(:,6),STDATA(:,3))
scatter(STDATA(:,6),STDATA(:,4))
scatter(STDATA(:,6),STDATA(:,5))
title('Dimension vs Pointing Knowledge (deg)')
xlabel('deg')
ylabel('Length (mm)')
legend('X (mm)', 'Y (mm)', 'Z (mm)', 'location', 'best')

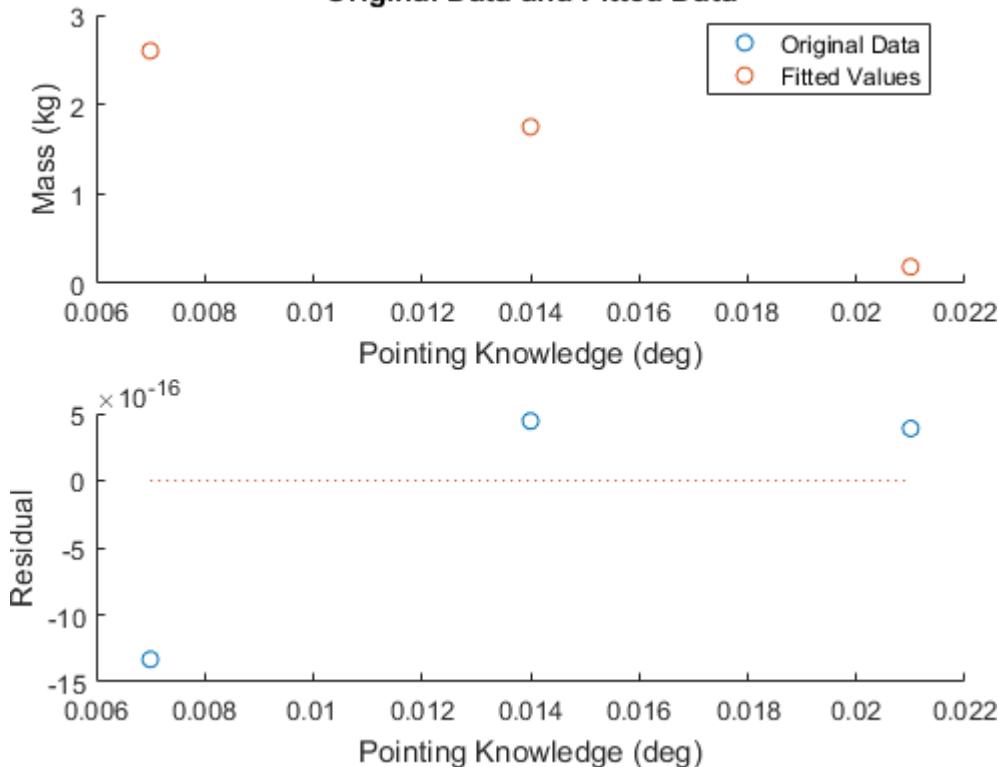
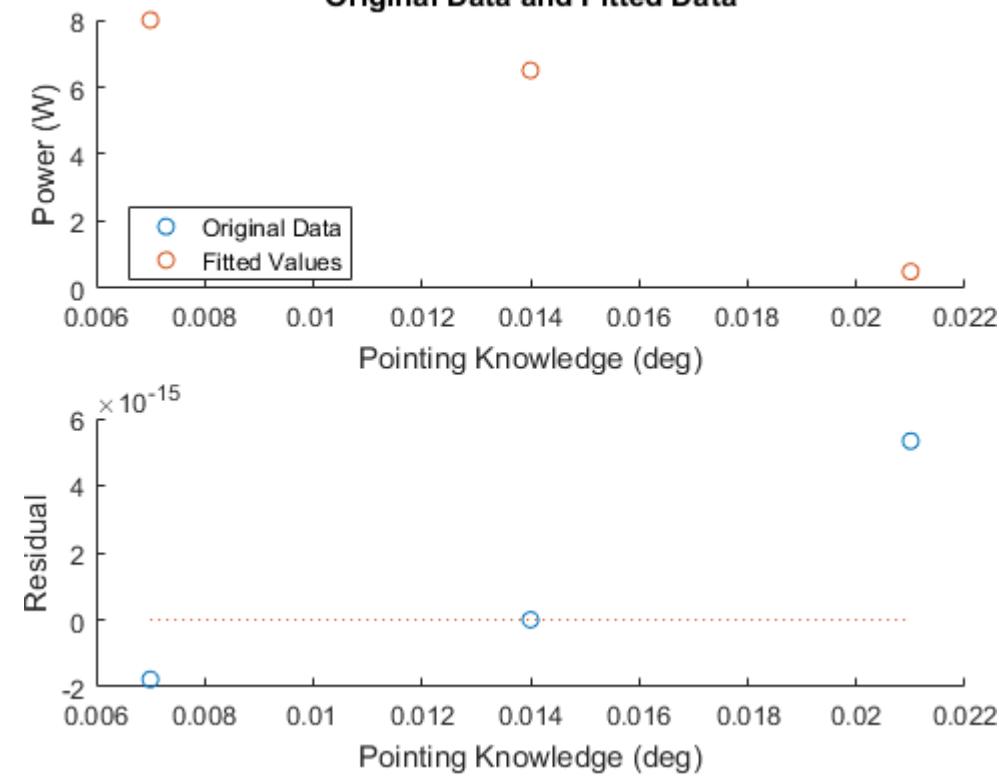
```

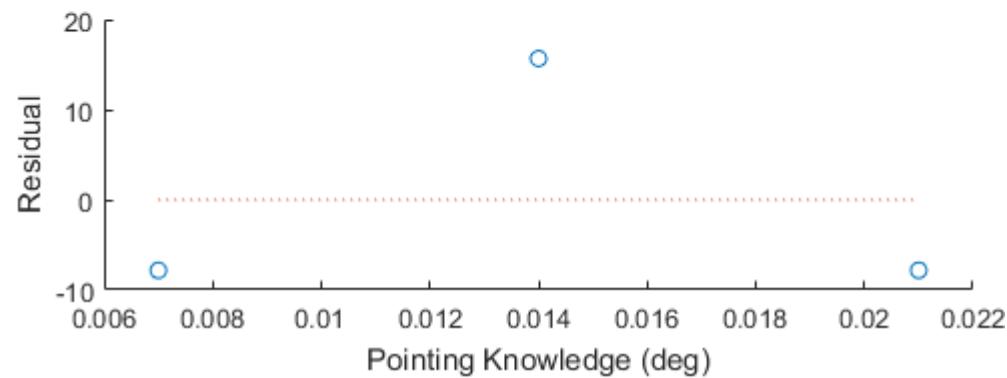
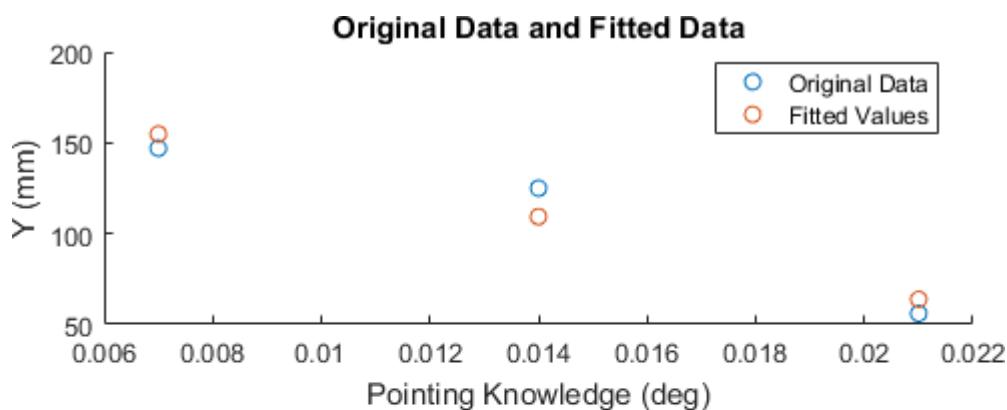
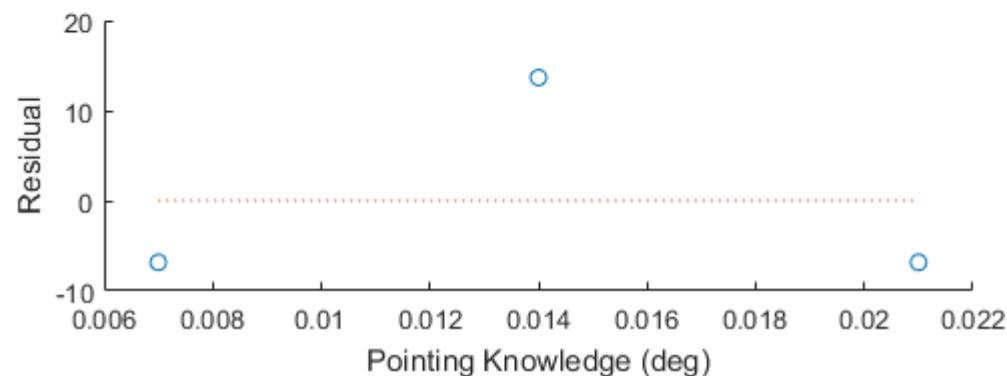
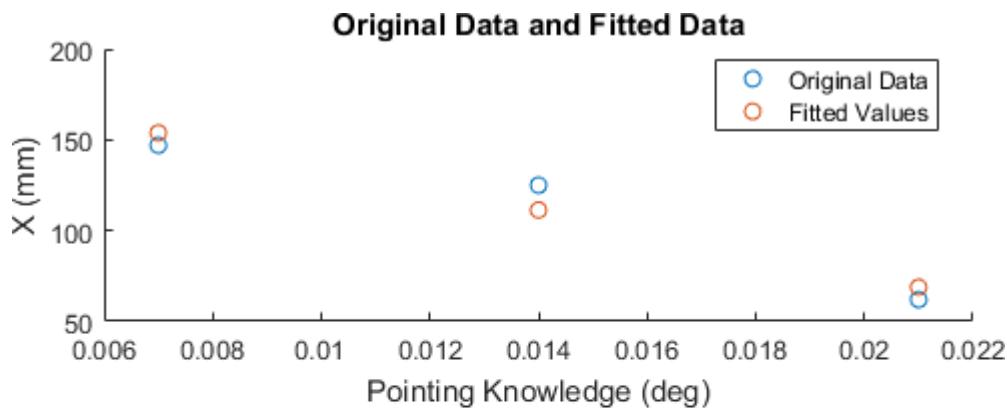
Mass vs Pointing Knowledge (deg)**Power vs Pointing Knowledge (deg)**

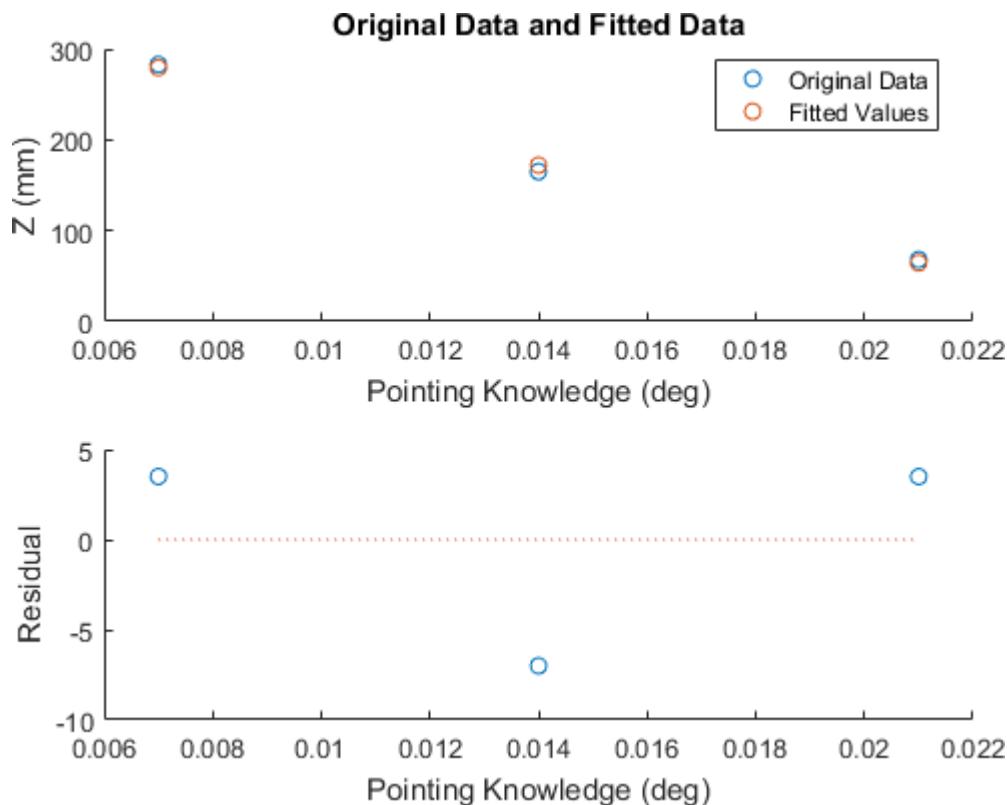


Star Tracker Regression

```
[STDFit, STDGOF] = fit(STDATA(:,6),STDATA(:,1),'poly2');
[STPFit, STPGOF] = fit(STDATA(:,6),STDATA(:,2),'poly2');
[STXFit, STXGOF] = fit(STDATA(:,6),STDATA(:,3),'poly1');
[STYFit, STYGOF] = fit(STDATA(:,6),STDATA(:,4),'poly1');
[STZFit, STZGOF] = fit(STDATA(:,6),STDATA(:,5),'poly1');
STFitted = [STDFit(STDATA(:,6)), STPFit(STDATA(:,6)), STXFit(STDATA(:,6)), ...
            STYFit(STDATA(:,6)),STZFit(STDATA(:,6))];
STResiduals = STDATA(:,1:5)-STFitted;
FitResiduals(STDATA(:,6),STDATA(:,1),STFitted(:,1),STResiduals(:,1),...
             'title','Pointing Knowledge (deg)', 'Mass (kg)')
FitResiduals(STDATA(:,6),STDATA(:,2),STFitted(:,2),STResiduals(:,2),...
             'title','Pointing Knowledge (deg)', 'Power (W)')
FitResiduals(STDATA(:,6),STDATA(:,3),STFitted(:,3),STResiduals(:,3),...
             'title','Pointing Knowledge (deg)', 'X (mm)')
FitResiduals(STDATA(:,6),STDATA(:,4),STFitted(:,4),STResiduals(:,4),...
             'title','Pointing Knowledge (deg)', 'Y (mm)')
FitResiduals(STDATA(:,6),STDATA(:,5),STFitted(:,5),STResiduals(:,5),...
             'title','Pointing Knowledge (deg)', 'Z (mm)')
```

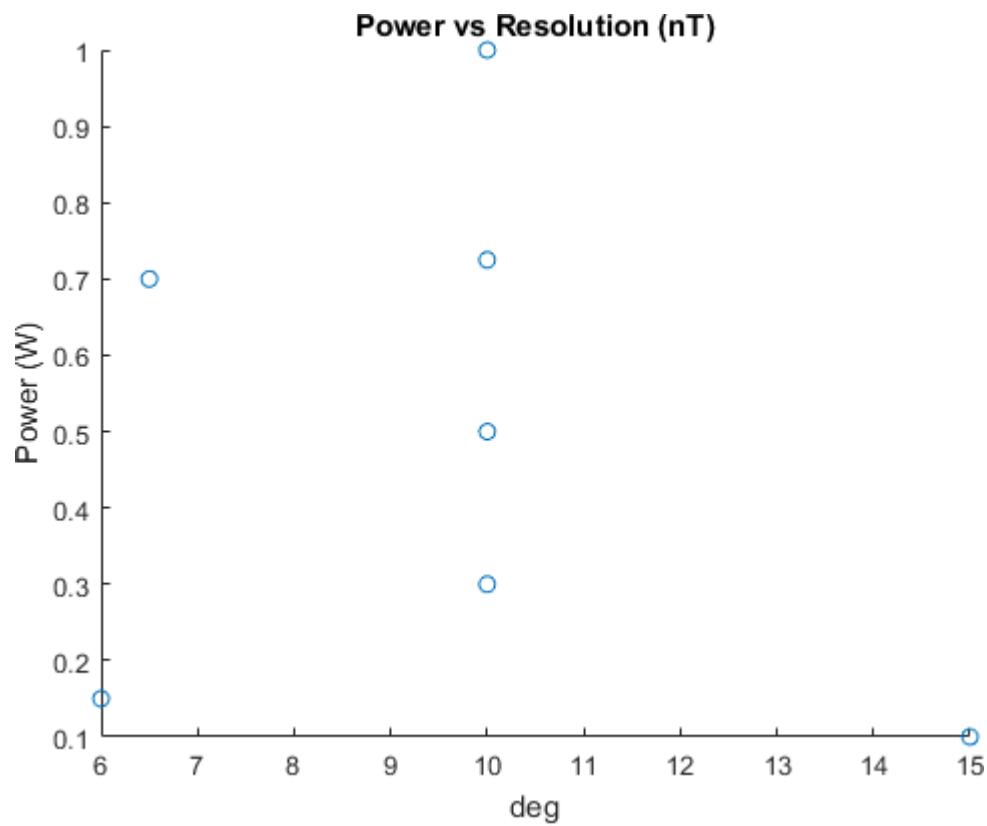
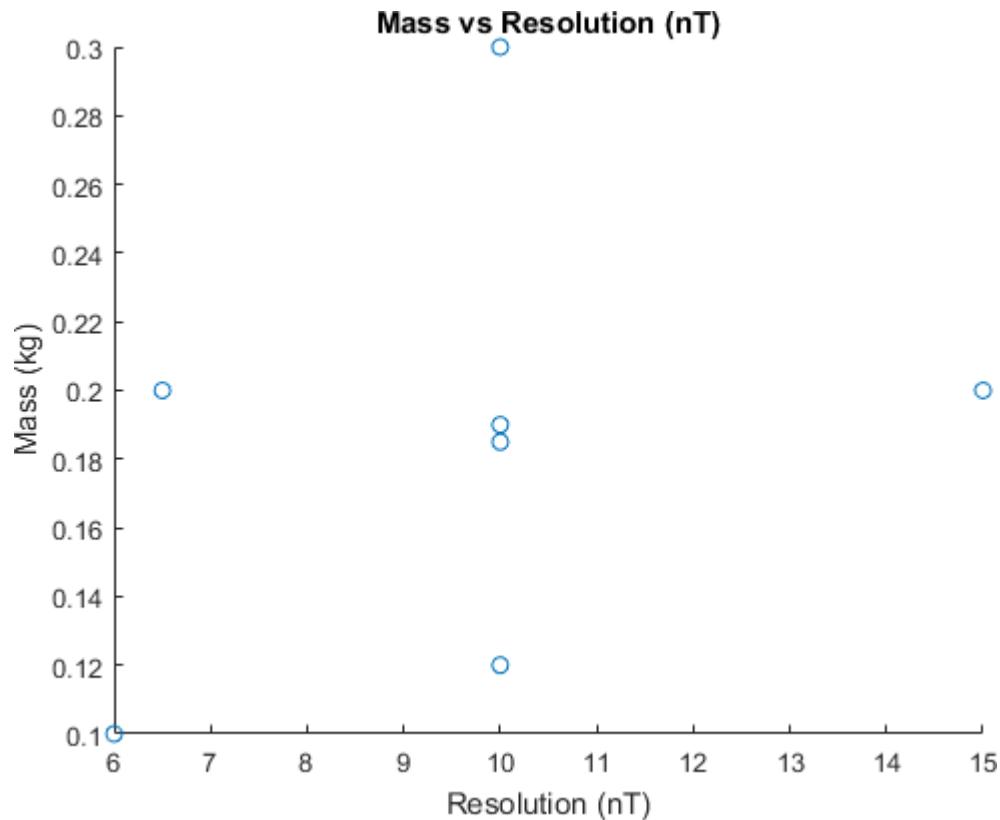
Original Data and Fitted Data**Original Data and Fitted Data**

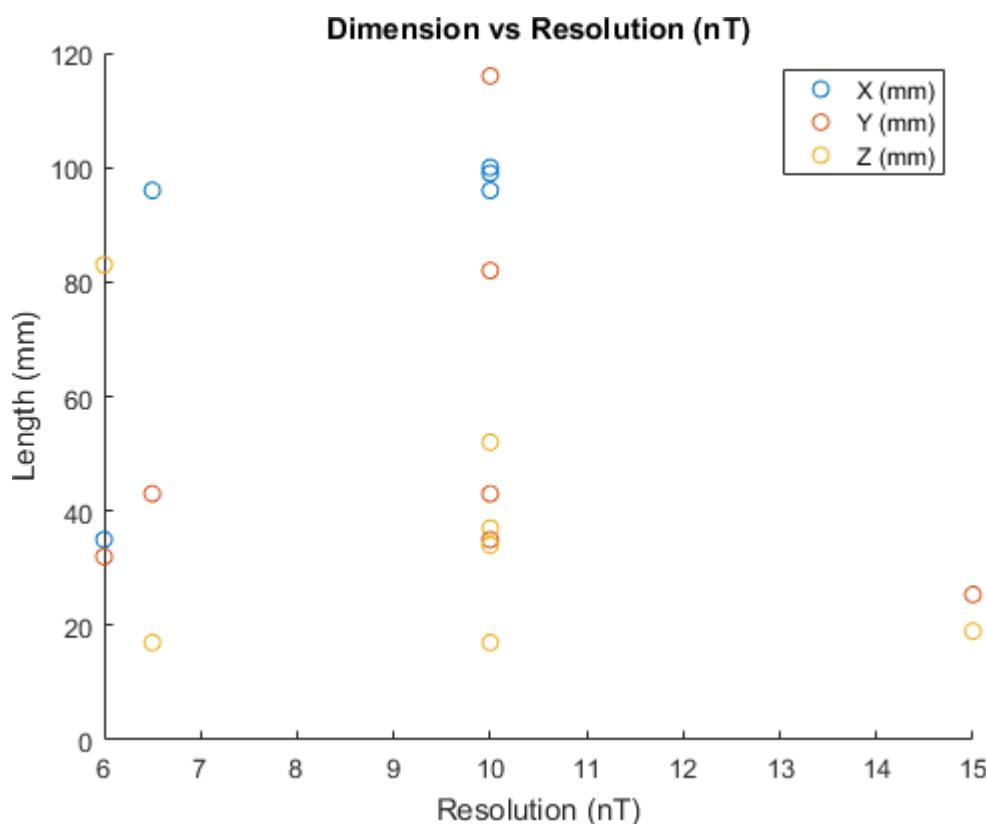




Magnetometer Data

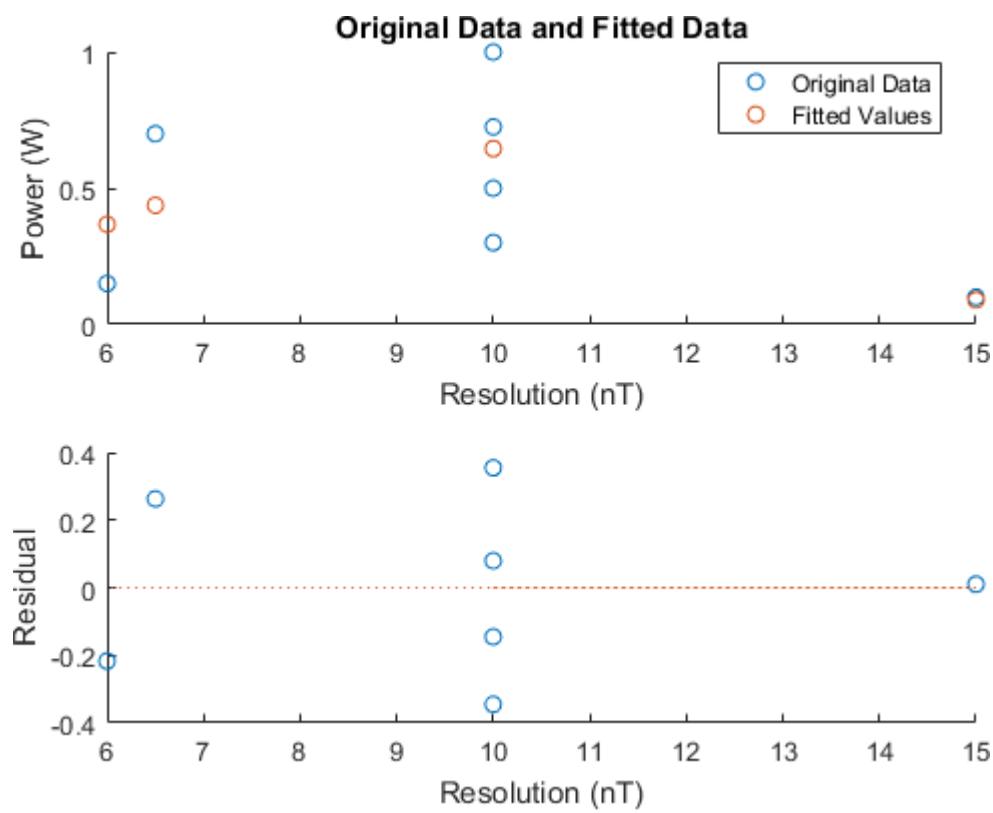
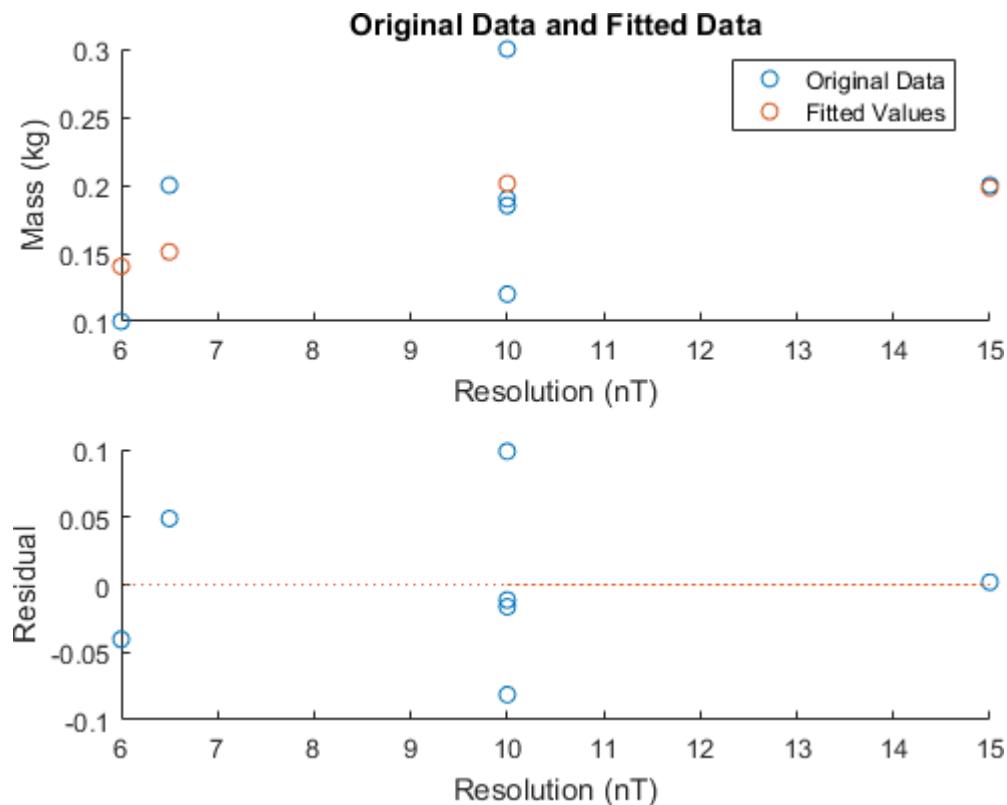
```
%mass power x y z resolution (nT)
MgtmData = [0.12      0.5    116    116    37    10;
0.185    0.725   96     43     17     10;
0.2      0.1     25.4   25.4    19     15;
0.19    0.3      99     35     52     10;
0.3      1       100    82     34     10;
0.2      0.7     96     43     17     6.5;
0.1      0.15    35     32     83     6];
%Mass
figure
scatter(MgtmData(:,6),MgtmData(:,1))
title('Mass vs Resolution (nT)')
xlabel('Resolution (nT)')
ylabel('Mass (kg)')
%Power
figure
scatter(MgtmData(:,6),MgtmData(:,2))
title('Power vs Resolution (nT)')
xlabel('deg')
ylabel('Power (W)')
%Dimentions
figure
hold on
scatter(MgtmData(:,6),MgtmData(:,3))
scatter(MgtmData(:,6),MgtmData(:,4))
scatter(MgtmData(:,6),MgtmData(:,5))
title('Dimension vs Resolution (nT)')
xlabel('Resolution (nT)')
ylabel('Length (mm)')
legend('X (mm)', 'Y (mm)', 'Z (mm)', 'location', 'best')
```

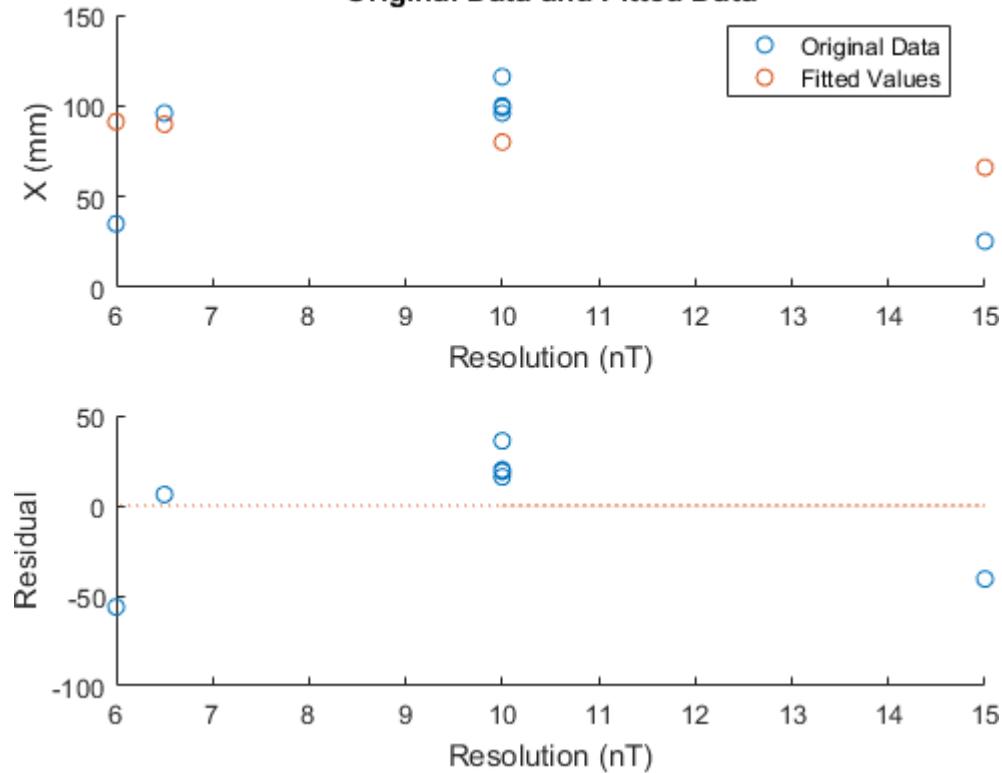
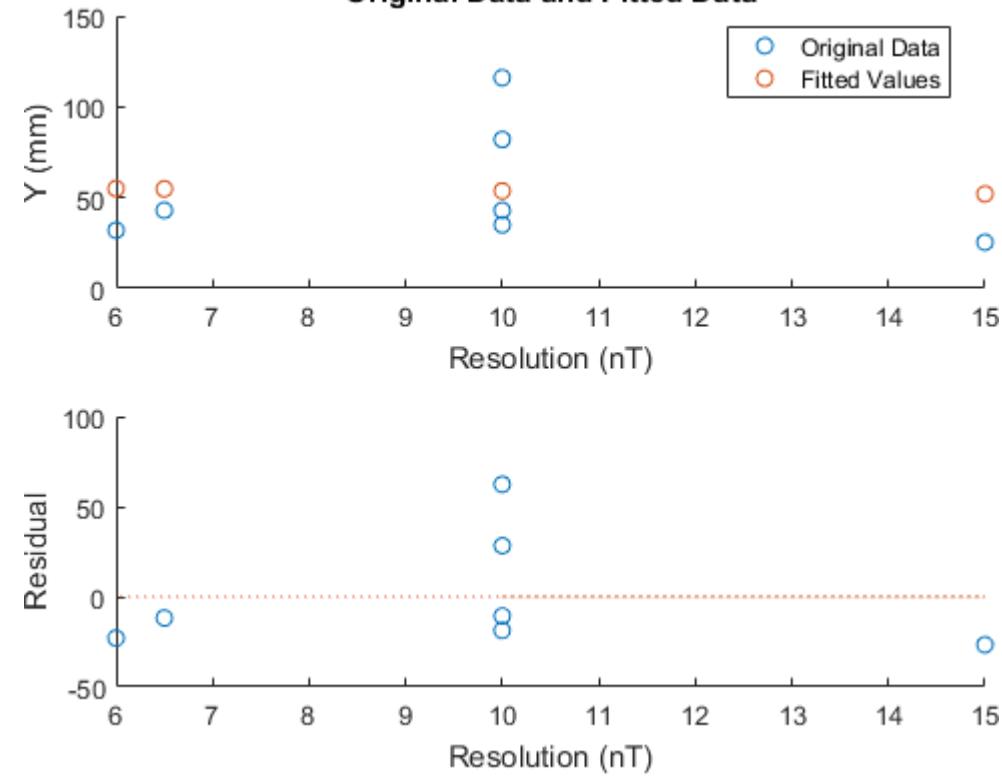


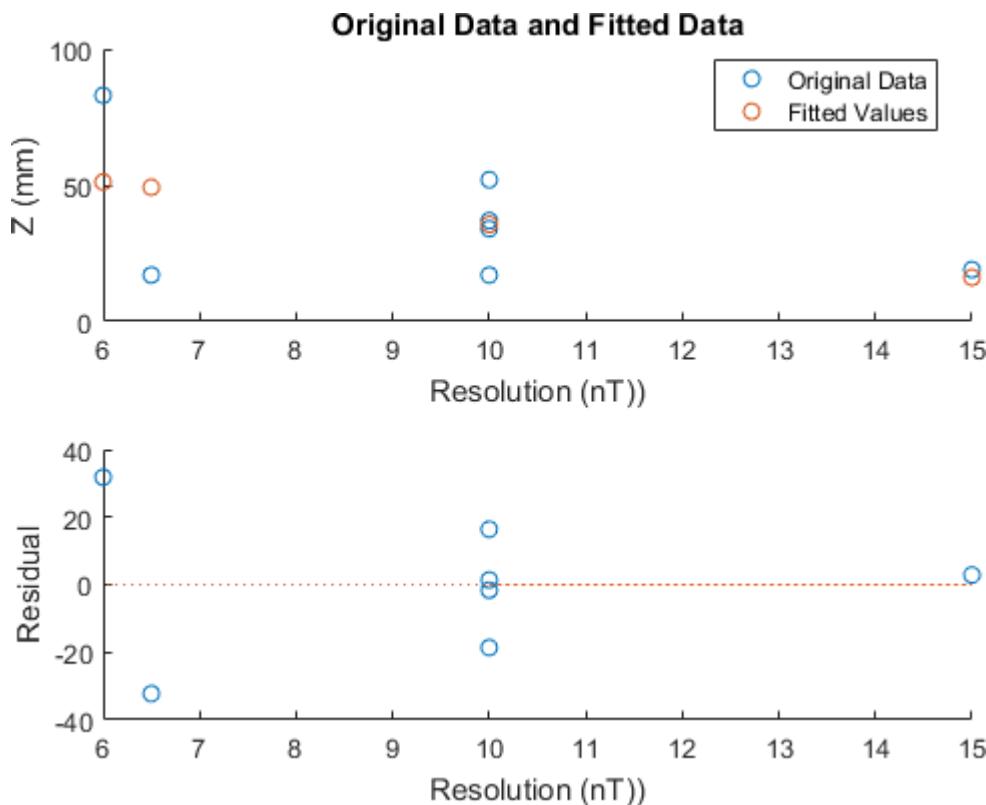


Magnetometer Regression

```
[MMDFit, MMDGOF] = fit(MgtmData(:,6),MgtmData(:,1), 'poly2');
[MMPFit, MMPGOF] = fit(MgtmData(:,6),MgtmData(:,2), 'poly2');
[MMXFit, MMXGOF] = fit(MgtmData(:,6),MgtmData(:,3), 'poly1');
[MMYFit, MMYGOF] = fit(MgtmData(:,6),MgtmData(:,4), 'poly1');
[MMZFit, MMZGOF] = fit(MgtmData(:,6),MgtmData(:,5), 'poly1');
MMFitted = [MMDFit(MgtmData(:,6)), MMPFit(MgtmData(:,6)), MMXFit(MgtmData(:,6)), ...
    MMYFit(MgtmData(:,6)), MMZFit(MgtmData(:,6))];
MMResiduals = MgtmData(:,1:5)-MMFitted;
FitResiduals(MgtmData(:,6),MgtmData(:,1),MMFitted(:,1),MMResiduals(:,1),...
    'title', 'Resolution (nT)', 'Mass (kg)')
FitResiduals(MgtmData(:,6),MgtmData(:,2),MMFitted(:,2),MMResiduals(:,2),...
    'title', 'Resolution (nT)', 'Power (W)')
FitResiduals(MgtmData(:,6),MgtmData(:,3),MMFitted(:,3),MMResiduals(:,3),...
    'title', 'Resolution (nT)', 'X (mm)')
FitResiduals(MgtmData(:,6),MgtmData(:,4),MMFitted(:,4),MMResiduals(:,4),...
    'title', 'Resolution (nT)', 'Y (mm)')
FitResiduals(MgtmData(:,6),MgtmData(:,5),MMFitted(:,5),MMResiduals(:,5),...
    'title', 'Resolution (nT)', 'Z (mm)')
```



Original Data and Fitted Data**Original Data and Fitted Data**

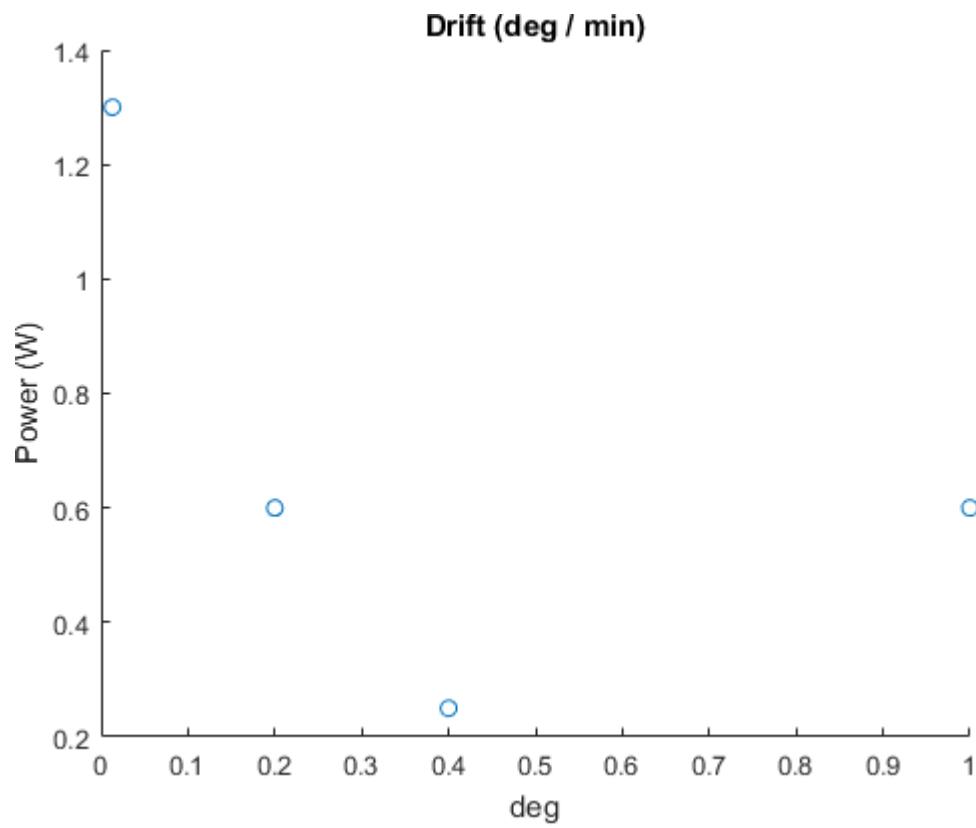
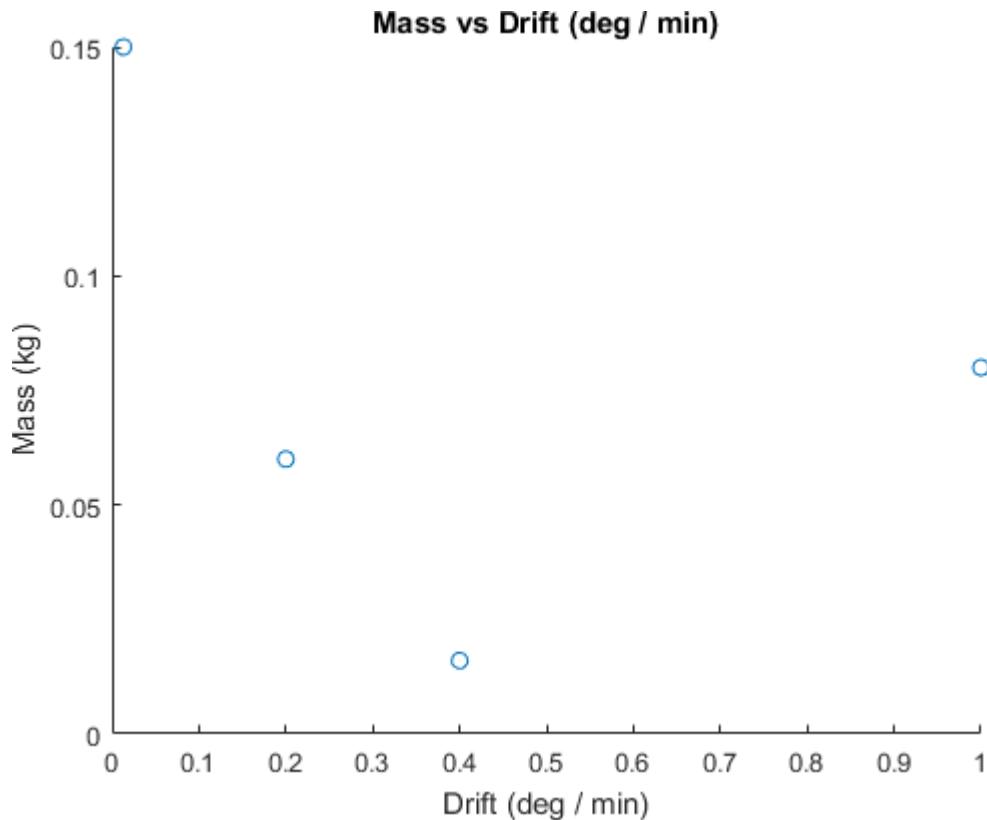


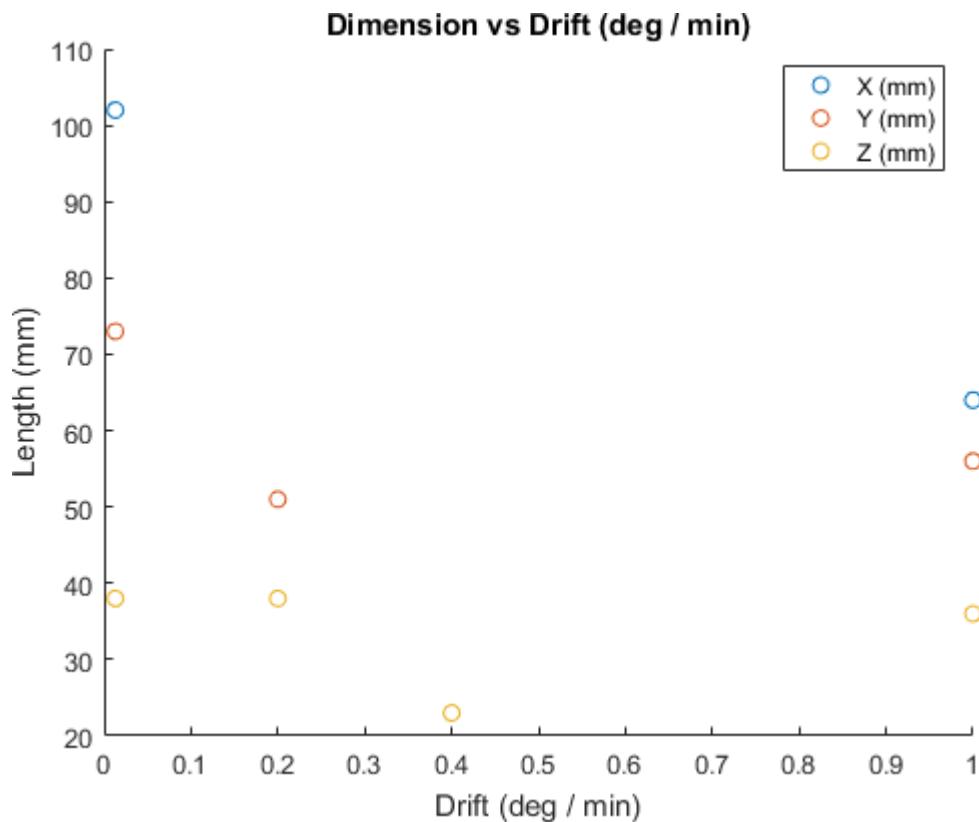
IMU Data

```

IMUDATA = [0.08 0.6      64      56      36      1;
0.06    0.6      51      51      38      0.2;
0.15    1.3     102      73      38      0.013;
0.016   0.25     23      23      23      0.4];
%Mass
figure
scatter(IMUDATA(:,6),IMUDATA(:,1))
title('Mass vs Drift (deg / min)')
xlabel('Drift (deg / min)')
ylabel('Mass (kg)')
%Power
figure
scatter(IMUDATA(:,6),IMUDATA(:,2))
title('Drift (deg / min)')
xlabel('deg')
ylabel('Power (W)')
%Dimensions
figure
hold on
scatter(IMUDATA(:,6),IMUDATA(:,3))
scatter(IMUDATA(:,6),IMUDATA(:,4))
scatter(IMUDATA(:,6),IMUDATA(:,5))
title('Dimension vs Drift (deg / min)')
xlabel('Drift (deg / min)')
ylabel('Length (mm)')
legend('X (mm)', 'Y (mm)', 'Z (mm)', 'location', 'best')

```





IMU Regression

```
[IMUDFit, IMUDGOF] = fit(IMUDATA(:,6),IMUDATA(:,1),'poly1');
[IMUPFit, IMUPGOF] = fit(IMUDATA(:,6),IMUDATA(:,2),'poly1');
[IMUXFit, IMUXGOF] = fit(IMUDATA(:,6),IMUDATA(:,3),'poly1');
[IMUYFit, IMUYGOF] = fit(IMUDATA(:,6),IMUDATA(:,4),'poly1');
[IMUZFit, IMUZGOF] = fit(IMUDATA(:,6),IMUDATA(:,5),'poly1');
```

Regression Functions and Goodness of Fit

```
disp('Reaction Wheel Functions')
disp('Maximum Torque Regression')
MassT,MassTGOF
PowerT, PowerTGOF
XDimFitT, XDimGof
YDimFitT, YDimGof
ZDimFitT, ZDimGof
MassH,MassTGOFH
disp('Maximum Momentum Capacity')
PowerH, PowerTGOF
XDimFitH, XDimGOFH
YDimFitH, YDimGOFH
ZDimFitH, ZDimGOFH
disp('Maxnetorquer Regression')
MtqDFit, MtqDGOF
MtqPFFit, MtqPGOF
MtqXFit, MtqXGOF
MtqYFit, MtqYGOF
MtqZFit, MtqZGOF
disp('Star Tracker Regression')
STDFit, STDGOF
```

```

STPFit, STPGOF
STXFit, STXGOF
STYFit, STYGOF
STZFit, STZGOF
disp('Magnetometer Regression')
MMDFit, MMDGOF
MMPFit, MMPGOF
MMXFit, MMXGOF
MMYFit, MMYGOF
MMZFit, MMZGOF
disp('IMU Regression')
IMUDFit, IMUDGOF
IMUPFit, IMUPGOF
IMUXFit, IMUXGOF
IMUYFit, IMUYGOF
IMUZFit, IMUZGOF

```

Reaction Wheel Functions
Maximum Torque Regression

MassT =

```

Linear model Poly1:
MassT(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      21.94 (13.62, 30.25)
p2 =      0.1656 (-0.189, 0.5203)

```

MassTGOF =

```

sse: 0.4725
rsquare: 0.9020
dfe: 5
adjrsquare: 0.8824
rmse: 0.3074

```

PowerT =

```

Linear model Poly1:
PowerT(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      6.662 (2.26, 11.06)
p2 =      0.5111 (0.3233, 0.6989)

```

PowerTGOF =

```

sse: 0.1604
rsquare: 0.6994
dfe: 5
adjrsquare: 0.6393
rmse: 0.1791

```

XDimFitT =

```

General model:
XDimFitT(x) = a*log(x) + b
Coefficients (with 95% confidence bounds):

```

```
a =      21.9 (7.559, 36.24)
b =     177.7 (109.4, 246)
```

```
XDimGof =
```

```
sse: 1.5442e+03
rsquare: 0.7550
dfe: 5
adjrsquare: 0.7060
rmse: 17.5736
```

```
YDimFitT =
```

```
General model:
YDimFitT(x) = a*log(x) + b
Coefficients (with 95% confidence bounds):
a =      21.05 (4.643, 37.46)
b =     172.1 (93.94, 250.3)
```

```
YDimGof =
```

```
sse: 2.0219e+03
rsquare: 0.6851
dfe: 5
adjrsquare: 0.6221
rmse: 20.1091
```

```
ZDimFitT =
```

```
General model:
ZDimFitT(x) = a*log(x) + b
Coefficients (with 95% confidence bounds):
a =      23.49 (-4.062, 51.05)
b =     158.4 (27.1, 289.7)
```

```
ZDimGof =
```

```
sse: 5.7022e+03
rsquare: 0.4900
dfe: 5
adjrsquare: 0.3880
rmse: 33.7703
```

```
MassH =
```

```
Linear model Poly1:
MassH(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      1.666 (1.445, 1.887)
p2 =     0.1216 (-0.009627, 0.2528)
```

```
MassTGOFH =
```

```
sse: 0.0632
rsquare: 0.9869
dfe: 5
adjrsquare: 0.9843
rmse: 0.1124
```

Maximum Momentum Capacity

PowerH =

```
Linear model Poly1:
PowerH(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      0.4666 (0.115, 0.8182)
p2 =      0.5106 (0.3016, 0.7196)
```

PowerTGOF =

```
sse: 0.1604
rsquare: 0.6994
dfe: 5
adjrsquare: 0.6393
rmse: 0.1791
```

XDimFitH =

```
General model:
XDimFitH(x) = a*log(x) + b
Coefficients (with 95% confidence bounds):
a =      20.55 (16.23, 24.87)
b =     120.4 (109.4, 131.5)
```

XDimGOFH =

```
sse: 203.7929
rsquare: 0.9677
dfe: 5
adjrsquare: 0.9612
rmse: 6.3842
```

YDimFitH =

```
General model:
YDimFitH(x) = a*log(x) + b
Coefficients (with 95% confidence bounds):
a =      20.21 (13.29, 27.12)
b =      118 (100.2, 135.7)
```

YDimGOFH =

```
sse: 522.2982
rsquare: 0.9186
dfe: 5
adjrsquare: 0.9024
rmse: 10.2205
```

ZDimFitH =

```
General model:
ZDimFitH(x) = a*log(x) + b
Coefficients (with 95% confidence bounds):
a =      23.61 (6.689, 40.53)
b =     100.2 (56.79, 143.7)
```

```
ZDimGOFH =
sse: 3.1291e+03
rsquare: 0.7201
dfe: 5
adjrsquare: 0.6641
rmse: 25.0166
```

Maxnetorquer Regression

```
MtqDFit =
Linear model Poly1:
MtqDFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      0.001029 (-0.03713, 0.03919)
p2 =      0.3457 (0.1461, 0.5453)
```

MtqDGOF =

```
sse: 0.0749
rsquare: 9.6078e-04
dfe: 5
adjrsquare: -0.1988
rmse: 0.1224
```

MtqPFit =

```
Linear model Poly1:
MtqPFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      0.05024 (-0.01899, 0.1195)
p2 =      0.399 (0.03694, 0.7611)
```

MtqPGOF =

```
sse: 0.2466
rsquare: 0.4103
dfe: 5
adjrsquare: 0.2924
rmse: 0.2221
```

MtqXFit =

```
Linear model Poly1:
MtqXFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      1.087 (-5.444, 7.618)
p2 =      17.65 (-16.51, 51.81)
```

MtqXGOF =

```
sse: 2.1946e+03
rsquare: 0.0353
dfe: 5
adjrsquare: -0.1576
rmse: 20.9505
```

```
MtqYFit =
Linear model Poly1:
MtqYFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
  p1 =      3.363 (-27.05, 33.77)
  p2 =     34.37 (-124.7, 193.4)
```

```
MtqYGOF =
sse: 4.7586e+04
rsquare: 0.0159
dfe: 5
adjrsquare: -0.1809
rmse: 97.5565
```

```
MtqZFit =
Linear model Poly1:
MtqZFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
  p1 =      26.67 (-0.7283, 54.07)
  p2 =     67.33 (-75.97, 210.6)
```

```
MtqZGOF =
sse: 3.8630e+04
rsquare: 0.5560
dfe: 5
adjrsquare: 0.4672
rmse: 87.8979
```

Star Tracker Regression

```
STDFit =
Linear model Poly2:
STDFit(x) = p1*x^2 + p2*x + p3
Coefficients:
  p1 =      -7296
  p2 =       31.79
  p3 =       2.735
```

```
STDGOF =
sse: 2.2218e-30
rsquare: 1
dfe: 0
adjrsquare: NaN
rmse: NaN
```

```
STPFit =
Linear model Poly2:
STPFit(x) = p1*x^2 + p2*x + p3
Coefficients:
  p1 = -4.592e+04
  p2 =        750
```

```
p3 = 5
```

```
STPGOF =
```

```
sse: 2.3666e-29
rsquare: 1
dfe: 0
adjrsquare: NaN
rmse: NaN
```

```
STXFit =
```

```
Linear model Poly1:
STXFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 = -6071 (-2.756e+04, 1.541e+04)
p2 = 196.3 (-128.5, 521.2)
```

```
STXGOF =
```

```
sse: 280.1667
rsquare: 0.9280
dfe: 1
adjrsquare: 0.8561
rmse: 16.7382
```

```
STYFit =
```

```
Linear model Poly1:
STYFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 = -6500 (-3.113e+04, 1.813e+04)
p2 = 200.3 (-172.1, 572.7)
```

```
STYGOF =
```

```
sse: 368.1667
rsquare: 0.9183
dfe: 1
adjrsquare: 0.8367
rmse: 19.1877
```

```
STZFit =
```

```
Linear model Poly1:
STZFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 = -1.536e+04 (-2.636e+04, -4353)
p2 = 387 (220.6, 553.4)
```

```
STZGOF =
```

```
sse: 73.5000
rsquare: 0.9968
dfe: 1
adjrsquare: 0.9937
rmse: 8.5732
```

Magnetometer Regression

MMDFit =

Linear model Poly2:
 $MMDFit(x) = p1*x^2 + p2*x + p3$
 Coefficients (with 95% confidence bounds):
 $p1 = -0.001765 (-0.009936, 0.006406)$
 $p2 = 0.04348 (-0.128, 0.2149)$
 $p3 = -0.05692 (-0.9138, 0.7999)$

MMDGOF =

sse: 0.0208
 rsquare: 0.1741
 dfe: 4
 adjrsquare: -0.2389
 rmse: 0.0721

MMMPFit =

Linear model Poly2:
 $MMMPFit(x) = p1*x^2 + p2*x + p3$
 Coefficients (with 95% confidence bounds):
 $p1 = -0.02006 (-0.05542, 0.01529)$
 $p2 = 0.3905 (-0.3514, 1.132)$
 $p3 = -1.254 (-4.961, 2.454)$

MMPGOF =

sse: 0.3889
 rsquare: 0.4134
 dfe: 4
 adjrsquare: 0.1202
 rmse: 0.3118

MMXFit =

Linear model Poly1:
 $MMXFit(x) = p1*x + p2$
 Coefficients (with 95% confidence bounds):
 $p1 = -2.795 (-16.24, 10.65)$
 $p2 = 108 (-26.72, 242.7)$

MMXGOF =

sse: 7.1582e+03
 rsquare: 0.0541
 dfe: 5
 adjrsquare: -0.1351
 rmse: 37.8371

MMYFit =

Linear model Poly1:
 $MMYFit(x) = p1*x + p2$
 Coefficients (with 95% confidence bounds):
 $p1 = -0.3261 (-13.16, 12.51)$

```
p2 =      56.92 (-71.74, 185.6)
```

```
MMYGOF =
```

```
sse: 6.5270e+03
rsquare: 8.5208e-04
dfe: 5
adjrsquare: -0.1990
rmse: 36.1304
```

```
MMZFit =
```

```
Linear model Poly1:
MMZFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      -3.896 (-12.12, 4.327)
p2 =      74.57 (-7.854, 157)
```

```
MMZGOF =
```

```
sse: 2.6792e+03
rsquare: 0.2288
dfe: 5
adjrsquare: 0.0746
rmse: 23.1480
```

IMU Regression

```
IMUDFit =
```

```
Linear model Poly1:
IMUDFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      -0.04192 (-0.4176, 0.3337)
p2 =      0.0934 (-0.1124, 0.2992)
```

```
IMUDGOF =
```

```
sse: 0.0084
rsquare: 0.1034
dfe: 2
adjrsquare: -0.3450
rmse: 0.0647
```

```
IMUPFit =
```

```
Linear model Poly1:
IMUPFit(x) = p1*x + p2
Coefficients (with 95% confidence bounds):
p1 =      -0.4949 (-3.239, 2.249)
p2 =      0.8871 (-0.6161, 2.39)
```

```
IMUPGOF =
```

```
sse: 0.4473
rsquare: 0.2314
dfe: 2
adjrsquare: -0.1530
rmse: 0.4729
```

```
IMUXFit =  
  
Linear model Poly1:  
IMUXFit(x) = p1*x + p2  
Coefficients (with 95% confidence bounds):  
p1 = -21.93 (-245.4, 201.5)  
p2 = 68.84 (-53.56, 191.2)
```

```
IMUXGOF =  
  
sse: 2.9657e+03  
rsquare: 0.0818  
dfe: 2  
adjrsquare: -0.3773  
rmse: 38.5077
```

```
IMUYFit =  
  
Linear model Poly1:  
IMUYFit(x) = p1*x + p2  
Coefficients (with 95% confidence bounds):  
p1 = -10.02 (-154.4, 134.3)  
p2 = 54.79 (-24.28, 133.9)
```

```
IMUYGOF =  
  
sse: 1.2375e+03  
rsquare: 0.0427  
dfe: 2  
adjrsquare: -0.4359  
rmse: 24.8748
```

```
IMUZFit =  
  
Linear model Poly1:  
IMUZFit(x) = p1*x + p2  
Coefficients (with 95% confidence bounds):  
p1 = -2.082 (-53.07, 48.9)  
p2 = 34.59 (6.663, 62.52)
```

```
IMUZGOF =  
  
sse: 154.3662  
rsquare: 0.0152  
dfe: 2  
adjrsquare: -0.4772  
rmse: 8.7854
```

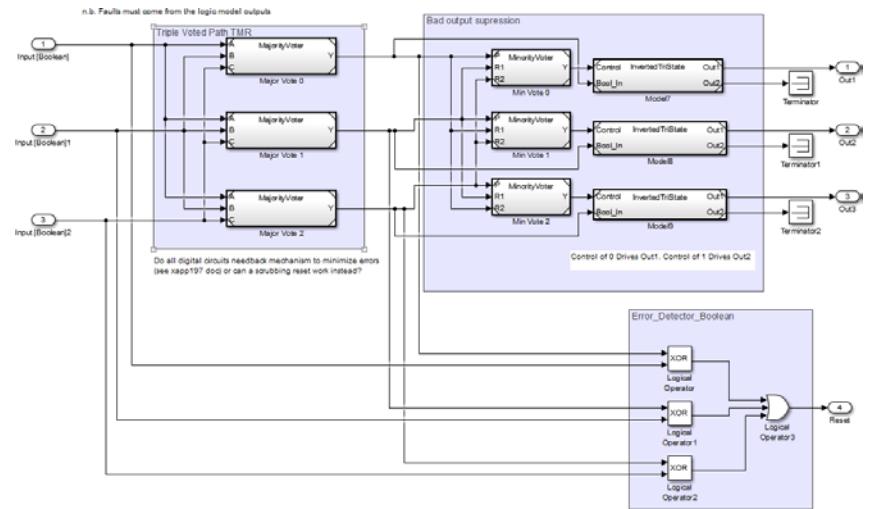


Figure C.1: TMR Model

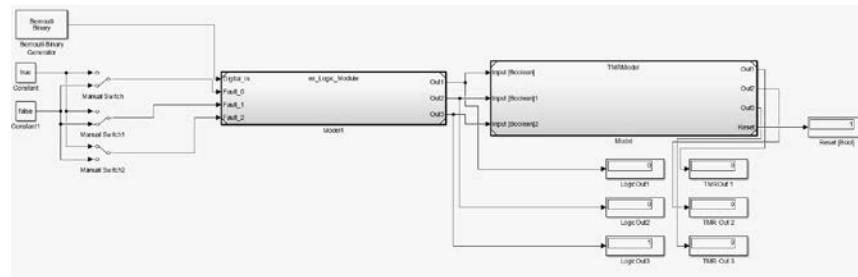


Figure C.2: TMR test detecting error

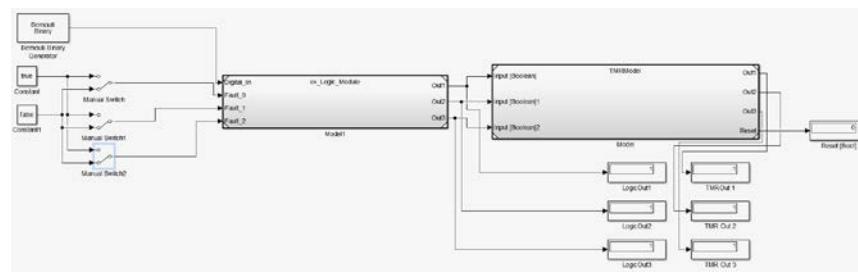


Figure C.3: TMR test detecting no failures

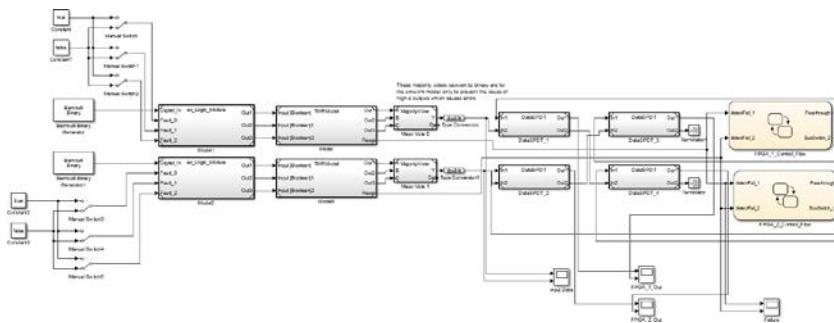


Figure C.4: Setup to test a novel switching algorithm

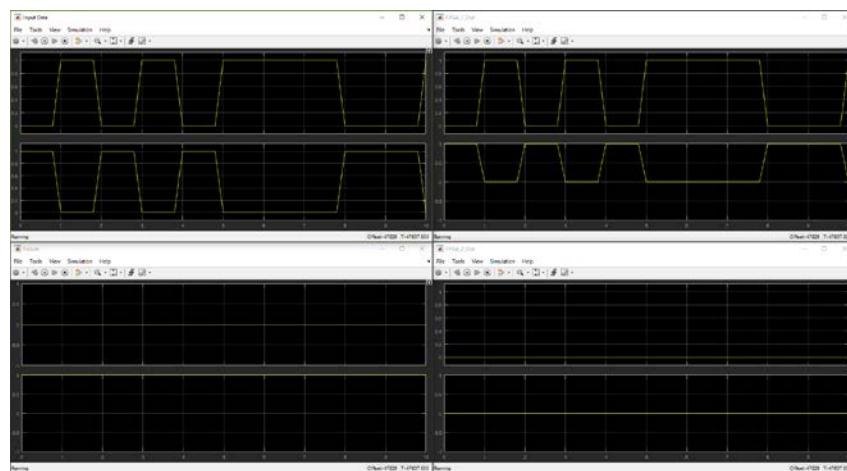


Figure C.5: Detection of a failed fpga.

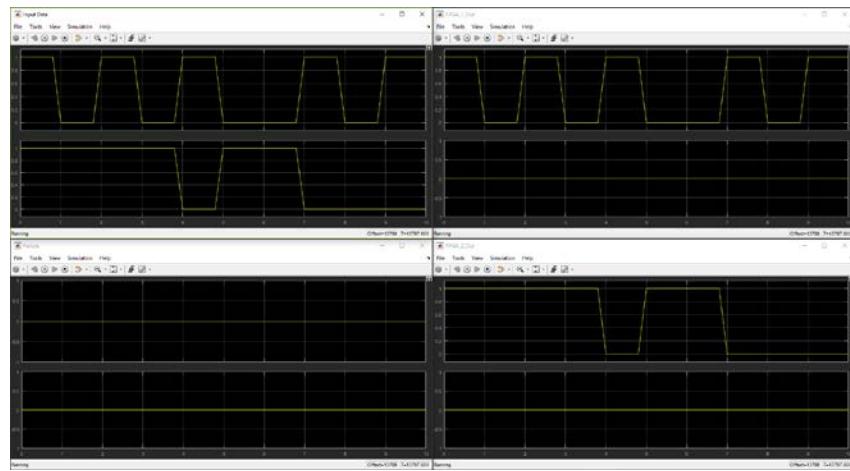


Figure C.6: No failures detected in FPGAs

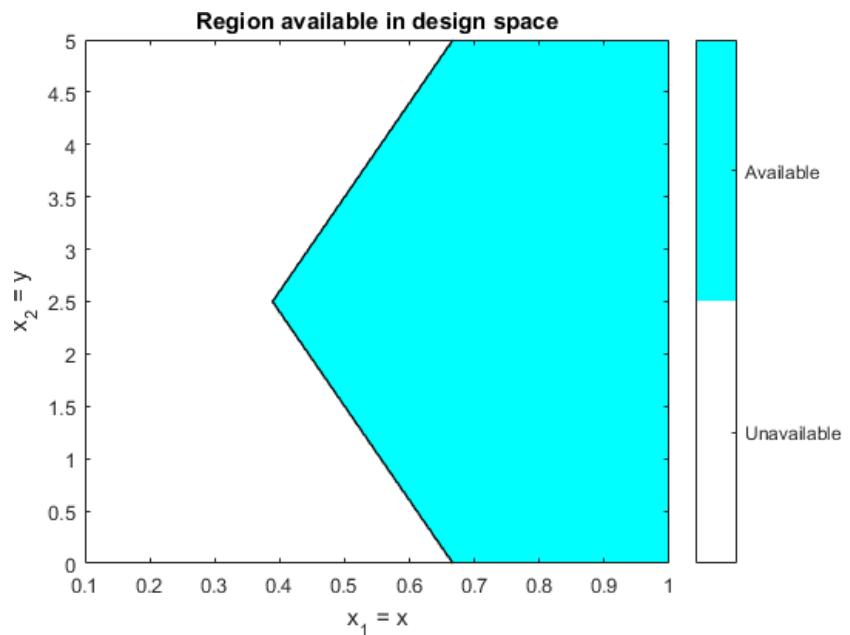


Figure C.7: Design space of benchmark optimization problem

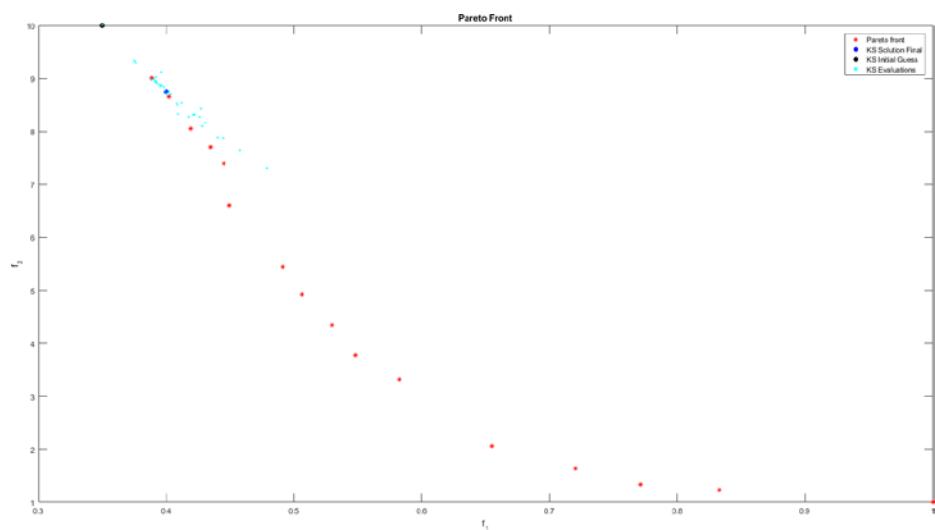


Figure C.8: Evaluation from the initialization point of the KS function. The initial function is outside of the feasible design space while the final solution is feasible and located within the Pareto optimized region.

Data Rate Response

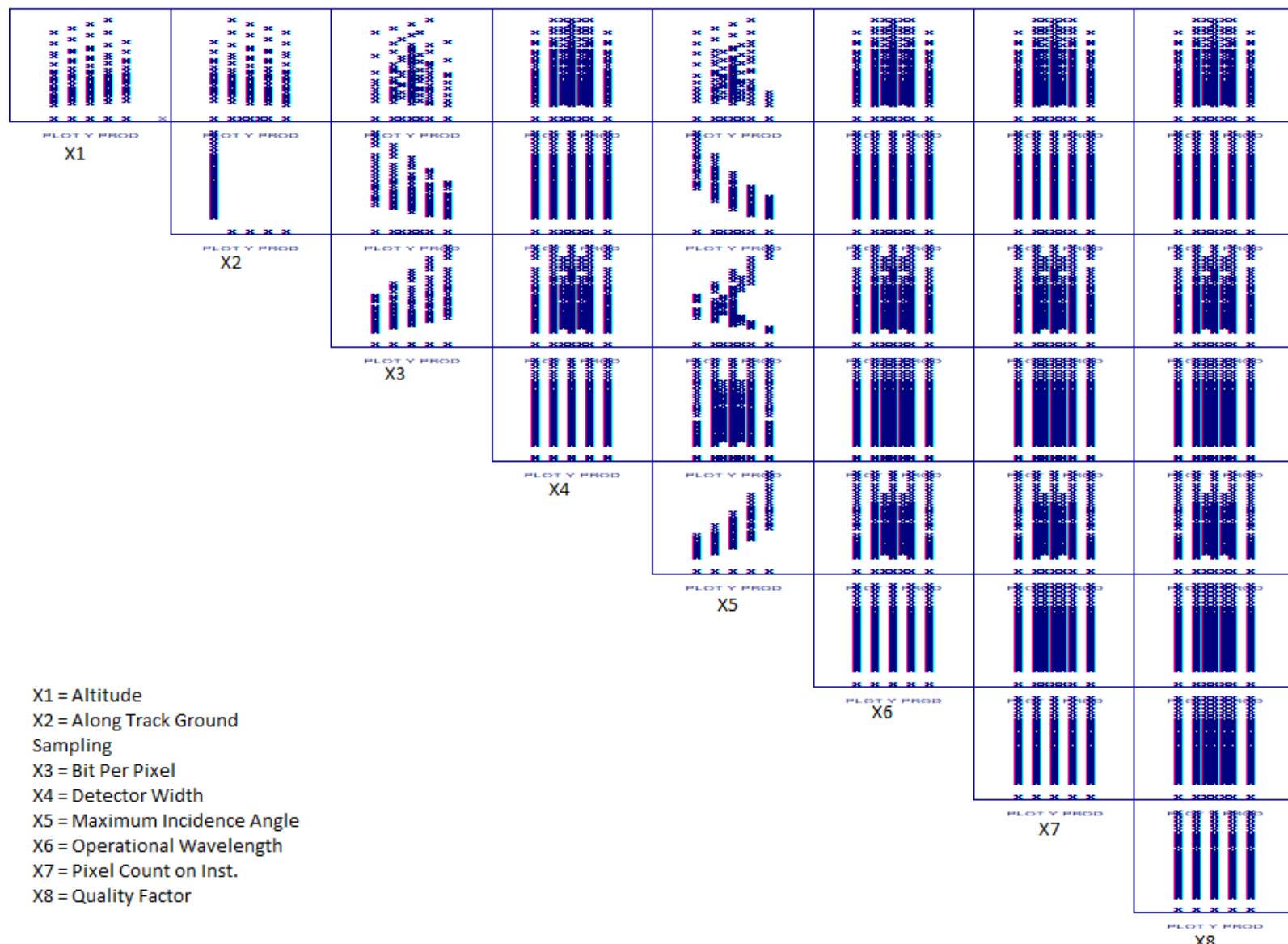


Figure C.9: DoE scatter plot of Aperture Diameter

Pixel Integration Time Response

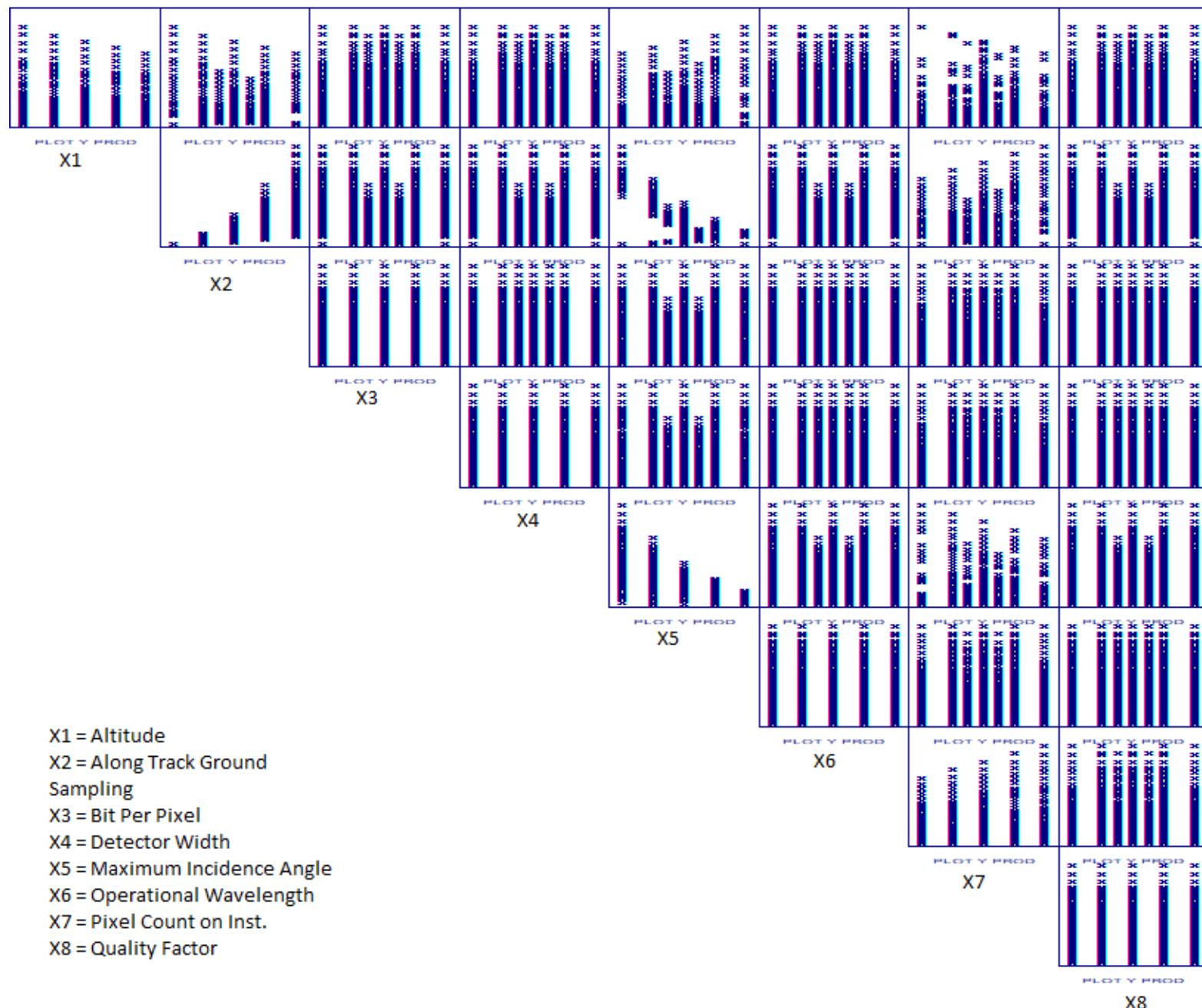


Figure C.10: DoE scatter plot of Aperture Diameter

Payload Power Estimate Response

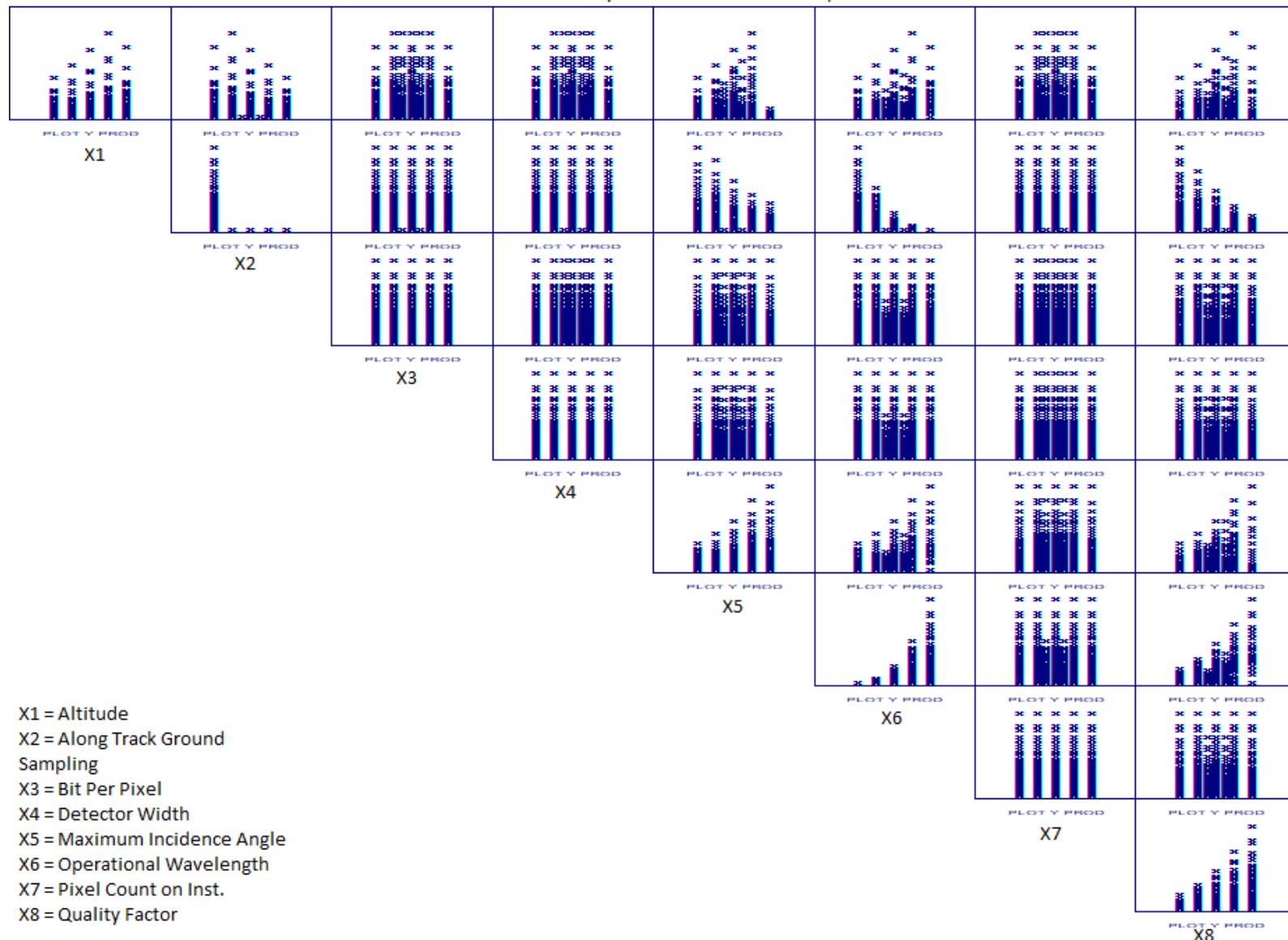


Figure C.11: DoE scatter plot of Aperture Diameter

Contents

- Data Analysis for DOEs
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- Reaction Wheel
- Magnetorquers
- StarTracker

Data Analysis for DOEs

```
clc; clear all; close all;
```

READ Payload Data file

```
if exist('ADCSDOEData.mat', 'file') == 2
    load('ADCSDOEData.mat') %Saves a few minutes if the data has been parsed and saved and analyzed
else
```

```

fid = fopen('DOE_ACDS', 'r');
text = textscan(fid, '%s', 'Delimiter', '', 'endofline', '');
text = text{1}{1};
fid = fclose(fid);
AerodynamicTorque = regexp(text, 'AerodynamicTorque:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
CenterGravity = regexp(text, 'CenterGravity:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
CenterPressure = regexp(text, 'CenterPressure:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
CenterSolarPressure = regexp(text, 'CenterSolarPressure:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
CoeffDrag = regexp(text, 'CoeffDrag:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
Density = regexp(text, 'Density:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
DisturbanceTorque = regexp(text, 'DisturbanceTorque:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens'); %modified to nt contain IFOV
GravityGradient = regexp(text, 'GravityGradient:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
IncidenceAngle = regexp(text, 'IncidenceAngle:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
Iy = regexp(text, 'Iy:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
Iz = regexp(text, 'Iz:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MagDipole = regexp(text, 'MagDipole:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MagneticField = regexp(text, 'MagneticField:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MomentumStorageRx = regexp(text, 'MomentumStorageRx:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MtxMass = regexp(text, 'MtxMass:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MtxPWR = regexp(text, 'MtxPWR:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MtxX = regexp(text, 'MtxX:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MtxY = regexp(text, 'MtxY:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
MtxZ = regexp(text, 'MtxZ:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
OrbPer = regexp(text, 'OrbPer:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
PointKnowledge = regexp(text, 'PointKnowledge:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
Radius = regexp(text, 'Radius:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
ReflectanceFactor = regexp(text, 'ReflectanceFactor:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
ResidualDipole = regexp(text, 'ResidualDipole:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
RxMass = regexp(text, 'RxMass:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
RxPWR = regexp(text, 'RxPWR:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
RxX = regexp(text, 'RxX:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
RxY = regexp(text, 'RxY:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
RxZ = regexp(text, 'RxZ:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
STMass = regexp(text, 'STMass:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
STPWR = regexp(text, 'STPWR:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
STX = regexp(text, 'STX:\s+(\d*(.)?(\d*)?(e)?[+-]?(\\d*))', 'tokens');
```

```

STY = regexp(text,'STY:\s+(\d*(.)?\d*)(e)?[+-]?(d*)','tokens');
STZ = regexp(text,'STZ:\s+(\d*(.)?\d*)(e)?[+-]?(d*)','tokens');
SolarRadiation = regexp(text,'SolarRadiation:\s+(\d*(.)?\d*)(e)?[+-]?(d*)','tokens');
SunIA = regexp(text,'SunIA:\s+(\d*(.)?\d*)(e)?[+-]?(d*)','tokens');
SurfaceArea = regexp(text,'SurfaceArea:\s+(\d*(.)?\d*)(e)?[+-]?(d*)','tokens');
clear text fid%Remove file to clear up memory

```

Convert to Usable Doubles

```

AerodynamicTorque = str2double([AerodynamicTorque{:}]');
CenterGravity = str2double([CenterGravity{:}]');
CenterPressure = str2double([CenterPressure{:}]');
CenterSolarPressure = str2double([CenterSolarPressure{:}]');
CoeffDrag = str2double([CoeffDrag{:}]');
Density = str2double([Density{:}]');
DisturbanceTorque = str2double([DisturbanceTorque{:}]');
GravityGradient = str2double([GravityGradient{:}]');
IncidenceAngle = str2double([IncidenceAngle{:}]');
Iy = str2double([Iy{:}]');
Iz = str2double([Iz{:}]');
MagDipole = str2double([MagDipole{:}]');
MagneticField = str2double([MagneticField{:}]');
MomentumStorageRx = str2double([MomentumStorageRx{:}]');
MtxMass = str2double([MtxMass{:}]');
MtxPWR = str2double([MtxPWR{:}]');
MtxX = str2double([MtxX{:}]');
MtxY = str2double([MtxY{:}]');
MtxZ = str2double([MtxZ{:}]');
OrbPer = str2double([OrbPer{:}]');
PointKnowledge = str2double([PointKnowledge{:}]');
Radius = str2double([Radius{:}]');
ReflectanceFactor = str2double([ReflectanceFactor{:}]');
ResidualDipole = str2double([ResidualDipole{:}]');
RxMass = str2double([RxMass{:}]');
RxPWR = str2double([RxPWR{:}]');
RxX = str2double([RxX{:}]');
RxY = str2double([RxY{:}]');
RxZ = str2double([RxZ{:}]');
STMass = str2double([STMass{:}]');
STPWR = str2double([STPWR{:}]');
STX = str2double([STX{:}]');
STY = str2double([STY{:}]');
STZ = str2double([STZ{:}]');
SolarRadiation = str2double([SolarRadiation{:}]');
SunIA = str2double([SunIA{:}]');
SurfaceArea = str2double([SurfaceArea{:}]');

```

Remove NaN caused by metadata and parameter saving

```

AerodynamicTorque = AerodynamicTorque(~isnan(AerodynamicTorque));
CenterGravity = CenterGravity(~isnan(CenterGravity));
CenterPressure = CenterPressure(~isnan(CenterPressure));
CenterSolarPressure = CenterSolarPressure(~isnan(CenterSolarPressure));
Density = Density(~isnan(Density));
CoeffDrag = CoeffDrag(~isnan(CoeffDrag));
DisturbanceTorque = DisturbanceTorque(~isnan(DisturbanceTorque));
GravityGradient = GravityGradient(~isnan(GravityGradient));
IncidenceAngle = IncidenceAngle(~isnan(IncidenceAngle));
Iy = Iy(~isnan(Iy));
Iz = Iz(~isnan(Iz));
MagDipole = MagDipole(~isnan(MagDipole));
MagneticField = MagneticField(~isnan(MagneticField));
MomentumStorageRx = MomentumStorageRx(~isnan(MomentumStorageRx));
MtxMass = MtxMass(~isnan(MtxMass));
MtxPWR = MtxPWR(~isnan(MtxPWR));
MtxX = MtxX(~isnan(MtxX));
MtxY = MtxY(~isnan(MtxY));
MtxZ = MtxZ(~isnan(MtxZ));
OrbPer = OrbPer(~isnan(OrbPer));

```

```

PointKnowledge = PointKnowledge(~isnan(PointKnowledge));
Radius = Radius(~isnan(Radius));
ReflectanceFactor = ReflectanceFactor(~isnan(ReflectanceFactor));
ResidualDipole = ResidualDipole(~isnan(ResidualDipole));
RxMass = RxMass(~isnan(RxMass));
RxPWR = RxPWR(~isnan(RxPWR));
RxX = RxX(~isnan(RxX));
RxY = RxY(~isnan(RxY));
RxZ = RxZ(~isnan(RxZ));
STMass = STMass(~isnan(STMass));
STPWR = STPWR(~isnan(STPWR));
STX = STX(~isnan(STX));
STY = STY(~isnan(STY));
STZ = STZ(~isnan(STZ));
SolarRadiation = SolarRadiation(~isnan(SolarRadiation));
SunIA = SunIA(~isnan(SunIA));
SurfaceArea = SurfaceArea(~isnan(SurfaceArea));
save('ADCSDOEData.mat')

```

```
end
```

Design Variable Orthogonalization

Design variables include radius, Iy, Iz, Reflectance Factor, SunIA, Cd, Pt Knowledge

```

[Radius, RadiusA, RadiusB] = CodeFactorLevel(Radius);
[Iy, IyA, IyB] = CodeFactorLevel(Iy);
[Iz, IzA, IzB] = CodeFactorLevel(Iz);
[ReflectanceFactor, RFA, RFB] = CodeFactorLevel(ReflectanceFactor);
[SunIA, SIAA, SIAB] = CodeFactorLevel(SunIA);
[CoeffDrag, CDA, CDB] = CodeFactorLevel(CoeffDrag);
[PointKnowledge, PKA, PKB] = CodeFactorLevel(PointKnowledge);
[ResidualDipole, RDA, RDB] = CodeFactorLevel(ResidualDipole);

```

Response Variable Test of Normality

```

[H, PVal, WStatistic] = kstest(RxX);
if H == 0
    fprintf('RxX / RxY is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('RxX/RxY is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(RxZ);
if H == 0
    fprintf('RxZ is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('RxZ is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(RxMass);
if H == 0
    fprintf('RxMass is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('RxMass is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(RxPWR);
if H == 0
    fprintf('RxPWR is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('RxPWR is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(MtxX);
if H == 0

```

```

fprintf('Mtx is a normal distribution with PVal %d and Wstat %d.\n',...
    PVal, WStatistic)
else
    fprintf('Mtx is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(MtxZ);
if H == 0
    fprintf('MtxZ is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('MtxZ is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(MtxMass);
if H == 0
    fprintf('MtxMass is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('MtxMass is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(MtxPWR);
if H == 0
    fprintf('MtxPWR is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('MtxPWR is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(STX);
if H == 0
    fprintf('STX is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('STX is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(STZ);
if H == 0
    fprintf('STZ is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('STZ is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(STMass);
if H == 0
    fprintf('STMass is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('STMass is not a normal distribution.\n')
end
[H, PVal, WStatistic] = kstest(STPWR);
if H == 0
    fprintf('STPWR is a normal distribution with PVal %d and Wstat %d.\n',...
        PVal, WStatistic)
else
    fprintf('STPWR is not a normal distribution.\n')
end

```

RxX/RxY is not a normal distribution.
RxZ is not a normal distribution.
RxMass is not a normal distribution.
RxPWR is not a normal distribution.
Mtx is not a normal distribution.
MtxZ is not a normal distribution.
MtxMass is not a normal distribution.
MtxPWR is not a normal distribution.
STX is not a normal distribution.
STZ is not a normal distribution.
STMass is not a normal distribution.
STPWR is not a normal distribution.

ANOVA Test

Can not be run due to non-normal response distribution

Data Files for NIST DATAPlot

For a 8^5 factorial analysis these end up around 42MB per response variable

```

DesVarData = [Radius, Iy, Iz, ReflectanceFactor, SunIA, CoeffDrag, PointKnowledge, ResidualDipole];
%Reaction Wheel
Data = [3*RxX.*RxY.*RxZ/1000/1000/1000, DesVarData]';
fileID = fopen('ADCSRxVol.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

Data = [3*RxMass, DesVarData]';
fileID = fopen('ADCSRxMass.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

Data = [3*RxPWR, DesVarData]';
fileID = fopen('ADCSRxPower.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

%Star Tracker
Data = [STX.*STY.*STZ/1000/1000/1000, DesVarData]';
fileID = fopen('ADCSSTVol.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

Data = [STMass, DesVarData]';
fileID = fopen('ADCSSTMass.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

Data = [STPWR, DesVarData]';
fileID = fopen('ADCSSTPower.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

%MagneticTorqueRod
Data = [2*MtxX.*MtxY.*MtxZ/1000/1000/1000, DesVarData]';
fileID = fopen('ADCSMagTorqueVol.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

Data = [2*MtxMass, DesVarData]';
fileID = fopen('ADCSMagTorqueMass.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

Data = [2*MtxPWR, DesVarData]';
fileID = fopen('ADCSMagTorquePower.dat','w');
fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s\r\n','Y','X1','X2','X3','X4','X5','X6','X7','X8');
fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f\r\n',Data);
fclose(fileID);

```

Orthogonality Verification

```

DesVars = {Radius,Iy, Iz, ReflectanceFactor, SunIA, CoeffDrag, PointKnowledge, ResidualDipole};
NUMFAC = length(DesVars);
orthocheck = zeros(NUMFAC);
for i = 1:NUMFAC
    for j = 1:NUMFAC
        orthocheck(i,j) = sum(Data(i+1,:).*Data(j+1,:));

```

```

    if i == j
        orthocheck(i,j) = 0;
    end

end
disp(orthocheck)

```

1.0e-12 *

Columns 1 through 7

0	0.3182	0.0893	0	0	0	-0.2274
0.3182	0	-0.2056	0.0056	-0.0016	0	-0.4545
0.0893	-0.2056	0	0.0018	0.0018	0	0.3411
0	0.0056	0.0018	0	0	0	-0.2274
0	-0.0016	0.0018	0	0	0	-0.2274
0	0	0	0	0	0	0
-0.2274	-0.4545	0.3411	-0.2274	-0.2274	0	0
0.0002	0.2269	0.2218	0.0002	0.0002	0	-0.4545

Column 8

0.0002
0.2269
0.2218
0.0002
0.0002
0
-0.4545
0

DOE Interaction Plot VERIFICATION FOR NIST

Reaction Wheel

```

Data(1,:) = 3*RxX.*RxY.*RxZ;
fRxVol = figure;
NUMFAC = length(DesVars);
DesVarNames = {'Radius','Ix','Iz','ReflectanceFactor','SunIA','CoeffDrag',...
    'PointKnowledge', 'ResidualDipole'};
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end
a = axes;
t1 = title('RxWheel Volume (mm^3) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
Data(1,:) = 3*RxMass;
fRxMass = figure;

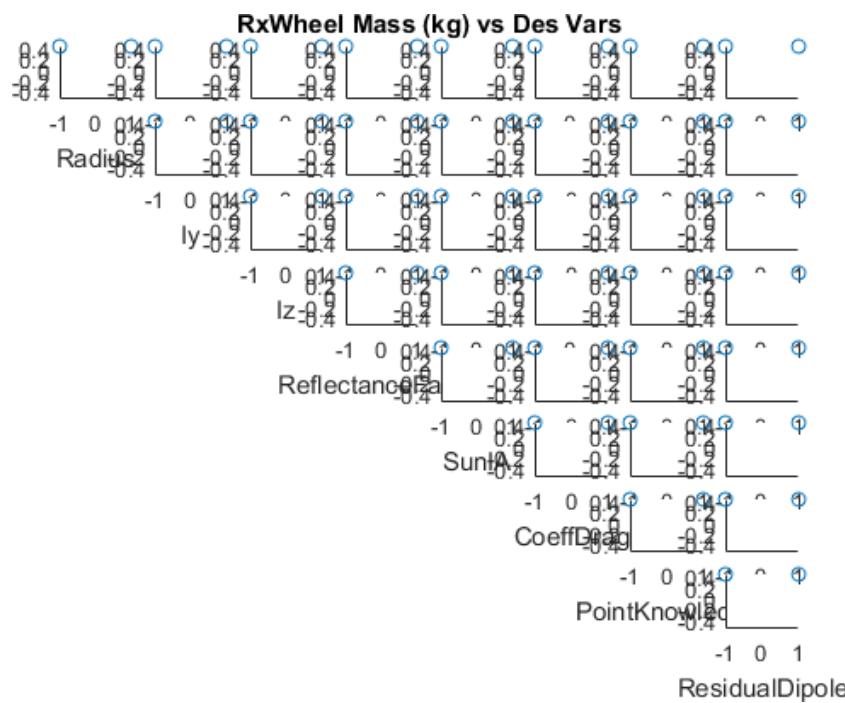
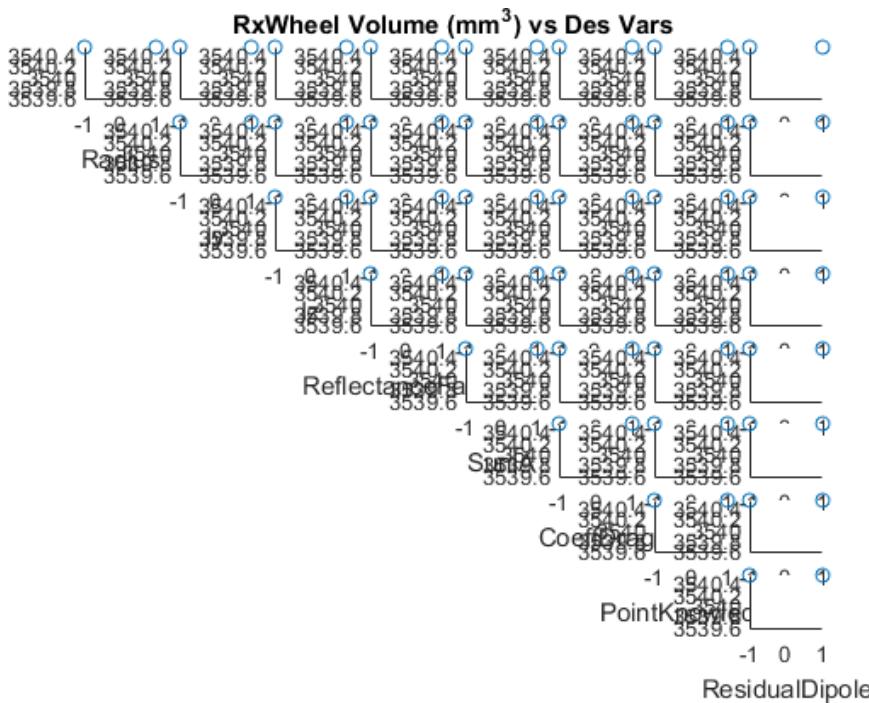
for i = 1:NUMFAC
    for j = 1:NUMFAC

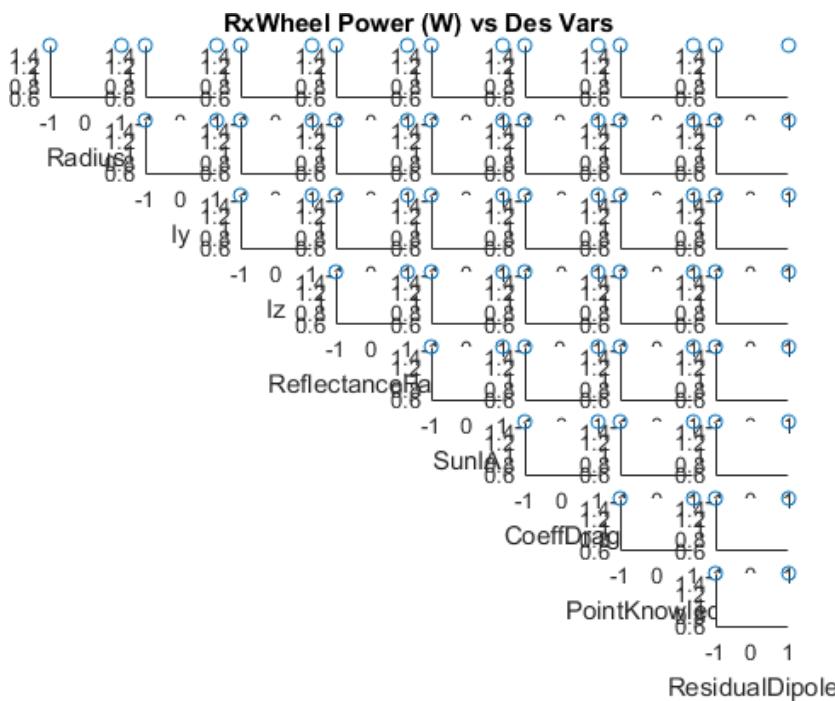
```

```

if i == j
    varname = cellstr(DesVarNames{i});
    subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
    scatter(Data(i+1,:),Data(1,:))
    xlabel(varname)
    axis([-1 1 -inf inf])
elseif j > i
    KVec = Data(i+1,:).*Data(j+1,:);
%disp(min(KVec));
%disp(max(KVec));
    subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
    scatter(KVec,Data(1,:))
    axis([-1 1 -inf inf])
end
end
a = axes;
t1 = title('RxWheel Mass (kg) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
Data(1,:) = 3*RxPWR;
fRxPower = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
%disp(min(KVec));
%disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end
a = axes;
t1 = title('RxWheel Power (W) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');

```





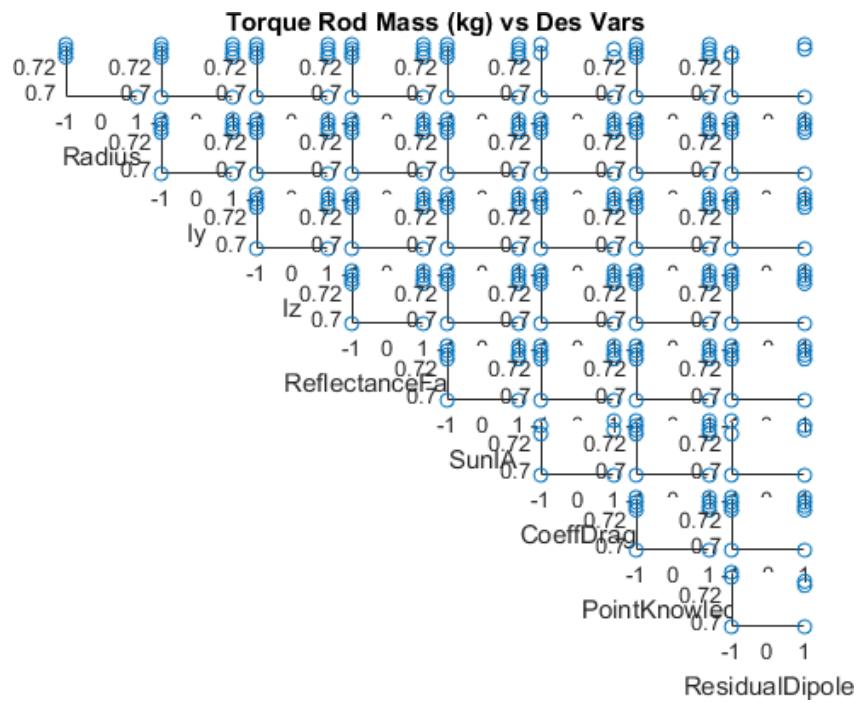
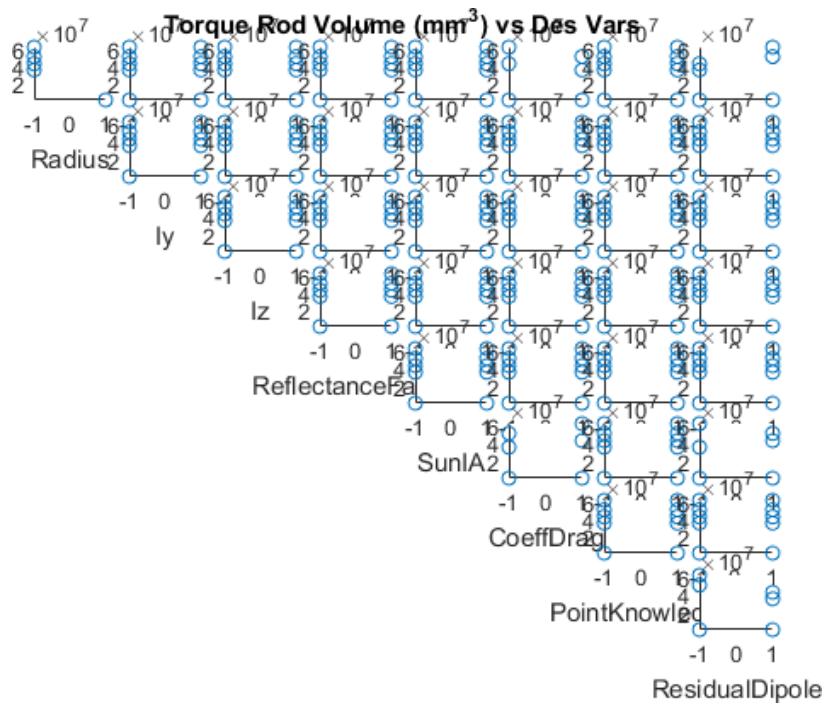
Magnetorquers

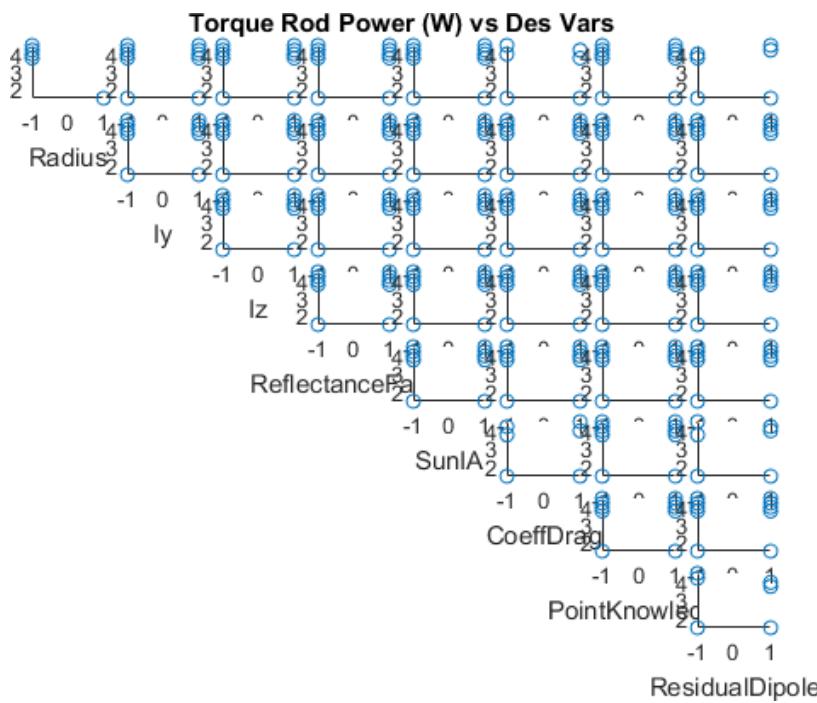
```

Data(1,:) = 2*MtxX.*MtxY.*MtxZ;
fRxVol = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end
a = axes;
t1 = title('Torque Rod Volume (mm^3) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
Data(1,:) = 2*MtxMass;
fRxMass = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end

```

```
    end
end
a = axes;
t1 = title('Torque Rod Mass (kg) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
Data(1,:) = 3*MtxPWR;
fRxPower = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end
a = axes;
t1 = title('Torque Rod Power (W) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
```





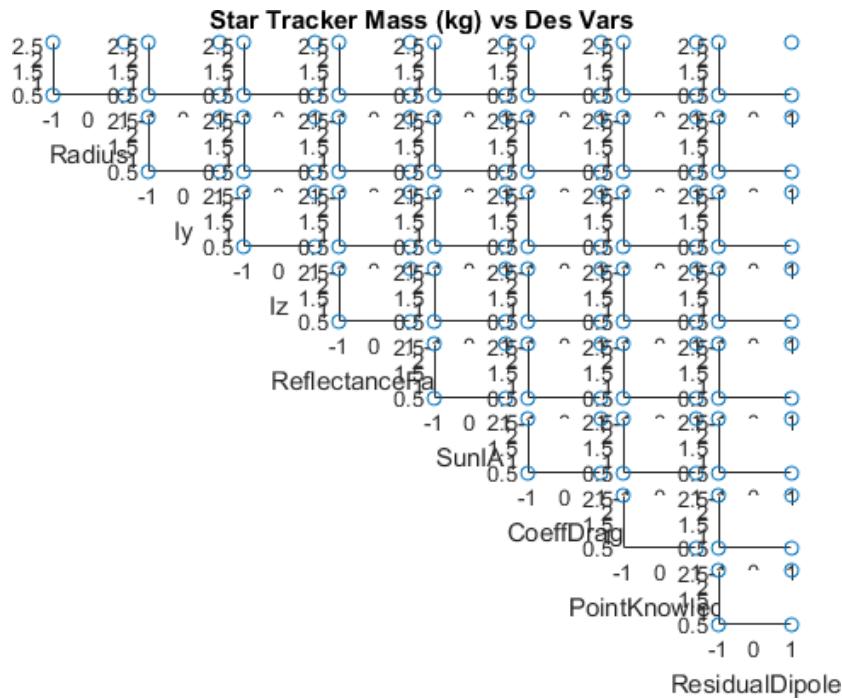
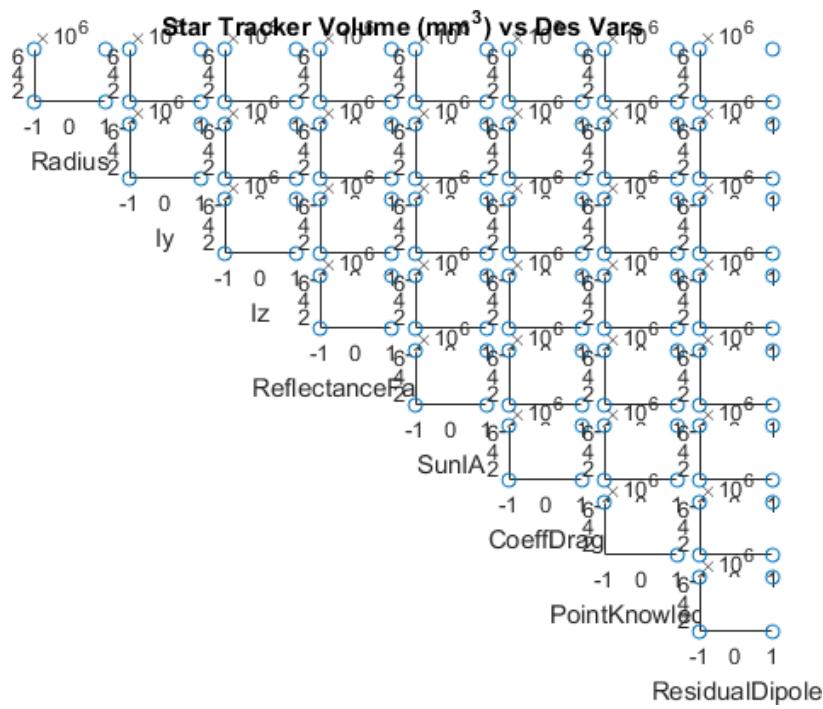
StarTracker

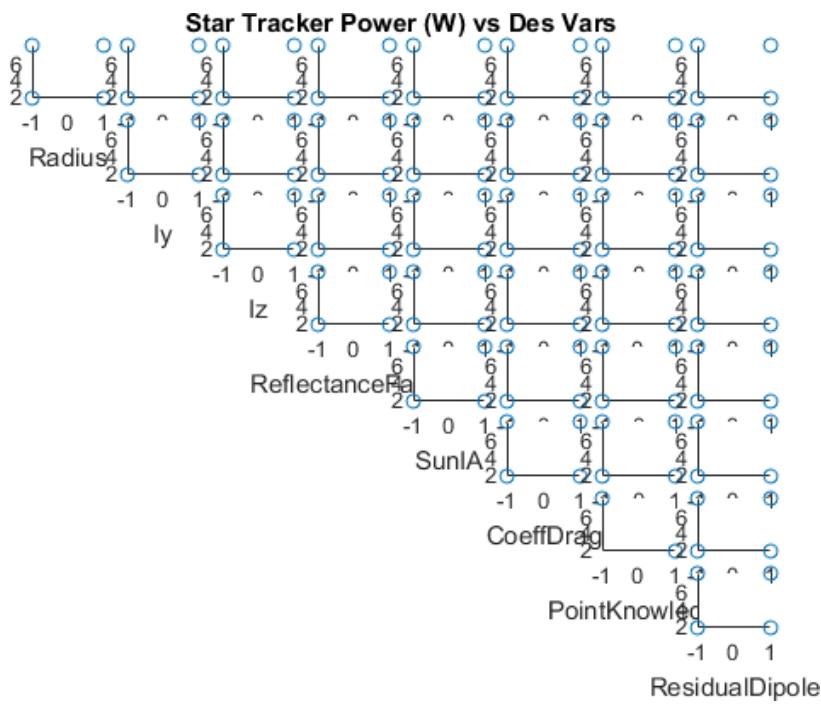
```

Data(1,:) = STX.*STY.*STZ;
fSTVol = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end
a = axes;
t1 = title('Star Tracker Volume (mm^3) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
Data(1,:) = STMass;
fRxMass = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end

```

```
    end
end
a = axes;
t1 = title('Star Tracker Mass (kg) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
Data(1,:) = STPWR;
fRxPower = figure;
for i = 1:NUMFAC
    for j = 1:NUMFAC
        if i == j
            varname = cellstr(DesVarNames{i});
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(Data(i+1,:),Data(1,:))
            xlabel(varname)
            axis([-1 1 -inf inf])
        elseif j > i
            KVec = Data(i+1,:).*Data(j+1,:);
            %disp(min(KVec));
            %disp(max(KVec));
            subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
            scatter(KVec,Data(1,:))
            axis([-1 1 -inf inf])
        end
    end
end
a = axes;
t1 = title('Star Tracker Power (W) vs Des Vars');
a.Visible = 'off'; % set(a,'Visible','off');
t1.Visible = 'on'; % set(t1,'Visible','on');
```





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Appendix D

CODES

D.1 Design of Experiments

D.1.1 Code Factor Level

```

1 function [Y,a,b] = CodeFactorLevel(U)
2     a = (max(U)+min(U))/2;
3     b = (max(U)-min(U))/2;
4     Y = (U-a)/b;
5 end

```

D.1.2 Inverse Code Factor Level

```

1 function Y = InvCodeFactorLevel(U,a,b)
2 %U is the coded values from CodeFactorLevel()
3 %a is the constant provided by CodeFactorLevel()
4 %b is the constant provided by CodeFactorLevel()
5 Y = b*U+a;
6 end

```

D.1.3 DOE Payload

```

1 import numpy as np
2 import math
3
4 from openmdao.api import Component, IndepVarComp, Group, Component
, Problem, ScipyOptimizer, ExecComp, DumpRecorder

```

```
5 from openmdao.drivers.fullfactorial_driver import
6     FullFactorialDriver
7
8     class OrbitPeriod(Component):
9         """ Evaluates the period for a circular orbit in min:1
10            .658669e-04*(6378.14+Altitude)**(3/2) """
11
12     def __init__(self):
13         super(OrbitPeriod, self).__init__()
14         self.add_param('Altitude', val=0.0)
15         self.add_output('OrbPer', val=1.0)
16
17     def solve_nonlinear(self, params, unknowns, resids):
18         h1 = params['Altitude']
19         unknowns['OrbPer'] = 1.658669e-04*(6378.14+h1)**1.5
20
21     def linearize(self, params, unknowns, resids):
22         J = {}
23         J['OrbPer', 'Altitude'] = 0.0002488*(6378.14+params['Altitude'])**.5
24
25     return J
26
27
28     class GroundVelocity(Component):
29         """ Evaluates the equation f(x,y) = 2*pi*Re/P"""
30
31     def __init__(self):
32         super(GroundVelocity, self).__init__()
33         self.add_param('OrbPer', val=0.0)
```

```

29         self.addoutput('GroundVelocity', val=1.)
30
31     def solve_nonlinear(self, params, unknowns, resids):
32         OrbPer1 = params['OrbPer']
33         unknowns['GroundVelocity'] = 2*math.pi*6378.14/OrbPer1/60
34
35     def linearize(self, params, unknowns, resids):
36         J = {}
37         J['GroundVelocity', 'OrbPer'] = 40074.2496/params['OrbPer'
38             ]**2
39
40     class AngularRadius(Component):
41         """Angular Radius as seen from spacecraft"""
42         def __init__(self):
43             super(AngularRadius, self).__init__()
44             self.add_param('Altitude', val=0.0)
45             self.addoutput('AngRadius', val=0.0)
46
47         def solve_nonlinear(self, params, unknowns, resids):
48             h1 = params['Altitude']
49             unknowns['AngRadius'] = math.asin(6378.14/(6378+h1))*180/
50                         math.pi #returns in degrees
51
52         def linearize(self, params, unknowns, resids):
53             J = {}
54             J['AngRadius', 'Altitude'] = -(6378.14*((params['Altitude']-

```

```

] + 6378.14) ** 2) ** .5) / ((6378.14 + params[ 'Altitude' ]) ** 2 * (
params[ 'Altitude' ] ** 2 + 12756.28 * params[ 'Altitude' ])
* * .5)

54

55 class LNot(Component):
56     """Angular Radius measured from the center of earth of the
57     region seen by the spacecraft"""
58
59     def __init__(self):
60         super(LNot, self).__init__()
61         self.add_param('AngRadius', val=0.0)
62         self.addoutput('LNot', val=0.0)

63

64     def solve_nonlinear(self, params, unknowns, resids):
65         AngRadius = params[ 'AngRadius' ]
66         unknowns[ 'LNot' ] = 90 - AngRadius #returns in degrees

67

68     def linearize(self, params, unknowns, resids):
69         J = {}
70         J[ 'LNot', 'AngRadius' ] = -1
71         return J

72

73 class DMax(Component):
74     """Solves for the distance to the horizon from the satellite
75     """
76
77     def __init__(self):
78         super(DMax, self).__init__()

```

```

76         self.add_param('LNot', val=0.0)
77         self.add_output('DMax', val=0.0)
78
79     def solve_nonlinear(self, params, unknowns, resids):
80         LNot = params['LNot']
81         unknowns['DMax'] = math.tan(LNot*math.pi/180)*6378.14 #
82
83         returns km
84
85     def linearize(self, params, unknowns, resids):
86         J = {}
87         J[ 'DMax' , 'LNot' ] = 6378.14/(tan(params[ 'LNot' ]*math.pi
88
89         /180)**2)
90
91         return J
92
93
94     class EtaLook(Component):
95
96         """Nadir Angle Range"""
97
98         def __init__(self):
99             super(EtaLook, self).__init__()
100            self.add_param('IMax', val=0.0)
101            self.add_param('AngRadius', val=0.0)
102            self.add_output('EtaLook', val=0.0)
103
104
105        def solve_nonlinear(self, params, unknowns, resids):
106            IMax = params['IMax']
107            AngRadius = params['AngRadius']
108            unknowns['EtaLook'] = math.asin(math.cos((90-IMax)*math.
109
110            pi/180)*math.sin(AngRadius*math.pi/180))*180/math.pi #

```

```

    returns deg

100
101     def linearize(self, params, unknowns, resids):
102         J = {}
103         J[ 'EtaLook', 'IAMax' ] = -(math.sin(params[ 'IAMax' ]*math.pi
104                                         /180) * math.sin(params[ 'AngRadius' ]*math.pi/180))
105                                         /((1-math.cos(params[ 'IAMax' ]*math.pi/180)**2*math.sin(
106                                         (params[ 'AngRadius' ]*math.pi/180)**2))**0.5
107
108         J[ 'EtaLook', 'AngRadius' ] = math.cos(params[ 'IAMax' ]*math.pi/180)*math.cos(params[ 'AngRadius' ]*math.pi/180)/(1-
109                                         math.cos(params[ 'IAMax' ]*math.pi/180)**2*math.sin(
110                                         (params[ 'AngRadius' ]*math.pi/180)**2))**0.5
111
112         return J
113
114     class ECAMax(Component):
115         def __init__(self):
116             super(ECAMax, self).__init__()
117             self.add_param('EtaLook', val=0.0)
118             self.add_param('IAMax', val=0.0)
119             self.add_output('ECAMax', val=0.0)
120
121
122     def solve_nonlinear(self, params, unknowns, resids):
123         EtaLook = params[ 'EtaLook' ]
124         IAMax = params[ 'IAMax' ]
125         unknowns[ 'ECAMax' ] = 90-(90-IAMax)-EtaLook #returns deg
126
127
128     def linearize(self, params, unknowns, resids):
129

```

```

120 J = {}

121 J[ 'ECAMax' , ' IAMax ' ]= -1

122 J[ 'ECAMax' , ' EtaLook ' ]= -1

123 return J

124

125 class SlantRange(Component):
126     def __init__(self):
127         super(SlantRange, self).__init__()
128         self.add_param( 'ECAMax' , val=0.0)
129         self.add_param( 'EtaLook' , val=0.0)
130         self.add_output( 'SlantRange' , val=0.0)

131

132     def solve_nonlinear(self , params , unknowns , resids):
133         ECAMax= params [ 'ECAMax' ]
134         EtaLook = params [ 'EtaLook' ]
135         unknowns [ 'SlantRange' ] = 6378.14*math.sin(ECAMax*math.pi
136             /180 )/math.sin( EtaLook *math.pi/180 ) #r e t u r n s km

137     def linearize(self , params , unknowns , resids):
138         J = {}
139         ECAMax= params [ 'ECAMax' ]
140         EtaLook = params [ 'EtaLook' ]
141         J[ 'SlantRange' , 'ECAMax' ] = 6378.14*math.cos(ECAMax*math.
142             pi/180)/math.sin(EtaLook *math.pi/180)
143         J[ 'SlantRange' , 'EtaLook' ] = -6378.14* math.cos(ECAMax*math.
144             .pi/180)/math.sin(EtaLook *math.pi/180)/math.tan(
145             EtaLook *math.pi/180)

```

```

143         return J
144
145     class SwathWidth(Component):
146         def __init__(self):
147             super(SwathWidth, self).__init__()
148             self.add_param('ECAMax', val=0.0)
149             self.add_output('SwathWidth', val=0.0)
150
151         def solve_nonlinear(self, params, unknowns, resids):
152             ECAMax = params['ECAMax']
153             unknowns['SwathWidth'] = 2*ECAMax
154
155         def linearize(self, params, unknowns, resids):
156             J = {}
157             J['SwathWidth', 'ECAMax'] = 2
158             return J
159
160     class IFOV(Component):
161         def __init__(self):
162             super(IFOV, self).__init__()
163             self.add_param('YMax', val=0.0)
164             self.add_param('SlantRange', val=0.0)
165             self.add_output('IFOV', val=0.0)
166
167         def solve_nonlinear(self, params, unknowns, resids):
168             YMax = params['YMax']
169             SlantRange = params['SlantRange']

```

```

170     unknowns[ 'IFOV' ] = YMax/1000/SlantRange*180/math.pi #
171             returns degrees
172
173     def linearize(self, params, unknowns, resids):
174         J = {}
175         YMax = params[ 'YMax' ]
176         SlantRange = params[ 'SlantRange' ]
177         J[ 'IFOV', 'YMax' ] = 180* math.pi/SlantRange
178         J[ 'IFOV', 'SlantRange' ] = -YMax*180/math.pi/(SlantRange
179                         **2)
180
181         return J
182
183     class XMax(Component):
184         def __init__(self):
185             super(XMax, self).__init__()
186             self.add_param( 'YMax', val=0.0)
187             self.add_param( 'IMAX', val=0.0)
188             self.add_output( 'XMax', val=0.0)
189
190         def solve_nonlinear(self, params, unknowns, resids):
191             YMax = params[ 'YMax' ]
192             IMAx = params[ 'IMAX' ]
193             unknowns[ 'XMax' ] = YMax/math.cos(IMAx*math.pi/180) #
194             returns m
195
196         def linearize(self, params, unknowns, resids):
197             J = {}

```

```

194     YMax = params[ 'YMax' ]
195     IAMax = params[ 'IAMax' ]
196     J[ 'XMax', 'YMax' ] = 1/math.cos(IAMax)
197     J[ 'XMax', 'IAMax' ] = YMax*math.tan(IAMax)/math.cos(IAMax)
198     return J
199
200 class CrossTrackPixelResolution(Component):
201     """XinSMADequationstablep288 @nadir"""
202     def __init__(self):
203         super(CrossTrackPixelResolution, self).__init__()
204         self.add_param('IFOV', val=0.0)
205         self.add_param('Altitude', val=0.0)
206         self.add_output('CrossTrackPixelResolution', val=0.0)
207
208     def solve_nonlinear(self, params, unknowns, resids):
209         IFOV = params[ 'IFOV' ]
210         Altitude = params[ 'Altitude' ]
211         unknowns[ 'CrossTrackPixelResolution' ] = IFOV*Altitude*
212             math.pi/180 #returns m
213
214     def linearize(self, params, unknowns, resids):
215         J = {}
216         IFOV = params[ 'IFOV' ]
217         Altitude = params[ 'Altitude' ]
218         J[ 'CrossTrackPixelResolution', 'IFOV' ] = Altitude*math.pi
219             /180
220         J[ 'CrossTrackPixelResolution', 'Altitude' ] = IFOC*math.pi

```

```

/180

219     return J

220

221 class AlongTrackPixelResolution(Component):
222     """Y in SMAD equation table p288 @ nadir"""
223     def __init__(self):
224         super(AlongTrackPixelResolution, self).__init__()
225         self.add_param('IFOV', val=0.0)
226         self.add_param('Altitude', val=0.0)
227         self.add_output('AlongTrackPixelResolution', val=0.0)

228

229     def solve_nonlinear(self, params, unknowns, resids):
230         IFOV = params['IFOV']
231         Altitude = params['Altitude']
232         unknowns['AlongTrackPixelResolution'] = IFOV*Altitude*
233             math.pi/180 #returns m

234     def linearize(self, params, unknowns, resids):
235         J = {}
236         IFOV = params['IFOV']
237         Altitude = params['Altitude']
238         J['AlongTrackPixelResolution', 'IFOV'] = Altitude*math.pi
239             /180
240         J['AlongTrackPixelResolution', 'h'] = IFOC*math.pi/180
241
242 class CrossTrackPixelCount(Component):

```

```

243     """ZC in SMADequatin table p288"""
244
245     def __init__(self):
246         super(CrossTrackPixelCount, self).__init__()
247         self.add_param('EtaLook', val=0.0)
248         self.add_param('IFOV', val=0.0)
249         self.add_output('CrossTrackPixelCount', val=0.0)
250
251     def solve_nonlinear(self, params, unknowns, resids):
252         IFOV = params['IFOV']
253         EtaLook = params['EtaLook']
254         unknowns['CrossTrackPixelCount'] = 2*EtaLook/IFOV #
255         return m
256
257     def linearize(self, params, unknowns, resids):
258         J = {}
259         IFOV = params['IFOV']
260         EtaLook = params['EtaLook']
261         J[('CrossTrackPixelCount', 'IFOV')] = -2*EtaLook/(IFOV**2)
262         J[('CrossTrackPixelCount', 'EtaLook')] = 2/IFOV
263         return J
264
265     class SwathCount(Component):
266         """ZA @ NADIR in SMADEquation table p288"""
267
268         def __init__(self):
269             super(SwathCount, self).__init__()
270             self.add_param('GroundVelocity', val=0.0)
271             self.add_param('AlongTrackPixelResolution', val=0.0)

```

```

269         self.addoutput('SwathCount', val=0.0)

270

271     def solve_nonlinear(self, params, unknowns, resids):
272         GroundVelocity=params['GroundVelocity']
273         AlongTrackPixelResolution= params[''
274                                         AlongTrackPixelResolution'']
275
276         unknowns['SwathCount']= GroundVelocity/
277                                         AlongTrackPixelResolution #Returns swaths at nadir per
278                                         second
279
280
281         def linearize(self, params, unknowns, resids):
282             J = {}
283             GroundVelocity=params['GroundVelocity']
284             AlongTrackPixelResolution= params[''
285                                         AlongTrackPixelResolution'']
286             J[ 'SwathCount', 'GroundVelocity' ] = 1/
287                                         AlongTrackPixelResolution
288             J[ 'SwathCount', 'AlongTrackPixelResolution' ] = -
289                                         GroundVelocity/(AlongTrackPixelResolution**2)
290
291             return J
292
293
294     class PixelRate(Component):
295
296         def __init__(self):
297             super(PixelRate, self).__init__()
298             self.add_param('SwathCount', val=0.0)
299             self.add_param('CrossTrackPixelCount', val=0.0)
300             self.addoutput('PixelRate', val=0.0)

```

```
290
291     def solve_nonlinear(self, params, unknowns, resids):
292         SwathCount = params['SwathCount']
293         CrossTrackPixelCount = params['CrossTrackPixelCount']
294         unknowns['PixelRate'] = SwathCount * CrossTrackPixelCount
295
296     def linearize(self, params, unknowns, resids):
297         J = {}
298         SwathCount = params['SwathCount']
299         AlongTrackPixelCount = params['CrossTrackPixelCount']
300         J['PixelRate', 'SwathCount'] = CrossTrackPixelCount
301         J['PixelRate', 'CrossTrackPixelCount'] = SwathCount
302         return J
303
304 class DataRate(Component):
305     def __init__(self):
306         super(DataRate, self).__init__()
307         self.add_param('PixelRate', val=0.0)
308         self.add_param('BitPerPixel', val=0.0)
309         self.add_output('DataRate', val=0.0)
310
311     def solve_nonlinear(self, params, unknowns, resids):
312         PixelRate = params['PixelRate']
313         BitPerPixel = params['BitPerPixel']
314         unknowns['DataRate'] = PixelRate * BitPerPixel
315
316     def linearize(self, params, unknowns, resids):
```

```

317     J = {}
318     PixelRate = params['PixelRate']
319     BitPerPixel = params['BitPerPixel']
320     J['DataRate', 'BitPerPixel'] = PixelRate
321     J['DataRate', 'PixelRate'] = BitPerPixel
322     return J
323
324 class PixelIntegrationTime(Component):
325     """ This must be higher than the time constant for the
326     detector; used in optimizer """
327     def __init__(self):
328         super(PixelIntegrationTime, self).__init__()
329         self.add_param('AlongTrackPixelResolution', val=0.0)
330         self.add_param('GroundVelocity', val=0.0)
331         self.add_param('CrossTrackPixelCount', val=0.0)
332         self.add_param('PixelInstrumentCount', val=0.0)
333         self.add_output('PixelIntegrationTime', val=0.0)
334
335     def solve_nonlinear(self, params, unknowns, resids):
336         AlongTrackPixelResolution = params['
337             AlongTrackPixelResolution']
338         GroundVelocity = params['GroundVelocity']
339         CrossTrackPixelCount = params['CrossTrackPixelCount']
340         PixelInstrumentCount = params['PixelInstrumentCount']
341         unknowns['PixelIntegrationTime'] =
342             AlongTrackPixelResolution*PixelInstrumentCount/
343             GroundVelocity/CrossTrackPixelCount

```

```

340
341     def linearize(self, params, unknowns, resids):
342         J = {}
343         AlongTrackPixelResolution = params['
344             AlongTrackPixelResolution']
345         GroundVelocity = params['GroundVelocity']
346         CrossTrackPixelCount = params['CrossTrackPixelCount']
347         PixelInstrumentCount = params['PixelInstrumentCount']
348         J['PixelIntegrationTime', 'AlongTrackPixelResolution'] =
349             PixelInstrumentCount/CrossTrackPixelCount/
350                 GroundVelocity
351         J['PixelIntegrationTime', 'GroundVelocity'] = -
352             AlongTrackPixelResolution*PixelInstrumentCount/(
353                 GroundVelocity **2)/CrossTrackPixelCount
354         J['PixelIntegrationTime', 'CrossTrackPixelCount'] = -
355             AlongTrackPixelResolution*PixelInstrumentCount/
356             GroundVelocity/(CrossTrackPixelCount **2)
357         J['PixelIntegrationTime', 'PixelInstrumentCount'] =
358             AlongTrackPixelResolution/CrossTrackPixelCount/
359                 GroundVelocity
360
361         return J
362
363     class FocalLength(Component):
364         def __init__(self):
365             super(FocalLength, self).__init__()
366             self.add_param('Altitude', val=0.0)
367             self.add_param('CrossTrackPixelResolution', val=0.0)

```

```

358         self.add_param('DetWidth', val=0.0)
359         self.add_output('FocalLength', val=0.0)
360
361     def solve_nonlinear(self, params, unknowns, resids):
362         Altitude = params['Altitude']
363         DetWidth = params['DetWidth']
364         CrossTrackPixelResolution = params[''
365                                         CrossTrackPixelResolution']
366
367         unknowns['FocalLength'] = Altitude*DetWidth/
368                                         CrossTrackPixelResolution
369
370     def linearize(self, params, unknowns, residues):
371         J = {}
372         Altitude = params['Altitude']
373         DetWidth = params['DetWidth']
374         CrossTrackPixelResolution = params[''
375                                         CrossTrackPixelResolution']
376         J['FocalLength', 'Altitude'] = DetWidth/
377                                         CrossTrackPixelResolution
378         J['FocalLength', 'DetWidth'] = Altitude/
379                                         CrossTrackPixelResolution
380         J['FocalLength', 'CrossTrackPixelResolution'] = -Altitude
381             *DetWidth/(CrossTrackPixelResolution**2)
382
383         return J
384
385
386     class ApertureDiameter(Component):
387         def __init__(self):

```

```

379     super(ApertureDiameter, self).__init__()
380     self.add_param('DetWidth', val=0.0)
381     self.add_param('FocalLength', val=0.0)
382     self.add_param('QualFactor', val=0.0)
383     self.add_param('OpWavelength', val=0.0)
384     self.add_output('ApertureDiameter', val=0.0)
385
386     def solve_nonlinear(self, params, unknowns, resids):
387         DetWidth = params['DetWidth']
388         OpWavelength = params['OpWavelength']
389         FocalLength = params['FocalLength']
390         QualFactor = params['QualFactor']
391         unknowns['ApertureDiameter'] = 2.44*OpWavelength*
392                         FocalLength*QualFactor/DetWidth
393
394     def linearize(self, params, unknowns, resids):
395         J = {}
396         DetWidth = params['DetWidth']
397         OpWavelength = params['OpWavelength']
398         FocalLength = params['FocalLength']
399         QualFactor = params['QualFactor']
400         J['ApertureDiameter', 'DetWidth'] = -2.44*OpWavelength*
401                         FocalLength*QualFactor/(DetWidth**2)
402         J['ApertureDiameter', 'OpWavelength'] = 2.44*FocalLength*
403                         QualFactor/DetWidth
404         J['ApertureDiameter', 'FocalLength'] = 2.44*OpWavelength*
405                         QualFactor/DetWidth

```

```

402     J[ 'ApertureDiameter' , 'QualFactor' ] = 2.44*OpWavelength*
403         FocalLength/DetWidth
404
405 class FOV(Component):
406     def __init__(self):
407         super(FOV, self).__init__()
408         self.add_param('IFOV', val=0.0)
409         self.add_param('PixelInstrumentCount', val=0.0)
410         self.addoutput('FOV', val=0.0)
411
412     def solve_nonlinear(self, params, unknowns, resids):
413         IFOV = params['IFOV']
414         PixelInstrumentCount = params['PixelInstrumentCount']
415         unknowns['FOV'] = IFOV*PixelInstrumentCount
416
417     def linearize(self, params, unknowns, resids):
418         J = {}
419         J[ 'FOV', 'IFOV' ] = params['PixelInstrumentCount']
420         J[ 'FOV', 'PixelInstrumentCount' ] = params['IFOV']
421         return J
422
423 class PhysParams(Component):
424     """Based of ThematicMapper scaling equations from SMAD ch 9
425     """
426     def __init__(self):
427         super(PhysParams, self).__init__()

```

```

427         self.add_param('ApertureDiameter', val=0.0)
428         self.add_output('ApRat', val=0.0)
429         self.add_output('XDim', val=0.0)
430         self.add_output('YDim', val=0.0)
431         self.add_output('ZDim', val=0.0)
432         self.add_output('PwrEst', val=0.0)
433         self.add_output('MassEst', val=0.0)
434
435     def solve_nonlinear(self, params, unknowns, resids):
436         ApertureDiameter = params['ApertureDiameter']
437         Ratio = ApertureDiameter / 0.015
438         if Ratio <= 0.5:
439             K = 2
440         else:
441             K = 1
442         unknowns['XDim'] = Ratio * 0.045
443         unknowns['YDim'] = Ratio * 0.050
444         unknowns['ZDim'] = Ratio * 0.080
445         unknowns['ApRat'] = K
446         unknowns['PwrEst'] = K * (Ratio ** 3) * 1.26
447         unknowns['MassEst'] = K * (Ratio ** 3) * 0.23
448
449     class PayloadDesign(Group):
450         def __init__(self):
451             super(PayloadDesign, self).__init__()
452             self.add('Altitude', IndepVarComp('Altitude', 450.),
453                     promotes=['Altitude'])

```

```

453     self.add('IAMax', IndepVarComp('IAMax', 70.), promotes=['
454         IAMax'])
455     self.add('YMax', IndepVarComp('YMax', 0.1), promotes=['
456         YMax'])
457     self.add('BitPerPixel', IndepVarComp('BitPerPixel', 8.),
458             promotes=['BitPerPixel'])
459     self.add('PixelInstrumentCount', IndepVarComp('
460             PixelInstrumentCount', 200.), promotes=['
461                 PixelInstrumentCount'])
462     self.add('DetWidth', IndepVarComp('DetWidth', 30.),
463             promotes=['DetWidth'])
464     self.add('QualFactor', IndepVarComp('QualFactor', 1.1),
465             promotes=['QualFactor'])
466     self.add('OpWavelength', IndepVarComp('OpWavelength', 4.2
467             e-06), promotes=['OpWavelength'])

468
469     self.add('d01', OrbitPeriod(), promotes=['Altitude',
470             'OrbPer'])
471     self.add('d02', GroundVelocity(), promotes=['OrbPer',
472             'GroundVelocity'])
473     self.add('d03', AngularRadius(), promotes=['Altitude',
474             'AngRadius'])
475     self.add('d04', LNot(), promotes=['LNot', 'AngRadius'])
476     self.add('d05', DMax(), promotes=['LNot', 'DMax'])
477     self.add('d06', EtaLook(), promotes=['EtaLook', 'IAMax',
478             'AngRadius'])
479     self.add('d07', ECAMax(), promotes=['ECAMax', 'EtaLook'])

```

```

    IAMax'])
468 self.add('d08', SlantRange(), promotes=['ECAMax', 'EtaLook
        ', 'SlantRange'])
469 self.add('d09', SwathWidth(), promotes=['SwathWidth',
        ECAMax'])
470 self.add('d10', IFOV(), promotes=['YMax', 'SlantRange',
        IFOV'])
471 self.add('d11', XMax(), promotes=['YMax', 'IAMax', 'XMax'])
472 self.add('d12', CrossTrackPixelResolution(), promotes=['
        IFOV', 'Altitude', 'CrossTrackPixelResolution'])
473 self.add('d13', AlongTrackPixelResolution(), promotes=['
        IFOV', 'Altitude', 'AlongTrackPixelResolution'])
474 self.add('d14', CrossTrackPixelCount(), promotes=['
        EtaLook', 'IFOV', 'CrossTrackPixelCount'])
475 self.add('d15', SwathCount(), promotes=['GroundVelocity',
        'AlongTrackPixelResolution', 'SwathCount'])
476 self.add('d16', PixelRate(), promotes=['PixelRate',
        'CrossTrackPixelCount', 'SwathCount'])
477 self.add('d17', DataRate(), promotes=['PixelRate',
        'BitPerPixel', 'DataRate'])
478 self.add('d18', PixelIntegrationTime(), promotes=['
        AlongTrackPixelResolution', 'GroundVelocity',
        'CrossTrackPixelCount', 'PixelInstrumentCount',
        'PixelIntegrationTime'])
479 self.add('d19', FocalLength(), promotes=['Altitude',
        'DetWidth', 'CrossTrackPixelResolution', 'FocalLength'])
480 self.add('d20', ApertureDiameter(), promotes='['

```

```

        OpWavelength', 'FocalLength', 'QualFactor', 'DetWidth', '
        ApertureDiameter'])

481     self.add('d21', FOV(), promotes=['IFOV',
                                         PixelInstrumentCount', 'FOV'])

482     self.add('d22', PhysParams(), promotes=['ApertureDiameter',
                                                 'XDim', 'YDim', 'ZDim', 'PwrEst', 'MassEst', 'ApRat'])

483

484     self.add('obj_cmp', ExecComp('obj = ApertureDiameter',
                                    ApertureDiameter=0.0), promotes=['obj',
                                         'ApertureDiameter'])

485

486 top = Problem()

487 root = top.root = PayloadDesign()

488

489 #FIRESAT EXAMPLE

490 #top.driver = FullFactorialDriver(num_levels=2, num_par_doe=1,
                                       load_balance=False)

491 #top.driver.add_desvar('h', lower=700.0, upper=710)

492 #top.driver.add_desvar('IAMax', lower=68., upper=70.)

493 #top.driver.add_desvar('YMax', lower=67, upper=68.0)

494 #top.driver.add_desvar('BitPerPixel', lower=8., upper=16.)

495

496 #top.driver = FullFactorialDriver(num_levels=5, num_par_doe=1,
                                       load_balance=False) #For use in full DOE

497 top.driver = FullFactorialDriver(num_levels=5, num_par_doe=1,
                                       load_balance=False) #for use to find DOE factor generation

498 top.driver.add_desvar('Altitude', lower=300, upper=450)

```

```

499 top.driver.adddesvar('IAMax', lower = 50., upper = 77.)
500 top.driver.adddesvar('YMax', lower = 100, upper = 1000)
501 top.driver.adddesvar('BitPerPixel', lower=8., upper = 16.)
502 top.driver.adddesvar('PixelInstrumentCount', lower=200., upper =
300.)

503 top.driver.adddesvar('DetWidth', lower = 2.0e-6, upper = 4.0e
-6)
504 top.driver.adddesvar('QualFactor', lower = 1.1, upper = 2.0)
505 top.driver.adddesvar('OpWavelength', lower = 3.0e-06, upper =
17.0e-06)

506

507 top.driver.addobjective('obj')

508 #recorder = DumpRecorder('DOEPayload')#For use in full DOE
509 recorder = DumpRecorder('DOEPayload')#increase I to see changes
between DOEdesvar iter

510 recorder.options['record params'] = False
511 recorder.options['record unknowns'] = True
512 recorder.options['record_resids'] = False
513 recorder.options['excludes'] = ['OrbPer', 'GroundVelocity', 'LNot',
'DMax', 'SlantRange', 'AngRadius', 'ECAMax', 'EtaLook', 'SwathWidth',
', 'XMax', 'CrossTrackPixelResolution',
AlongTrackPixelResolution', 'CrossTrackPixelCount', 'SwathCount',
', 'PixelRate', 'FocalLength']

514 top.driver.addrecorder(recorder)

515

516 top.setup()

517 top.run()

```

518

519 top . c l e a n u p ()

D.1.4 Payload DOE Analysis

```

1 %%Data A n a l y s i s f o r D O E s
2 clc; clear all; close all;
3 %% REGEX TEST
4 % PARABOLOID TEST
5 %fxy = regexp(text , ' f x y :$s+(\$d*(.)?(\$d*)?(e)?[+-]?(\$d*))' ,
tokens'); %value of function
6 %fx y = str2double([fx y{:}]');
7 %xparams = regexp(text , ' comp$.x:$s+(\$d*(.)?(\$d*)?(e)?[+-]?(\$d*))' ,
tokens')';
8 %xparams = str2double([xparams{:}]');
9 %yparams = regexp(text , ' comp$.y:$s+(\$d*(.)?(\$d*)?(e)?[+-]?(\$d*))' ,
tokens')';
10 %yparams = str2double([yparams{:}]');
11 %%Payload P a r s i n g RegExpress
12 %VarName = regexp(text , ' VarName:$s+(\$d*(.)?(\$d*)?(e)?[+-]?(\$d*))' ,
tokens') ;
13 %VarName= str2double([VarName{:}]');
14 % D e s i g n Vars : Altitude, BitPerPixel, DetWidth, IAMax ,
OpWavelength ,
15 % PixelInstrumentCount, QualFactor
16 %% READ Payload Data file
17 if exist('PayloadDOEData.mat' , 'file') == 2
18     load('PayloadDOEData.mat') %Saves a few minutes if the data

```

```

has been p a r s e d and s a v e d and a n a l y z e d

19 else
20     fid = fopen('DOEPayload','r');
21     text = textscan(fid, '%s', 'Delimiter', ',', 'endofline', '');
22     text = text{1}{1};
23     fid = fclose(fid);
24     Altitude = regexp(text, 'Altitude:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
25     AlongTrackGroundSampling = regexp(text, 'YMax:$s+(\$d*(.)(\$d*))?(e)?[+-]?(\$d*)', 'tokens');
26     ApertureDiameter = regexp(text, 'ApertureDiameter:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
27     BitPerPixel = regexp(text, 'BitPerPixel:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
28     DataRate = regexp(text, 'DataRate:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
29     DetWidth = regexp(text, 'DetWidth:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
30     FOV = regexp(text, '[^I]+FOV:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens'); %modified to not contain IFOV
31     IAMax = regexp(text, 'IAMax:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
32     IFOV = regexp(text, 'IFOV:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
33     MassEst = regexp(text, 'MassEst:$s+(\$d*(.)(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
34     OpWavelength = regexp(text, 'OpWavelength:$s+(\$d*(.)(\$d*)?(e))'

```

```

?[-]?(\$d*)','tokens');

35 PixelInstrumentCount = regexp(text,'PixelInstrumentCount:\$s
+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))','tokens');

36 PixelIntegrationTime = regexp(text,'PixelIntegrationTime:\$s
+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))','tokens');

37 PwrEst = regexp(text,'PwrEst:\$s+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))'
,'tokens');

38 QualFactor = regexp(text,'QualFactor:\$s+(\$d*(.)?(\$d*)(e)
?[-]?(\$d*))','tokens');

39 XDim = regexp(text,'XDim:\$s+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))','
tokens');

40 YDim = regexp(text,'YDim:\$s+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))','
tokens');

41 ZDim = regexp(text,'ZDim:\$s+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))','
tokens');

42 KRatio = regexp(text,'ApRat:\$s+(\$d*(.)?(\$d*)(e)?[-]?(\$d*))'
,'tokens');

43 clear text fid%Remove file to clear up memory

44 %%Convert to Usable Doubles

45 Altitude = str2double([Altitude{:}]');

46 AlongTrackGroundSampling = str2double([
    AlongTrackGroundSampling{:}]');

47 ApertureDiameter = str2double([ApertureDiameter{:}]');

48 BitPerPixel = str2double([BitPerPixel{:}]');

49 DataRate = str2double([DataRate{:}]');

50 DetWidth = str2double([DetWidth{:}]');

51 FOV= str2double ([FOV{:}]');

```

```

52 IAMax = str2double ([IAMax{:}]');
53 IFOV = str2double ([IFOV{:}]');
54 MassEst = str2double ([MassEst{:}]');
55 OpWavelength = str2double ([OpWavelength{:}]');
56 PixelInstrumentCount = str2double ([PixelInstrumentCount{:}]')
57 ;
58 PixelIntegrationTime = str2double ([PixelIntegrationTime{:}]')
59 ;
60 PwrEst = str2double ([PwrEst{:}]');
61 QualFactor = str2double ([QualFactor{:}]');
62 XDim = str2double ([XDim{:}]');
63 YDim = str2double ([YDim{:}]');
64 ZDim = str2double ([ZDim{:}]');
65 KRatio = str2double ([KRatio{:}]');
66 %% Remove NaN caused by metadata and parameter saving
67 Altitude = Altitude (~isnan(Altitude));
68 [Altitude, AltitudeA, AltitudeB] = CodeFactorLevel(Altitude)
69 ;
70 AlongTrackGroundSampling = AlongTrackGroundSampling (~isnan(
71 AlongTrackGroundSampling));
72 [AlongTrackGroundSampling, AtgsA, AtgsB] = CodeFactorLevel(
73 AlongTrackGroundSampling);
74 ApertureDiameter = ApertureDiameter (~isnan(ApertureDiameter))
75 ;
76 %[ApertureDiameter, ApDiamA, ApDiamB] = CodeFactorLevel(
77 ApertureDiameter);
78 BitPerPixel = BitPerPixel (~isnan(BitPerPixel));

```

```

72 [ BitPerPixel , BitPerPixelA , BitPerPixelB ] = CodeFactorLevel(
73     BitPerPixel);
74 DetWidth = DetWidth(~isnan(DetWidth));
75 [ DetWidth , DetWidthA , DetWidthB ] = CodeFactorLevel(DetWidth);
76 DataRate = DataRate(~isnan(DataRate));
77 %[ DataRate , DataRateA , DataRateB ] = CodeFactorLevel(DataRate)
78 ;
79 FOV = FOV(~isnan(FOV));
80 %[FOV, FovA, FovB] = CodeFactorLevel(FOV);
81 IAMax = IAMax(~isnan(IAMax));
82 [ IAMax , IAMaxA , IAMaxB ] = CodeFactorLevel(IAMax);
83 IFOV = IFOV(~isnan(IFOV));
84 %[ IFOV, IfovA , ifovB ] = CodeFactorLevel(IFOV);
85 MassEst = MassEst(~isnan(MassEst));
86 %[ MassEst , MassEstA , MassEstB ] = CodeFactorLevel(MassEst);
87 OpWavelength = OpWavelength(~isnan(OpWavelength));
88 [OpWavelength, OpwavelengthA, OpWavelengthB] =
89     CodeFactorLevel(OpWavelength);
90 PixelInstrumentCount = PixelInstrumentCount(~isnan(
91     PixelInstrumentCount));
92 [ PixelInstrumentCount , PicA , PicB ] = CodeFactorLevel(
93     PixelInstrumentCount);
94 PixelIntegrationTime= PixelIntegrationTime(~isnan(
95     PixelIntegrationTime));
96 %[ PixelIntegrationTime , PitA , PitB ] = CodeFactorLevel(
97     PixelIntegrationTime);
98 PwrEst = PwrEst(~isnan(PwrEst));

```

```

92 %[ PwrEst , PwrEstA , PwrEstB ] = CodeFactorLevel(PwrEst);
93 QualFactor = QualFactor(~isnan(QualFactor));
94 [ QualFactor , QualFactorA , QualFactorB ] = CodeFactorLevel(Q
95     ualFactor);
96 XDim = XDim(~isnan(XDim));
97 %[ XDim, XdA, XdB] = CodeFactorLevel(XDim);
98 YDim = YDim(~isnan(YDim));
99 %[ YDim, YdA, YdB] = CodeFactorLevel(YDim);
100 ZDim = ZDim(~isnan(ZDim));
101 %[ ZDim, ZdA, ZdB] = CodeFactorLevel(ZDim);
102 KRatio=KRatio(~isnan(KRatio));
103 save('PayloadDOEData.mat')
104 %%ANOVA Te st
105 DesVars = {Altitude , AlongTrackGroundSampling , BitPerPixel ,
106     DetWidth , IAMax , ...
107     OpWavelength , PixelInstrumentCount , QualFactor};
108 DesVarNames = {'Altitude' , 'AlongTrackGroundSampling' , ' '
109     'BitPerPixel' , ...
110     'DetWidth' , 'IAMax' , 'OpWavelength' , 'PixelInstrumentCount'
111     , 'QualFactor'};
112 [DRAanovaP, DRAanovaTbl, DRAanovaStat] = anovan ( DataRate ,
113     DesVars , ' model ' ...
114     , ' interaction ' , ' varnames ' , DesVarNames );
115 [ADAnovaP, ADAnovaTbl, ADAnovaStat] = anovan ( ApertureDiameter
116     , DesVars , ...
117     ' model ' , ' interaction ' , ' varnames ' , DesVarNames );
118 [ PWRAnovaP, PWRAnovaTbl , PWRAnovaStat ] = anovan ( PwrEst ,

```

```

    DesVars,'model',...
113    'interaction','varnames',DesVarNames);
114 [ PITAnovaP,PITAnovaTbl,PITAnovaStat]=anova(
    PixelIntegrationTime,...
115    DesVars,'model','interaction','varnames',DesVarNames);
116 save('PayloadDOEData.mat')
117 end
118 %% Data Test
119 %For a 8^5 factorial analysis these end up around 42MB per
    response
120 %variable
121 Data=[PixelIntegrationTime,Altitude,AlongTrackGroundSampling,
    BitPerPixel,DetWidth,IAMax,OpWavelength,PixelInstrumentCount,
    QualFactor];%Only for Data2
122 fileID=fopen('PayloadPIT.dat','w');
123 fprintf(fileID,'%12s %9s %9s %9s %9s %9s %9s %9s %9s\n','Y',
    'X1','X2','X3','X4','X5','X6','X7','X8');
124 fprintf(fileID,'%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
    %9.8f\n',Data);
125 fclose(fileID);
126 %% DOE Scatter Plots (for comparing to DATAPLOT from NIST)
127 %figure %POWER ESTIMATE
128 %scatter(Altitude,PwrEst)
129 %title('Altitude Response')
130 %
131 %figure
132 %scatter(AlongTrackGroundSampling,PwrEst)

```

```
133 % title('YMax Response')
134 %
135 % figure
136 % scatter(BitPerPixel, PwrEst)
137 % title('BitPerPixelResponse')
138 %
139 % figure
140 % scatter(DetWidth, PwrEst)
141 % title('DetWidth Response')
142 %
143 % figure
144 % scatter(IAMax, PwrEst)
145 % title('IAMax Response')
146 %
147 % figure
148 % scatter(OpWavelength, PwrEst)
149 % title('OpWavelength Response')
150 %
151 % figure
152 % scatter(PixelInstrumentCount, PwrEst)
153 % title('PixelQtyInstResponse')
154 %
155 % figure
156 % scatter(QualFactor, PwrEst)
157 % title('QualFactorResponse')
158 %%Normality Tests
159 %
```

```

160 % Uses the ShapiroWilk to test normality of variables from DOE.
161 % Coded vectors are all[-1 -0.5 0 0.5 1]'
162 %Altitude
163 testvec = [-1 -0.5 0 0.5 1]'; %This is the same as the coded
164 levels for all sets
165 testvec = InvCodeFactorLevel(testvec, AltitudeA, AltitudeB);
166 [H, PVal, WStatistic] = swtest(testvec);
167 if H == 0
168     fprintf('Altitude is a normal distribution with PVal %d and
169             Wstat %d.\n', ...
170             PVal, WStatistic)
171 else
172     fprintf('Altitude is not a normal distribution.\n')
173 end
174 % Along Track Ground Sample
175 testvec = [-1 -0.5 0 0.5 1]';
176 testvec = InvCodeFactorLevel(testvec, AtgsA, AtgsB);
177 [H, PVal, WStatistic] = swtest(testvec);
178 if H == 0
179     fprintf('ATGS is a normal distribution with PVal %d and Wstat
180             %d.\n', ...
181             PVal, WStatistic)
182 else
183     fprintf('ATGS is not a normal distribution.\n')
184 end
185 % Bit Per Pixel
186 testvec = [-1 -0.5 0 0.5 1];

```

```

184 testvec = InvCodeFactorLevel(testvec , BitPerPixelA , BitPerPixelB);
185 [H, PVal, WStatistic] = swtest(testvec);
186 if H == 0
187     fprintf('BPP is a normal distribution with PVal %d and Wstat
188                 %d.\n', ...
189             PVal, WStatistic)
190 else
191     fprintf('BPP is not a normal distribution.\n')
192 end
193 % DetWidth
194 testvec=[ -1 -0.5 0 0 .5 1]';
195 testvec= InvCodeFactorLevel(testvec , DetWidthA , DetWidthB);
196 [ H, PVal, WStatistic]=swtest(testvec);
197 if H == 0
198     fprintf('DetWidth is a normal distribution with PVal %d      and
199                 Wstat %d.\n', ...
200             PVal, WStatistic)
201 else
202     fprintf('DetWidth is not a normal distribution.\n')
203 end
204 % IAMax
205 testvec=[ -1 -0.5 0 0 .5 1]';
206 testvec=InvCodeFactorLevel(testvec , IAMAxA , IAMAxB);
207 [ H, PVal, WStatistic]=swtest(testvec);
208 if H == 0
209     fprintf('IAMax is a normal distribution with PVal %d and
210                 Wstat %d.\n', ...

```

```

208         PVal , WStatistic)
209     else
210         fprintf('IAMax is not a normal distribution.\$n')
211     end
212 %OperationalWavelength
213 testvec=[ -1 -0.5 0 0 .5 1]';
214 testvec= InvCodeFactorLevel(testvec,OpwavelengthA , OpWavelengthB
);
215 [H, PVal , WStatistic ]= swtest(testvec);
216 if H==0
217     fprintf('Op Wavelength is a normal distribution with PVal %
and Wstat %d.\$n',...
218         PVal , WStatistic)
219 else
220     fprintf('Op Wavelength is not a normal distribution.\$n')
221 end
222 %PixelInstrumentCount
223 testvec=[ -1 -0.5 0 0 .5 1]';
224 testvec= InvCodeFactorLevel(testvec,PicA , PicB );
225 [ H, PVal , WStatistic]=swtest(testvec);
226 if H==0
227     fprintf('PixelInst Ct is a normal distribution with PVal %d
and Wstat %d.\$n',...
228         PVal , WStatistic)
229 else
230     fprintf('PixelInst Ct is not a normal distribution.\$n')
231 end

```

```

232 % Quality Factor
233 testvec = [-1 -0.5 0 0.5 1]';
234 testvec = InvCodeFactorLevel(testvec, QualFactorA, QualFactorB);
235 [H, PVal, WStatistic] = swtest(testvec);
236 if H == 0
237     fprintf('QualFactor is a normal distribution with PVal %d and
238             Wstat %d.\n', ...
239             PVal, WStatistic)
240 else
241     fprintf('QualFactor is not a normal distribution.\n')
242 end
243 % DataRate
244 [H, PVal, KSSTAT, cv] = kstest(DataRate, 'alpha', 0.1);
245 if H == 0
246     fprintf('DataRate is a normal distribution with PVal %d and
247             Wstat %d.\n', ...
248             PVal, WStatistic)
249 else
250     fprintf('DataRate is not a normal distribution.\n')
251 %%ResidualPlots vs Design Var (DATARATE)
252 figure
253 scatter(Altitude, DRAnovaStat.resid)
254 title('Altitude vs Data Rate Residuals')
255 xlabel('Altitude')
256 ylabel('DR Residual')

```

```
257 figure
258 scatter(AlongTrackGroundSampling,DRAanovaStat.resid)
259 title('ATGS vs Data Rate Residuals')
260 xlabel('Along Track Ground Sampling')
261 ylabel('DR Residual')
262 figure
263 scatter(BitPerPixel,DRAanovaStat.resid)
264 title('BPP vs Data Rate Residuals')
265 xlabel('Bit Per Pixel')
266 ylabel('DR Residual')
267 figure
268 scatter(DetWidth,DRAanovaStat.resid)
269 title('Detector Width vs Data Rate Residuals')
270 xlabel('Detector Width')
271 ylabel('DR Residual')
272 figure
273 scatter(IAMax,DRAanovaStat.resid)
274 title('Max Incidence Angle vs Data Rate Residuals')
275 xlabel('IA_{max}')
276 ylabel('DR Residual')
277 figure
278 scatter(OpWavelength,DRAanovaStat.resid)
279 title('Operational Wavelength vs Data Rate Residuals')
280 xlabel('OpWavelength')
281 ylabel('DR Residual')
282 figure
283 scatter(PixelInstrumentCount,DRAanovaStat.resid)
```

```
284 title('PIC vs Data Rate Residuals')
285 xlabel('PixelInstrument Count')
286 ylabel('DR Residual')
287 figure
288 scatter(QualFactor, DRAanovaStat.resid)
289 title('QualFactor vs Data Rate Residuals')
290 xlabel('QualFactor')
291 ylabel('DR Residual')
292 %% Residual Plots
293 figure
294 plot([1:1:length(DRAanovaStat.resid)], DRAanovaStat.resid)
295 title('Data Rate Residual')
296 xlabel('Observation #')
297 ylabel('DR Residual')
298 figure
299 LagPlotVec = zeros(length(DRAanovaStat.resid), 1);
300 for i = 2:length(DRAanovaStat.resid)
301     LagPlotVec(i) = DRAanovaStat.resid(i - 1);
302 end
303 scatter(LagPlotVec, DRAanovaStat.resid)
304 title('Data Rate Residual Lag Plot')
305 xlabel('DR Residual(Lag {1})')
306 ylabel('DR Residual')
307 %%
308 figure
309 histogram(DRAanovaStat.resid)
310 title('Histogram of Data Rate Residuals')
```

```

311 xlabel('Residual')
312 ylabel('Count')
313 ResidualVec = sort(DRAnovaStat.resid);
314 n = length(DRAnovaStat.resid);
315 NormOrdStatMed = [1:1:n]';
316 NormOrdStatMed(end) = 0.5^(1/n);
317 NormOrdStatMed(1) = 1 - 0.5^(1/n);
318 for i = 2:n
319     NormOrdStatMed(i) = (i - 0.3175)/(n + 0.365);
320 end
321 figure
322 plot(NormOrdStatMed, ResidualVec)
323 title('Distribution of Residuals')
324 xlabel('CDF')
325 ylabel('Residual')
326 %%
327 figure
328 probplot('exponential', DataRate)
329 figure
330 histfit(DataRate)
331 kstest(boxcox(DataRate))
332 %% Orthogonality Verification
333 NUMFAC = length(DesVars);
334 orthocheck = zeros(NUMFAC);
335 for i = 1:NUMFAC
336     for j = 1:NUMFAC
337         orthocheck(i,j) = sum(Data(i+1,:).*Data(j+1,:));

```

```

338         if i == j
339             orthocheck(i,j) = 0;
340         end
341
342     end
343 end
344 disp(orthocheck)
345 %% DOE Interaction Plot VERIFICATION FOR NIST (PIT)
346 % fPIT=figure;
347 % NUMFAC= length(DesVars);
348 % DesVarNames = {'Altitude','ATGS','Bit/Pixel',...
349 %      'DetWidth','IAMax','OpWave','PixelCount','QualFac'};
350 % for i=1:NUMFAC
351 %     for j=1:NUMFAC
352 %         if i==j
353 %             varname = cellstr(DesVarNames{i});
354 %             subplot(NUMFAC,NUMFAC,(NUMFAC*i-NUMFAC)+j)
355 %             scatter(Data(i+1,:),Data(1,:))
356 %             xlabel(varname)
357 %             axis([-1 1 -inf inf])
358 %         elseif j > i
359 %             KVec = Data(i+1,:).*Data(j+1,:);
360 %             %disp(min(KVec));
361 %             %disp(max(KVec));
362 %             subplot(NUMFAC,NUMFAC,(NUMFAC*i-NUMFAC)+j)
363 %             scatter(KVec,Data(1,:))
364 %             axis([-1 1 -inf inf])

```

```

365 % end
366 % end
367 % end
368 % a = axes;
369 % t1 = title('PixelIntegration Time vs Des Vars');
370 % a.Visible='off';%set(a,'Visible','off');
371 % t1.Visible='on';%set(t1,'Visible','on');
372 %% Verify if statements work in DOE. [It does]
373 % ApTest = ApertureDiameter;
374 % K= zeros(length(ApTest),1);
375 % for i=1:length(ApTest)
376 %     if ApTest(i) < 0.5
377 %         K(i)=2;
378 %     else
379 %         K(i)=1;
380 %     end
381 % end

```

D.1.5 DOE ADCS

```

1 import numpy as np
2 import math
3
4 from openmdao.api import Component, IndepVarComp, Group, Component
      , Problem, ScipyOptimizer, ExecComp, DumpRecorder
5 from openmdao.drivers.fullfactorial_driver import
      FullFactorialDriver
6

```

```

7 ##Estimate environmental effects
8 class GravGradient(Component):
9     """ Evaluates gravity gradient p366"""
10
11     def __init__(self):
12         super(GravGradient, self).__init__()
13         self.add_param('Radius', val=0.0) #Orbit Radius in meters
14             (Re + Alt)
15         self.add_param('Iz', val = 0.0) #Moment of inertia about
16             Z axis
17         self.add_param('Iy', val = 0.0) #Moment of inertia about
18             y axis
19         self.add_param('IncidenceAngle', val = 0.0) #max
20             deviation of z axis from local vertical in radians
21         self.addoutput('Gravity Gradient', val=1.0)
22
23     def solve_nonlinear(self, params, unknowns, resids):
24         mu = 3.986e14 #m^3 / s^2
25         R = params['Radius']
26         Iz = params['Iz']
27         Iy = params['Iy']
28         Theta = params['IncidenceAngle']
29         unknowns['Gravity Gradient'] = 3*mu/2/(R*R*R)*abs(Iz-Iy)*
30             math.sin(2*Theta)
31
32     class SolarRadiation(Component):
33         def __init__(self):

```

```

29     super(SolarRadiation, self).__init__()
30     self.add_param('CenterSolarPressure', val=0.0)
31     self.add_param('CenterGravity', val=0.0)
32     self.add_param('SurfaceArea', val=0.0)
33     self.add_param('ReflectanceFactor', val=0.0)
34     self.add_param('SunIA', val=0.0)
35     self.add_output('SolarRadiation', val=0.0)
36
37     def solve_nonlinear(self, params, unknowns, resids):
38         CPS = params['CenterSolarPressure']
39         CG = params['CenterGravity']
40         SA = params['SurfaceArea']
41         q = params['ReflectanceFactor']
42         i = params['SunIA']
43         Fs = 1367 #W/m^2
44         c = 3e8
45         unknowns['SolarRadiation'] = (Fs/c*SA*(1+q)*math.cos(i))
46                     *(CPS-CG)
47
48     class MagneticField(Component):
49         def __init__(self):
50             super(MagneticField, self).__init__()
51             self.add_param('Radius', val=0.0) #m from center of earth
52             self.add_param('ResidualDipole', val= 0.0) #Am^2
53             self.add_output('MagneticField', val= 0.0) #Nm
54
55         def solve_nonlinear(self, params, unknowns, resids):

```



```

81             [ 140, 140.00, 3.845e-9, 1 6.15 ],
82             [ 150, 150.00, 2.070e-9, 2 2.52 ],
83             [ 180, 180.00, 5.464e-10, 29.74 ],
84             [ 200, 200.00, 2.789e-10, 37.11 ],
85             [ 250, 250.00, 7.248e-11, 45.55 ],
86             [ 300, 300.00, 2.418e-11, 53.63 ],
87             [ 350, 350.00, 9.518e-12, 53.30 ],
88             [ 400, 400.00, 3.725e-12, 58.52 ],
89             [ 450, 450.00, 1.585e-12, 60.83 ],
90             [ 500, 500.00, 6.967e-13, 63.82 ],
91             [ 600, 600.00, 1.454e-13, 71.84 ],
92             [ 700, 700.00, 3.614e-14, 88.67 ],
93             [ 800, 800.00, 1.170e-14, 124.64 ],
94             [ 900, 900.00, 5.245e-15, 181.05 ],
95             [1000, 1000.00, 3.019e-15, 268.00]])
96     for i in range(27):
97         if R >= atmos [ i , 0 ] and R < atmos [ i + 1 , 0 ]:
98             H = atmos [ i , 3 ]
99             rhon = atmos [ i , 2 ]
100            base = atmos [ i , 1 ]
101        elif R >= atmos [ i + 1 , 0 ]:
102            H = atmos [ i + 1 , 3 ]
103            rhon = atmos [ i + 1 , 2 ]
104            base = atmos [ i + 1 , 1 ]
105        unknowns [ 'Density' ] = rhon *math . exp (-(R-base)/H)
106
107    class AerodynamicTorque(Component):

```

```

108     def __init__(self):
109         super(AerodynamicTorque, self).__init__()
110         self.add_param('Radius', val=0.0)
111         self.add_param('Density', val=0.0)
112         self.add_param('CoeffDrag', val=0.0)
113         self.add_param('SurfaceArea', val=0.0)
114         self.add_param('CenterGravity', val=0.0)
115         self.add_param('CenterPressure', val=0.0)
116         self.add_output('AerodynamicTorque', val=0.04)
117
118     def solve_nonlinear(self, params, unknowns, resids):
119         R = params['Radius']
120         rho = params['Density']
121         Cd = params['CoeffDrag']
122         SA = params['SurfaceArea']
123         vel = math.sqrt(3.986e14/R) #Assumes circ orbit for
124             initial
125         F = 0.5 * rho * Cd * SA * vel * vel
126         CenterGravity = params['CenterGravity']
127         CenterPressure = params['CenterPressure']
128         unknowns['AerodynamicTorque'] = F*(CenterPressure-
129             CenterGravity)
130
131     class DisturbanceTorque(Component):
132         def __init__(self):
133             super(DisturbanceTorque, self).__init__()
134             self.add_param('AerodynamicTorque', val=0.0)

```

```

133     self.add_param('GravGradient', val= 0.0)
134     self.add_param('MagneticField', val= 0.0)
135     self.add_param('SolarRadiation', val= 0.0)
136     self.add_output('DisturbanceTorque', val= 0.0)
137
138 def solve_nonlinear(self, params, unknowns, resids):
139     A = params['AerodynamicTorque']
140     G = params['GravGradient']
141     M = params['MagneticField']
142     S = params['SolarRadiation']
143     unknowns['DisturbanceTorque'] = A + G + M + S
144
145 class OrbitPeriod(Component):
146     """ Evaluates the period for a circular orbit in min:1
147         .658669e-04*(6378.14+Altitude)**(3/2) """
148
149     def __init__(self):
150         super(OrbitPeriod, self).__init__()
151         self.add_param('Radius', val=0.0)
152         self.add_output('OrbPer', val=1.0)
153
154     def solve_nonlinear(self, params, unknowns, resids):
155         r = params['Radius']
156         unknowns['OrbPer'] = 1.658669e-04*(r/1000)**1.5
157
158 class SlewTorque(Component):

```

```

159     def __init__(self):
160         super(SlewTorque, self).__init__()
161         self.add_param('Iz', val=0.0) # kg-m2
162         self.add_param('SlewMaxDeg', val=0.0) #deg from slew rate
163         self.add_param('SlewMaxTime', val=0.0) #time (sec) from s
164         self.add_output('SlewTorque', val=0.0)
165
166     def solve_nonlinear(self, params, unknowns, resids):
167         I = params['Iz']
168         Theta = params['SlewMaxDeg']
169         tau = params['SlewMaxTime']
170         unknowns['SlewTorque'] = 4*Theta*math.pi/180*I/tau/tau
171
172     class MomentumStorageRx(Component):
173         def __init__(self):
174             super(MomentumStorageRx, self).__init__()
175             self.add_param('DisturbanceTorque', val=0.0)
176             self.add_param('OrbPer', val=0.0)
177             self.add_output('MomentumStorageRx', val=0.0)
178
179         def solve_nonlinear(self, params, unknowns, resids):
180             TD = params['DisturbanceTorque']
181             P = params['OrbPer']
182             unknowns['MomentumStorageRx'] = TD * P / 4 * 0.707
183
184     class MomentumStorageMW(Component):

```

```

185     def __init__(self):
186         super(MomentumStorageMW, self).__init__()
187         self.add_param('DisturbanceTorque', val=0.0)
188         self.add_param('OrbPer', val=0.0)
189         self.add_param('YawAcc', val=0.0)
190         self.add_output('MomentumStorageMW', val=0.0)
191
192     def solve_nonlinear(self, params, unknowns, resids):
193         TD = params['DisturbanceTorque']
194         P = params['OrbPer']
195         ThetaA = params['YawAcc']
196         unknowns['MomentumStorageMW'] = TD * P / 4 / ThetaA
197
198     class MomentumSpinnerOmega(Component):
199         def __init__(self):
200             super(MomentumSpinnerOmega, self).__init__()
201             self.add_param('MomentumStorageMW', val=0.0)
202             self.add_param('Iz', val=0.0)
203             self.add_output('MomentumSpinnerOmega', val=0.0)
204
205         def solve_nonlinear(self, params, unknowns, resids):
206             h = params['MomentumStorageMW']
207             I = params['Iz']
208             unknowns['MomentumSpinnerOmega'] = h / I
209
210     class MagDipole(Component):
211         def __init__(self):

```

```

212     super(MagDipole, self).__init__()
213     self.add_param('DisturbanceTorque', val=0.0)
214     self.add_param('MagneticField', val=0.0)
215     self.add_output('MagDipole', val = 0.0)
216
217     def solve_nonlinear(self, params, unknowns, resids):
218         T = params['DisturbanceTorque']
219         B = params['MagneticField']
220         unknowns['MagDipole'] = 1.5*T/B
221
222 class RxPhysParams(Component):
223     """based on ADCS regression"""
224     def __init__(self):
225         super(RxPhysParams, self).__init__()
226         self.add_param('MomentumStorageRx', val=0.0)
227         self.add_output('RxX', val=0.0)
228         self.add_output('RxY', val=0.0)
229         self.add_output('RxZ', val=0.0)
230         self.add_output('RxPWR', val=0.0)
231         self.add_output('RxMass', val=0.0)
232
233     def solve_nonlinear(self, params, unknowns, resids):
234         """ One Rx Wheel Dim """
235         H = params['MomentumStorageRx']
236         if H <= 0.015: #Smallest found reaction wheel
237             H = 0.015
238         unknowns['RxX'] = 20.55*math.log(H)+120.4

```

```

239     unknowns[ 'RxY' ] = 20.21*math.log(H)+118.0
240     unknowns[ 'RxZ' ] = 23.61*math.log(H)+100.2
241     unknowns[ 'RxPWR' ] = 0.466*H + .5106
242     unknowns[ 'RxMass' ] = 1.666*H+.1216
243
244 class MGTQRPhysParams(Component):
245     """ One Magnetic Torque Rod Dim"""
246     def __init__(self):
247         super(MGTQRPhysParams, self).__init__()
248         self.add_param('MagDipole', val=0.0)
249         self.add_output('MtxX', val=0.0)
250         self.add_output('MtxY', val=0.0)
251         self.add_output('MtxZ', val=0.0)
252         self.add_output('MtxPWR', val=0.0)
253         self.add_output('MtxMass', val=0.0)
254
255     def solve_nonlinear(self, params, unknowns, resids):
256         """ Total Volume Dimensions not the physical
257             configuration"""
258         D = params['MagDipole']
259         unknowns['MtxX'] = 0.1216 + 10.87*D
260         unknowns['MtxY'] = 118.0 + 3.363*D
261         unknowns['MtxZ'] = 100.2 + 26.67*D
262         unknowns['MtxPWR'] = .0502*D + .399
263         unknowns['MtxMass'] = .001029*D+.3457
264 class STPhysParams(Component):

```

```

265     """based on ADCS regression"""
266
267     def __init__(self):
268         super(STPhysParams, self).__init__()
269         self.add_param('PointKnowledge', val=0.0)
270         self.add_output('STX', val=0.0)
271         self.add_output('STY', val=0.0)
272         self.add_output('STZ', val=0.0)
273         self.add_output('STPWR', val=0.0)
274         self.add_output('STMass', val=0.0)
275
276     def solve_nonlinear(self, params, unknowns, resids):
277         """ Total Volume Dimensions not the physical
278             configuration"""
279         o = params['PointKnowledge']
280         unknowns['STX'] = -6071 * o + 196.3
281         unknowns['STY'] = -6500 * o + 200.3
282         unknowns['STZ'] = -1.536e4 * o + 387
283         unknowns['STPWR'] = -4.592e4 * o * o + 750 * o + 5
284         unknowns['STMass'] = -7296 * o * o + 31.79 * o + 2.735
285
286     class ADCSDesign(Group):
287         def __init__(self):
288             super(ADCSDesign, self).__init__()
289             #Input Variables based on previous systems
290             self.add('Radius', IndepVarComp('Radius', 7078.0),
291                     promotes=['Radius'])
292             self.add('Iz', IndepVarComp('Iz', 100.), promotes=['Iz'])

```

```

290     self.add('Iy', IndepVarComp('Iy', 100.), promotes=['Iy'])
291     self.add('IncidenceAngle', IndepVarComp('IncidenceAngle',
292                                         0.0), promotes=['IncidenceAngle'])
293     self.add('CenterSolarPressure', IndepVarComp(
294                                         'CenterSolarPressure', 0.0), promotes=[
295                                         'CenterSolarPressure'])
296     self.add('CenterGravity', IndepVarComp('CenterGravity',
297                                         0.0), promotes=['CenterGravity'])
298     self.add('ReflectanceFactor', IndepVarComp(
299                                         'ReflectanceFactor', 0.0), promotes=[
300                                         'ReflectanceFactor'])
301     self.add('SunIA', IndepVarComp('SunIA', 0.0), promotes=['SunIA'])
302     self.add('ResidualDipole', IndepVarComp('ResidualDipole',
303                                         0.0), promotes=['ResidualDipole'])
304     self.add('CenterPressure', IndepVarComp('CenterPressure',
305                                         0.0), promotes=['CenterPressure'])
306     self.add('SurfaceArea', IndepVarComp('SurfaceArea', 0.0),
307             promotes=['SurfaceArea'])
308     self.add('CoeffDrag', IndepVarComp('CoeffDrag', 0.0),
309             promotes=['CoeffDrag'])
310     self.add('PointKnowledge', IndepVarComp('PointKnowledge',
311                                         0.0), promotes=['PointKnowledge'])

312     #Design equations
313     self.add('d01', GravGradient(), promotes=['Radius', 'Iz', 'Iy',
314                                              'IncidenceAngle', 'GravityGradient'])
315     self.add('d02', SolarRadiation(), promotes=['

```

```

    CenterSolarPressure', 'CenterGravity',
    ReflectanceFactor', 'SunIA', 'SolarRadiation'])
304 self.add('d03', MagneticField(), promotes=['Radius', 'R
esidualDipole', 'MagneticField'])

305 self.add('d04', Density(), promotes=['Radius', 'Density'])

306 self.add('d05', AerodynamicTorque(), promotes=['Radius', 'R
esidualDipole', 'AerodynamicTorque'])

307 self.add('d06', DisturbanceTorque(), promotes=[

308     'DisturbanceTorque', 'AerodynamicTorque', 'GravGradient',
     'SolarRadiation', 'MagneticField'])

309 self.add('d07', OrbitPeriod(), promotes=['Radius', 'OrbPer
'])

310 self.add('d08', MomentumStorageRx(), promotes=[['OrbPer', 'R
esidualDipole', 'MagneticField', 'MagDipole']])

311 self.add('d10', RxPhysParams(), promotes=['RxX', 'RxY',
     'RxZ', 'RxPWR', 'RxMass', 'MomentumStorageRx'])

312 self.add('d11', MGTQRPhysParams(), promotes=['MtxX', 'MtxY',
     'MtxZ', 'MtxPWR', 'MtxMass', 'MagDipole'])

313 self.add('d12', STPhysParams(), promotes=['STX', 'STY',
     'STZ', 'STPWR', 'STMass', 'PointKnowledge'])

314 self.add('obj_cmp', ExecComp('obj = DisturbanceTorque',
     DisturbanceTorque=0.0), promotes=['obj', 'DisturbanceTorque'])

```

```

315
316 top = Problem()
317 root = top.root = ADCSDesign()
318
319 #FIRESAT EXAMPLE
320 top.driver = FullFactorialDriver(num_levels=2, num_par_doe=1, l
oad_balance=False)
321 top.driver.add_desvar('Radius', lower=6500.e3, upper=7200.e3) #
meters
322 top.driver.add_desvar('Iz', lower=1.7e-3, upper = 1.8e-3) #kg ^
m2, see http://www.leodium.ulg.ac.be/cmsms/uploads/08-09
_Pierlot.pdf
323 top.driver.add_desvar('Iy', lower = 1.9e-3, upper = 2.1e-3) #kg m
^2 see http://www.leodium.ulg.ac.be/cmsms/uploads/08-09
_Pierlot.pdf
324 top.driver.add_desvar('IncidenceAngle', lower=0., upper = 0.) #
rad about z axis
325 top.driver.add_desvar('CenterSolarPressure', lower=.03, upper =
.03) #meter
326 top.driver.add_desvar('CenterGravity', lower = 0., upper = 0.) #
meter
327 top.driver.add_desvar('ReflectanceFactor', lower=0.5, upper =
0.8) #0-1 typ o .6
328 top.driver.add_desvar('SunIA', lower = 0., upper = 10.) #rad
329 top.driver.add_desvar('ResidualDipole', lower = 1., upper = 1.2) #
Am^2
330 top.driver.add_desvar('CenterPressure', lower = 0.02, upper =

```

```

0.02) #from center see
331 top.driver.adddesvar('SurfaceArea', lower = .0294, upper =
    .0294) #m^2 see https://digitalcommons.usu.edu/cgi/viewcontent
    .cgi?article=1074&context=sma11sat
332 top.driver.add desvar('CoeffDrag', lower = 2.0, upper = 2.2) #
    dimensionless
333 top.driver.adddesvar('PointKnowledge', lower = .007, upper =
    .02) #degrees
334
335 top.driver.addobjective('obj')
336 recorder = DumpRecorder('DOE ACDS')#
337 recorder.options['recordparams'] = False
338 recorder.options['recordunknowns'] = True
339 recorder.options['recordresids'] = False
340 #recorder.options['excludes']=['OrbPer','Lnot']
341 top.driver.addrecorder(recorder)
342
343 top.setup()
344 top.run()
345
346 top.cleanup()

```

D.1.6 ADCS DOE Analysis

```

1 %%Data Analysis for DOEs
2 clc; clear all; close all;
3 %% READ Payload Data file
4 if exist('ADCSDOEData.mat', 'file') == 2

```

```

5      load('ADCSDOEData.mat') %Saves a few minutes if the data has
6      been parsed and saved and analyzed
7
8      fid = fopen('DOEACDS','r');
9      text = textscan(fid, '%s', 'Delimiter', ',', 'endofline', '');
10     text = text{1}{1};
11     fid = fclose(fid);
12
13     AerodynamicTorque = regexp(text, 'AerodynamicTorque:\$s+(\$d*(.)?
14     ?(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
15
16     CenterGravity = regexp(text, 'CenterGravity:\$s+(\$d*(.)?(\$d*)?(e)?
17     ?[+-]?(\$d*))', 'tokens');
18
19     CenterPressure = regexp(text, 'CenterPressure:\$s+(\$d*(.)?(\$d*)?
20     ?(e)?[+-]?(\$d*))', 'tokens');
21
22     CenterSolarPressure = regexp(text, 'CenterSolarPressure:\$s+(\$d*
23     *(.)?(\$d*)?(e)?[+-]?(\$d*))', 'tokens');
24
25     CoeffDrag = regexp(text, 'CoeffDrag:\$s+(\$d*(.)?(\$d*)?(e)?
26     ?[+-]?(\$d*))', 'tokens');
27
28     Density = regexp(text, 'Density:\$s+(\$d*(.)?(\$d*)?(e)?[+-]?(\$d
29     *))', 'tokens');
30
31     DisturbanceTorque = regexp(text, 'DisturbanceTorque:\$s+(\$d*(.)?
32     ?(\$d*)(e)?[+-]?(\$d*))', 'tokens'); %modified to nt contain
33
34     IFOV
35
36     GravityGradient = regexp(text, 'GravityGradient:\$s+(\$d*(.)?(\$d
37     *)?(e)?[+-]?(\$d*))', 'tokens');
38
39     IncidenceAngle = regexp(text, 'IncidenceAngle:\$s+(\$d*(.)?(\$d*)?
40     ?(e)?[+-]?(\$d*))', 'tokens');
41
42     Iy = regexp(text, 'Iy:\$s+(\$d*(.)?(\$d*)?(e)?[+-]?(\$d*))', '

```

```

tokens');

21 Iz = regexp(text, 'Iz:$s+($d*(.)?($d*)?(e)?[+-]?($d*))','
tokens');

22 MagDipole = regexp(text, 'MagDipole:$s+($d*(.)?($d*)?(e)
?[+-]?($d*))','tokens');

23 MagneticField = regexp(text, 'MagneticField:$s+($d*(.)?($d*)?(e)?[+-]?($d*))','tokens');

24 MomentumStorageRx = regexp(text, 'MomentumStorageRx:$s+($d*(.)
?($d*)?(e)?[+-]?($d*))','tokens');

25 MtxMass = regexp(text, 'MtxMass:$s+($d*(.)?($d*)?(e)?[+-]?($d
*))','tokens');

26 MtxPWR= regexp(text, 'MtxPWR:$s+($d*(.)?($d*)?(e)?[+-]?($d*))'
,'tokens');

27 MtxX= regexp(text, 'MtxX:$s+($d*(.)?($d*)?(e)?[+-]?($d*))','
tokens');

28 MtxY= regexp(text, 'MtxY:$s+($d*(.)?($d*)?(e)?[+-]?($d*))','
tokens');

29 MtxZ = regexp(text, 'MtxZ:$s+($d*(.)?($d*)?(e)?[+-]?($d*))','
tokens');

30 OrbPer = regexp(text, 'OrbPer:$s+($d*(.)?($d*)?(e)?[+-]?($d*))'
,'tokens');

31 PointKnowledge = regexp(text, 'PointKnowledge:$s+($d*(.)?($d*)
?(e)?[+-]?($d*))','tokens');

32 Radius = regexp(text, 'Radius:$s+($d*(.)?($d*)?(e)?[+-]?($d*))'
,'tokens');

33 ReflectanceFactor = regexp(text, 'ReflectanceFactor:$s+($d*(.)
?($d*)?(e)?[+-]?($d*))','tokens');

```

```

34 ResidualDipole = regexp(text,'ResidualDipole:$s+(\$d*(.))?(\$d*)
35 ?(e)?[+-]?(\$d*))','tokens');
36 RxMass = regexp(text,'RxMass:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))'
37 ','tokens');
38 RxPWR= regexp(text,'RxPWR:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
39 'tokens');
40 RxX= regexp(text,'RxX:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
41 'tokens');
42 RxY= regexp(text,'RxY:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
43 'tokens');
44 RxZ= regexp(text,'RxZ:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
45 'tokens');
46 STMass = regexp(text,'STMass:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))'
47 ','tokens');
48 STPWR= regexp(text,'STPWR:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
49 'tokens');
50 STX= regexp(text,'STX:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
51 'tokens');
52 STY= regexp(text,'STY:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
53 'tokens');
54 STZ= regexp(text,'STZ:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
55 'tokens');
56 SolarRadiation = regexp(text,'SolarRadiation:$s+(\$d*(.))?(\$d*)
57 ?(e)?[+-]?(\$d*))','tokens');
58 SunIA = regexp(text,'SunIA:$s+(\$d*(.))?(\$d*)?(e)?[+-]?(\$d*))',
59 'tokens');
60 SurfaceArea = regexp(text,'SurfaceArea:$s+(\$d*(.))?(\$d*)?(e)

```

```

48 ?[+ -]?($d *)', 'tokens');
49 clear text fid%Remove file to clear up memory
50 %%Convert to Usable Doubles
51 AerodynamicTorque = str2double ([AerodynamicTorque{:}]');
52 CenterGravity = str2double ([CenterGravity{:}]');
53 CenterPressure = str2double ([CenterPressure{:}]');
54 CenterSolarPressure = str2double ([CenterSolarPressure{:}]');
55 CoeffDrag = str2double ([CoeffDrag{:}]');
56 Density = str2double ([Density{:}]');
57 DisturbanceTorque = str2double ([DisturbanceTorque{:}]');
58 GravityGradient = str2double ([GravityGradient{:}]');
59 IncidenceAngle = str2double ([IncidenceAngle{:}]');
60 Iy = str2double ([Iy{:}]');
61 Iz = str2double ([Iz{:}]');
62 MagDipole = str2double ([MagDipole{:}]');
63 MagneticField = str2double ([MagneticField{:}]');
64 MomentumStorageRx = str2double ([MomentumStorageRx{:}]');
65 MtxMass = str2double ([MtxMass{:}]');
66 MtxPWR= str2double ([MtxPWR{:}]');
67 MtxX = str2double ([MtxX{:}]');
68 MtxY = str2double ([MtxY{:}]');
69 MtxZ = str2double ([MtxZ{:}]');
70 OrbPer = str2double ([OrbPer{:}]');
71 PointKnowledge = str2double ([PointKnowledge{:}]');
72 Radius = str2double ([Radius{:}]');
73 ReflectanceFactor = str2double ([ReflectanceFactor{:}]');
74 ResidualDipole = str2double ([ResidualDipole{:}]');

```

```

74 RxMass = str2double ([ RxMass{:}] ') ;
75 RxPWR= str2double ([RxPWR{:}] ') ;
76 RxX = str2double ([RxX{:}] ') ;
77 RxY = str2double ([RxY{:}] ') ;
78 RxZ = str2double ([RxZ{:}] ') ;
79 STMass = str2double ([ STMass{:}] ') ;
80 STPWR= str2double ([STPWR{:}] ') ;
81 STX = str2double ([STX{:}] ') ;
82 STY = str2double ([STY{:}] ') ;
83 STZ = str2double ([STZ{:}] ') ;
84 SolarRadiation = str2double ([ SolarRadiation{:}] ') ;
85 SunIA = str2double ([ SunIA{:}] ') ;
86 SurfaceArea = str2double ([ SurfaceArea{:}] ') ;
87 %%Remove NaN caused by metadata and parameter saving
88 AerodynamicTorque=AerodynamicTorque(~isnan(
89     AerodynamicTorque));
90 CenterGravity = CenterGravity (~isnan(CenterGravity));
91 CenterPressure = CenterPressure (~isnan(CenterPressure));
92 CenterSolarPressure = CenterSolarPressure (~isnan(
93     CenterSolarPressure));
94 Density = Density (~isnan(Density));
95 CoeffDrag = CoeffDrag (~isnan(CoeffDrag));
96 DisturbanceTorque = DisturbanceTorque (~isnan(
97     DisturbanceTorque));
98 GravityGradient = GravityGradient (~isnan(GravityGradient));
99 IncidenceAngle = IncidenceAngle (~isnan(IncidenceAngle));
100 Iy = Iy (~isnan(Iy));

```

```

98    Iz = Iz( ~isnan(Iz));
99    MagDipole = MagDipole( ~isnan(MagDipole));
100   MagneticField = MagneticField(~isnan(MagneticField));
101   MomentumStorageRx = MomentumStorageRx( ~isnan(
102     MomentumStorageRx));
103   MtxMass = MtxMass( ~isnan(MtxMass));
104   MtxPWR = MtxPWR(~isnan(MtxPWR));
105   MtxX = MtxX(~isnan(MtxX));
106   MtxY = MtxY(~isnan(MtxY));
107   MtxZ = MtxZ( ~isnan(MtxZ));
108   OrbPer = OrbPer( ~isnan(OrbPer));
109   PointKnowledge = PointKnowledge(~isnan(PointKnowledge));
110   Radius = Radius( ~isnan(Radius));
111   ReflectanceFactor = ReflectanceFactor(~isnan(
112     ReflectanceFactor));
113   ResidualDipole = ResidualDipole(~isnan(ResidualDipole));
114   RxMass = RxMass( ~isnan(RxMass));
115   RxPWR = RxPWR(~isnan(RxPWR));
116   RxX = RxX(~isnan(RxX));
117   RxY = RxY(~isnan(RxY));
118   RxZ = RxZ(~isnan(RxZ));
119   STMass = STMass( ~isnan(STMass));
120   STPWR = STPWR(~isnan(STPWR));
121   STX = STX(~isnan(STX));
122   STY = STY(~isnan(STY));
123   STZ = STZ(~isnan(STZ));
124   SolarRadiation = SolarRadiation(~isnan(SolarRadiation));

```

```

123     SunIA = SunIA (~isnan(SunIA));
124     SurfaceArea = SurfaceArea(~isnan(SurfaceArea));
125     save('ADCSDOEData.mat')
126 end
127 %% Design Variable Orthogonalization
128 %
129 % Design variables include radius, Iy, Iz, Reflectance      Factor,
130 % SunIA, Cd,
131 %
132 %
133 [Radius, RadiusA, RadiusB] = CodeFactorLevel(Radius);
134 [Iy, IyA, IyB] = CodeFactorLevel(Iy);
135 [Iz, IzA, IzB] = CodeFactorLevel(Iz);
136 [ReflectanceFactor, RFA, RFB] = CodeFactorLevel(ReflectanceFactor
    );
137 [SunIA, SIAA, SIAB] = CodeFactorLevel(SunIA);
138 [CoeffDrag, CDA, CDB] = CodeFactorLevel(CoeffDrag);
139 [PointKnowledge, PKA, PKB] = CodeFactorLevel(PointKnowledge);
140 [ResidualDipole, RDA, RDB] = CodeFactorLevel(ResidualDipole);
141 %% Response Variable Tests of Normality
142 [H, PVal, WStatistic] = kstest(RxX);
143 if H == 0
144     fprintf('RxX / RxY is a normal distribution with PVal %d and
145             Wstat %d. \n', ...
146             PVal, WStatistic)
147 else

```

```

147     fprintf( 'RxX/RxY is not a normal distribution.\$n')
148 end
149 [H, PVal, WStatistic] = kstest(RxZ);
150 if H==0
151     fprintf( 'RxZ is a normal distribution with PVal %d and Wstat
152         %d.\$n', ...
153             PVal, WStatistic)
154 else
155     fprintf( 'RxZ is not a normal distribution.\$n')
156 end
157 [H, PVal, WStatistic] = kstest(RxMass);
158 if H==0
159     fprintf( 'RxMass is a normal distribution with PVal %d and
160         Wstat %d.\$n', ...
161             PVal, WStatistic)
162 else
163     fprintf( 'RxMass is not a normal distribution.\$n')
164 end
165 [H, PVal, WStatistic] = kstest(RxPWR);
166 if H==0
167     fprintf( 'RxPWR is a normal distribution with PVal %d and
168         Wstat %d.\$n', ...
169             PVal, WStatistic)
170 else
171     fprintf( 'RxPWR is not a normal distribution.\$n')
172 end
173 [H, PVal, WStatistic] = kstest(MtxX);

```

```

171 if H==0
172     fprintf('Mtx is a normal distribution with PVal %d and Wstat
173             %d.%n',...
174             PVal, WStatistic)
175 else
176     fprintf('Mtx is not a normal distribution.%n')
177 end
178 [H, PVal, WStatistic] = kstest(MtxZ);
179 if H==0
180     fprintf('MtxZ is a normal distribution with PVal %d and Wstat
181             %d.%n',...
182             PVal, WStatistic)
183 else
184     fprintf('MtxZ is not a normal distribution.%n')
185 end
186 [H, PVal, WStatistic] = kstest(MtxMass);
187 if H==0
188     fprintf('MtxMass is a normal distribution with PVal %d and
189             Wstat %d.%n',...
190             PVal, WStatistic)
191 else
192     fprintf('MtxMass is not a normal distribution.%n')
193 end
194 [H, PVal, WStatistic] = kstest(MtxPWR);
195 if H==0
196     fprintf('MtxPWR is a normal distribution with PVal %d and
197             Wstat %d.%n',...

```

```

194 PVal, WStatistic)
195 else
196 fprintf('MtxPWR is not a normal distribution.\n')
197 end
198 [ H, PVal, WStatistic] = kstest(STX);
199 if H == 0
200 fprintf('STX is a normal distribution with PVal %d and Wstat
201 %d.\n', ...
202 PVal, WStatistic)
203 else
204 fprintf('STX is not a normal distribution.\n')
205 end
206 [ H, PVal, WStatistic] = kstest(STZ);
207 if H == 0
208 fprintf('STZ is a normal distribution with PVal %d and Wstat
209 %d.\n', ...
210 PVal, WStatistic)
211 else
212 fprintf('STZ is not a normal distribution.\n')
213 end
214 [H, PVal, WStatistic] = kstest(STMass);
215 if H == 0
216 fprintf('STMass is a normal distribution with PVal %d and
217 Wstat %d.\n', ...
218 PVal, WStatistic)
219 else
220 fprintf('STMass is not a normal distribution.\n')

```

```

218 end

219 [H, PVal, WStatistic] = kstest(STPWR);

220 if H == 0
221     fprintf('STPWR is a normal distribution with PVal %d and
222             Wstat %d.\n', ...
223             PVal, WStatistic)

224 else
225     fprintf('STPWR is not a normal distribution.\n')
226 end

227 %% ANOVA Test
228 %
229 % Can not be run due to non-normal response distribution
230 %

231 %% Data Files for NIST DATAPlot
232 %
233 % For a 8^5 factorial analysis these end up around 42MB per
234 % response
235 %

236 DesVarData = [Radius, Iy, Iz, ReflectanceFactor, SunIA, CoeffDrag
237 , PointKnowledge, ResidualDipole];
238
239 %Reaction Wheel
240 Data = [3 * RxX.* RxY.* RxZ/1000/1000/1000, DesVarData]';
241 fileID = fopen('ADCSRxVol.dat','w');
242 fprintf(fileID, '%12s %9s %9s %9s %9s %9s %9s %9s %9s\n', 'Y',
243 'X1', 'X2', 'X3', 'X4', 'X5', 'X6', 'X7', 'X8');

```

```

241 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
               %9.8f \n' , Data );
242 fclose(fileID );
243
244 Data = [ 3 * RxMass , DesVarData ]' ;
245 fileID = fopen('ADCSRxMass.dat' , 'w');
246 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s \n' , 'Y' , 'X1
               ' , 'X2' , 'X3' , 'X4' , 'X5' , 'X6' , 'X7' , 'X8' );
247 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
               %9.8f \n' , Data );
248 fclose(fileID );
249 Data = [ 3 * RxPWR , DesVarData ]' ;
250 fileID = fopen('ADCSRxPower.dat' , 'w');
251 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s \n' , 'Y' , 'X1
               ' , 'X2' , 'X3' , 'X4' , 'X5' , 'X6' , 'X7' , 'X8' );
252 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
               %9.8f \n' , Data );
253 fclose(fileID );
254 %Star Tracker
255 Data = [ STX.*STY.*STZ/1000/1000/1000 , DesVarData ]' ;
256 fileID = fopen('ADCSSTVol.dat' , 'w');
257 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s \n' , 'Y' , 'X1
               ' , 'X2' , 'X3' , 'X4' , 'X5' , 'X6' , 'X7' , 'X8' );
258 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
               %9.8f \n' , Data );
259 fclose(fileID );
260

```

```

261 Data = [ STMass , DesVarData ]' ;
262 fileID = fopen( 'ADCSSTMass.dat' , 'w' );
263 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s\n' , 'Y' , 'X1
   , 'X2' , 'X3' , 'X4' , 'X5' , 'X6' , 'X7' , 'X8' );
264 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
   %9.8f\n' , Data );
265 fclose(fileID);
266
267 Data = [STPWR, DesVarData ]' ;
268 fileID = fopen( 'ADCSSTPower.dat' , 'w' );
269 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s\n' , 'Y' , 'X1
   , 'X2' , 'X3' , 'X4' , 'X5' , 'X6' , 'X7' , 'X8' );
270 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
   %9.8f\n' , Data );
271 fclose(fileID);
272 %MagneticTorqueRod
273 Data = [ 2 * MtxX . * MtxY . * MtxZ /1 0 0 0 /1 0 0 0 /1 0 0 0 , DesVarData ]' ;
274 fileID = fopen( 'ADCSMagTorqueVol.dat' , 'w' );
275 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s\n' , 'Y' , 'X1
   , 'X2' , 'X3' , 'X4' , 'X5' , 'X6' , 'X7' , 'X8' );
276 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
   %9.8f\n' , Data );
277 fclose(fileID);
278
279 Data = [ 2 * MtxMass , DesVarData ]' ;
280 fileID = fopen( 'ADCSMagTorqueMass.dat' , 'w' );
281 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s %9s\n' , 'Y' , 'X1

```

```

      ', 'X2', 'X3', 'X4', 'X5', 'X6', 'X7', 'X8');

282 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
                  %9.8f \r\n' , Data);

283 fclose(fileID);

284

285 Data = [ 2 *MtxPWR, DesVarData ]';

286 fileID = fopen('ADCSMagTorquePower.dat' , 'w');

287 fprintf(fileID , '%12s %9s %9s %9s %9s %9s %9s %9s\r\n' , 'Y',
                  'X1
      ', 'X2', 'X3', 'X4', 'X5', 'X6', 'X7', 'X8');

288 fprintf(fileID , '%12.12f %9.8f %9.8f %9.8f %9.8f %9.8f %9.8f
                  %9.8f \r\n' , Data);

289 fclose(fileID);

290

291 %% Orthogonality Verification

292 DesVars = { Radius , Iy , Iz , ReflectanceFactor , SunIA , CoeffDrag ,
                  PointKnowledge , ResidualDipole };

293 NUMFAC= length(DesVars);

294 orthocheck= zeros(NUMFAC);

295 for i = 1 :NUMFAC

296     for j = 1 :NUMFAC

297         orthocheck(i,j)= sum( Data(i+1,:) .* Data(j+1,:));

298         if i == j
299             orthocheck(i,j) = 0;
300
301         end
302
303 end

```

```

304 disp(orthochek)
305 %%DOE Interaction Plot VERIFICATION FOR NIST
306 %%Reaction Wheel
307 Data(1,:) = 3*RxX.*RxY.*RxZ;
308 fRxVol=figure;
309 NUMFAC= length(DesVars);
310 DesVarNames = { 'Radius', 'Iy', 'Iz', 'ReflectanceFactor', 'SunIA', ...
311     'CoeffDrag',...
312     'PointKnowledge', 'ResidualDipole'};
313 for i=1:NUMFAC
314     for j=1:NUMFAC
315         if i==j
316             subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
317             scatter(Data(i+1,:), Data(1,:))
318             xlabel(varname)
319             axis([-1 1 -inf inf])
320         elseif j > i
321             KVec=Data(i+1,:).*Data(j+1,:);
322             %disp(min(KVec));
323             %disp(max(KVec));
324             subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
325             scatter(KVec, Data(1,:))
326             axis([-1 1 -inf inf])
327         end
328     end
329 end

```

```

330 a = axes;
331 t1 = title(' RxWheel Volume (mm^3) v s Des Vars ');
332 a.Visible = 'off'; % set(a,'Visible','off');
333 t1.Visible = 'on'; % set(t1,'Visible','on');
334 Data(1,:) = 3*RxMass;
335 fRxMass = figure;
336
337 for i = 1:NUMFAC
338     for j = 1:NUMFAC
339         if i == j
340             varname = cellstr(DesVarNames{i});
341             subplot(NUMFAC, NUMFAC, (NUMFAC*i - NUMFAC)+j)
342             scatter(Data(i+1,:), Data(1,:))
343             xlabel(varname)
344             axis([-1 1 -inf inf])
345         elseif j > i
346             KVec = Data(i+1,:).*Data(j+1,:);
347             %disp(min(KVec));
348             %disp(max(KVec));
349             subplot(NUMFAC, NUMFAC, (NUMFAC*i - NUMFAC)+j)
350             scatter(KVec, Data(1,:))
351             axis([-1 1 -inf inf])
352         end
353     end
354 end
355 a = axes;
356 t1 = title(' RxWheel Mass ( kg ) v s Des Vars ');

```

```

357 a.Visible = 'off'; % set(a,'Visible','off');
358 t1.Visible = 'on'; % set(t1,'Visible','on');
359 Data(1,:) = 3*RxPWR;
360 fRxPower = figure;
361 for i = 1:NUMFAC
362     for j = 1:NUMFAC
363         if i == j
364             varname = cellstr(DesVarNames{i});
365             subplot(NUMFAC, NUMFAC, (NUMFAC*i - NUMFAC)+j)
366             scatter(Data(i+1,:), Data(1,:))
367             xlabel(varname)
368             axis([-1 1 -inf inf])
369         elseif j > i
370             KVec = Data(i+1,:).*Data(j+1,:);
371             %disp(min(KVec));
372             %disp(max(KVec));
373             subplot(NUMFAC, NUMFAC, (NUMFAC*i - NUMFAC)+j)
374             scatter(KVec, Data(1,:))
375             axis([-1 1 -inf inf])
376         end
377     end
378 end
379 a = axes;
380 t1 = title(' RxWheel Power (W) v s Des Vars ');
381 a.Visible='off';%set(a,'Visible','off');
382 t1.Visible = 'on';% set(t1,'Visible','on');
383 %% Magnetoquers

```

```

384 Data ( 1 , : ) = 2 * MtxX . * MtxY . * MtxZ ;
385 fRxVol = figure ;
386 for i = 1 : NUMFAC
387     for j = 1 : NUMFAC
388         if i == j
389             varname = cellstr (DesVarNames { i }) ;
390             subplot (NUMFAC, NUMFAC, (NUMFAC * i - NUMFAC) + j)
391             scatter (Data ( i + 1 , : ), Data ( 1 , : ))
392             xlabel (varname)
393             axis ( [ -1 1 -inf inf ] )
394         elseif j > i
395             KVec = Data ( i + 1 , : ) . * Data ( j + 1 , : );
396             %disp ( min (KVec)) ;
397             %disp ( max (KVec)) ;
398             subplot (NUMFAC, NUMFAC, (NUMFAC * i - NUMFAC) + j)
399             scatter (KVec, Data ( 1 , : ))
400             axis ( [ -1 1 -inf inf ] )
401         end
402     end
403 end
404 a = axes ;
405 t1 = title (' Torque Rod Volume (mm^3 ) v s Des Vars ') ;
406 a . Visible = ' off ' ; % set ( a , ' Visible ' , ' off ' );
407 t1 . Visible = ' on ' ; % set ( t1 , ' Visible ' , ' on ' );
408 Data ( 1 , : ) = 2 * MtxMass ;
409 fRxMass = figure ;
410 for i = 1 : NUMFAC

```

```

411   f o r j = 1 :NUMFAC
412     i f i == j
413       varname = cellstr(DesVarNames{i});
414       subplot(NUMFAC, NUMFAC, (NUMFAC*i - NUMFAC)+j)
415       scatter(Data(i+1,:), Data(1,:))
416       xlabel(varname)
417       axis([-1 1 -inf inf])
418     e l s e i f j > i
419       KVec = Data(i+1,:).*Data(j+1,:);
420       %disp(min(KVec));
421       %disp(max(KVec));
422       subplot(NUMFAC, NUMFAC, (NUMFAC*i - NUMFAC)+j)
423       scatter(KVec, Data(1,:))
424       axis([-1 1 -inf inf])
425   e n d
426 e n d
427 e n d
428 a = a x e s ;
429 t1 = title('Torque Rod Mass (kg) v s Des Vars');
430 a.Visible = 'off'; % set(a,'Visible','off');
431 t1.Visible = 'on'; % set(t1,'Visible','on');
432 Data(1,:) = 3*MtxPWR;
433 fRxPower = figure;
434 f o r i = 1 :NUMFAC
435   f o r j = 1 :NUMFAC
436     i f i == j
437       varname = cellstr(DesVarNames{i});

```

```

438     subplot(NUMFAC, NUMFAC, (NUMFAC* i -NUMFAC)+j)
439         scatter(Data( i + 1 , : ), Data( 1 , : ))
440         xlabel(varname)
441         axis([-1 1 -inf inf])
442     elseif j > i
443         KVec = Data( i + 1 , : ) .* Data( j + 1 , : );
444         %d i s p ( min( KVec ) );
445         %d i s p ( max( KVec ) );
446     subplot(NUMFAC, NUMFAC, (NUMFAC* i -NUMFAC)+j)
447         scatter(KVec, Data( 1 , : ))
448         axis([-1 1 -inf inf])
449     end
450 end
451 end
452 a = a x e s ;
453 t1 = title(' Torque Rod Power (W) v s Des Vars ');
454 a.Visible = ' off'; %set(a,'Visible','off');
455 t1.Visible = ' on'; %set(t1,'Visible','on');
456 %% Star Tracker
457 Data( 1 , : ) = STX.*STY.*STZ;
458 fSTVol = figure;
459 for i = 1 :NUMFAC
460     for j = 1 :NUMFAC
461         if i == j
462             varname = cellstr(DesVarNames{ i });
463             subplot(NUMFAC, NUMFAC, (NUMFAC* i -NUMFAC)+j)
464             scatter(Data( i + 1 , : ), Data( 1 , : ))

```

```

465         xlabel(varname)
466         axis([-1 1 -inf inf])
467     elseif j > i
468         KVec = Data(i+1,:).*Data(j+1,:);
469         %dissp(min(KVec));
470         %dissp(max(KVec));
471         subplot(NUMFAC,NUMFAC,(NUMFAC*i-NUMFAC)+j)
472         scatter(KVec,Data(1,:))
473         axis([-1 1 -inf inf])
474     end
475 end
476 end
477 a = axes;
478 t1 = title('Star Tracker Volume (mm^3) vs Des Vars');
479 a.Visible = 'off'; % set(a,'Visible','off');
480 t1.Visible = 'on'; % set(t1,'Visible','on');
481 Data(1,:) = STMass;
482 fRxMass = figure;
483 for i = 1:NUMFAC
484     for j = 1:NUMFAC
485         if i == j
486             varname = cellstr(DesVarNames{i});
487             subplot(NUMFAC,NUMFAC,(NUMFAC*i-NUMFAC)+j)
488             scatter(Data(i+1,:),Data(1,:))
489             xlabel(varname)
490             axis([-1 1 -inf inf])
491         elseif j > i

```

```

492      KVec = Data(i+1,:).*Data(j+1,:);
493      %disp(min(KVec));
494      %disp(max(KVec));
495      subplot(NUMFAC,NUMFAC,(NUMFAC*i-NUMFAC)+j)
496      scatter(KVec,Data(1,:))
497      axis([-1 1 -inf inf])
498
499 end
500
501 a = axes;
502 t1 = title('Star Tracker Mass (kg) vs Des Vars');
503 a.Visible = 'off'; % set(a,'Visible','off');
504 t1.Visible = 'on'; % set(t1,'Visible','on');
505 Data(1,:) = STPWR;
506 fRxPower = figure;
507 for i = 1:NUMFAC
508     for j = 1:NUMFAC
509         if i == j
510             varname = cellstr(DesVarNames{i});
511             subplot(NUMFAC,NUMFAC,(NUMFAC*i-NUMFAC)+j)
512             scatter(Data(i+1,:),Data(1,:))
513             xlabel(varname)
514             axis([-1 1 -inf inf])
515         elseif j > i
516             KVec = Data(i+1,:).*Data(j+1,:);
517             %disp(min(KVec));
518             %disp(max(KVec));

```

```

519 subplot(NUMFAC, NUMFAC, (NUMFAC*i-NUMFAC)+j)
520 scatter(KVec, Data(1,:))
521 axis([-1 1 -inf inf])
522 end
523 end
524 end
525 a = axes;
526 t1 = title('Star Tracker Power (W)vs Des Vars');
527 a.Visible = 'off'; % set(a,'Visible','off');
528 t1.Visible = 'on'; % set(t1,'Visible','on');

```

D.2 Optimization Codes

D.2.1 Payload Optimization

```

1
2 #!/usr/bin/env python
3 # =====
4 # Standard Python modules
5 # =====
6 import os, sys, time
7 import pdb
8 import numpy as np
9 import math
10 # Run with Python 2.7 distribution on laptop else crashy crash
11 # =====
12 # Extension modules
13 # =====
14 #from pyOpt import *

```

```

15 from pyOpt import Optimization
16 from pyOpt import KSOPT
17 # =====
18 # Variable Mapping
19 # =====
20 #     x[0] = Altitude
21 #     x[1] = IAMax
22 #     x[2] = YMax
23 #     x[3] = Bit Per Pixel
24 #     x[4] = Pixel Instrument Count
25 #     x[5] = Detector Width
26 #     x[6] = Quality Factor
27 #     x[7] = Operational Wavelength
28 # =====
29 # Definitions for Obj Function
30 # =====
31 def objfunc(x):
32     #Design Equations for Optical Payload
33     OrbPer = 1.658669e-04*(6378.14+x[0])**1.5
34     GroundVelocity = 2*math.pi*6378.14/OrbPer/60
35     AngRadius = math.asin(6378.14/(6378+x[0]))*180/math.pi
36     LNot = 90-AngRadius
37     DMax = math.tan(LNot*math.pi/180)*6378.14 #returns km
38     EtaLook = math.asin(math.cos((90-x[1])*math.pi/180)*math.sin(
39         AngRadius*math.pi/180))*180/math.pi
40     ECAMax=90-(90-x[1])-EtaLook
41     SlantRange = 6378.14*math.sin(ECAMax*math.pi/180)/math.sin(

```

```

        EtaLook *math . pi /180 )

41   SwathWidth = 2*ECAMax
42   IFOV = x[2]/1000/SlantRange *180/math . pi
43   XMax = x[2]/math . cos(x[1]* math . pi/180)
44   CrossTrackPixelResolution = IFOV*x[0]* math . pi/180
45   AlongTrackPixelResolution = IFOV*x[0]* math . pi/180
46   CrossTrackPixelCount = 2* EtaLook/IFOV
47   SwathCount = GroundVelocity/AlongTrackPixelResolution
48   PixelRate = SwathCount* CrossTrackPixelCount
49   DataRate = PixelRate*x[3]
50   PixelIntegrationTime = AlongTrackPixelResolution*x[4]/
      GroundVelocity/CrossTrackPixelCount
51   FocalLength = x[0]*x[5]/CrossTrackPixelResolution
52   ApertureDiameter = 2.44*x[7]* FocalLength*x[6]/x[5]
53   FOV= IFOV*x [ 4 ]
54   Ratio = ApertureDiameter/0.015
55   if Ratio <=0.5:
56       K = 2
57   else:
58       K = 1
59   XDim = Ratio *0.045
60   YDim = Ratio *0.050
61   ZDim = Ratio *0.080
62   PwrEst = K*(Ratio **3)*1.26
63   MassEst = K*(Ratio **3)*0.230
64   GSD = math . tan (IFOV/2*math . pi/180)*2*x[0]
65   f=[ 0 . 0 ] * 4

```

```

66     f[ 0 ] = ApertureDiameter #For Size
67     f[ 1 ] = GSD #For Data quality
68     f[ 2 ] = -PixelIntegrationTime
69     f[ 3 ] = ZDim
70
71     g = [ 0.0 ] * 1
72
73     g[ 0 ] = ZDim - 0.1
74     fail = 0
75
76     return f, g, fail
77
78 #=====
79 # Initialize Optimization Problem
80 #=====
81 optprob = Optimization('Passive Optic Payload Optimization C'
82                         'onstrained', objfunc)
83
84 #optprob.addVar('x1','c',lower=0.1,upper=1.0,value=0.35) # 0.1
85             <=x <= 1
86
87 #optprob.addVar('x2','c',lower=0.0,upper=5.0,value=2.5) # 0 <=y
88             <= 5
89
90 optprob.addVar('Alt',lower=300.0,upper=450.0,value=400.0)
91 opt_prob.addVar('IA_Max', lower = 30.0, upper = 77.0, value =
92                 50.)
93
94 optprob.addVar('YMax',lower = 0.1,upper = 150.0,value = 20.)
95
96 optprob.addVar('BPP',lower=8.,upper = 16.,value = 8.)
97
98 optprob.addVar('PIC',lower=100,upper = 1000,value = 300)
99
100 opt_prob.addVar('DetWidth',lower = 1.1e-6,upper = 30.0e-6,
101                  value = 2.0e-6)
102
103 optprob.addVar('QualFac',lower = 1.1,upper = 2.0,value = 1.5)
104
105 optprob.addVar('OpWavelength',lower = 3.0e-06,upper = 17.0e

```

```

-06 , v a l u e = 5 e -06)

88 optprob.addObj('f')

89 optprob.addCon('g', type='i', lower = -1e21, upper = 0.0)

90 print optprob #VFY

91 # =====

92 # Initialize Solver and Solve/Record

93 # =====

94 ksopt = KSOPT()

95 ksopt.setOption('IPRINT', 2)

96 ksopt(optprob, sens_type='FD', store_hst=True)

97 optprob.write2file('FileTest.txt')

98 print optprob.solution(0)

99 # =====

100 #     x[0] = Altitude

101 #     x[1] = IAMax

102 #     x[2] = YMax

103 #     x[3] = Bit Per Pixel

104 #     x[4] = Pixel Instrument Count

105 #     x[5] = Detector Width

106 #     x[6] = Quality Factor

107 #     x[7] = Operational Wavelength

```

D.2.2 Payload Optimization Verification

```

1 %% Quick Check

2 clc; clear all; close all;

3 %%

4 Alt = 400000 %

```

```

5 DetWidth = 1.19e-6; %sq pixel size
6 f = 4.02e-3; %physical focal
7 IFOV = 2*atan2d(DetWidth,(2*f)) %deg
8 GSD = 2*Alt*tand(IFOV/2) %convert to deg and perform tangent
9 %%Verify the payload optimization results
10 %x = [7007068825630e-6 1.142e-6] %FIRESAT
11 x = [300301008300.4e-4 1.13e-5]
12 OrbPer = 1.658669e-04*(6378.14+x(1))^1.5
13 GroundVelocity = 2*pi*6378.14/OrbPer/60
14 AngRadius = asin(6378.14/(6378+x(1)))*180/pi
15 LNot = 90-AngRadius
16 DMax = tan(LNot*pi/180)*6378.14 %returns km
17 EtaLook = asin(cos((90-x(2))*pi/180)*sin(AngRadius*pi/180))*180/
    pi
18 ECAMax = 90-(90-x(2))-EtaLook
19 SlantRange = 6378.14 * sin(ECAMax*pi/180) / sin(EtaLook*pi/180)
20 SwathWidth = 2*ECAMax
21 IFOV = x(3)/1000/SlantRange*180/pi
22 XMax = x(3)/cos(x(2)*pi/180)
23 CrossTrackPixelResolution = IFOV*x(1)*pi/180 %in km
24 AlongTrackPixelResolution = IFOV*x(1)*pi/180 %in km
25 CrossTrackPixelCount = 2*EtaLook/IFOV
26 SwathCount = GroundVelocity/AlongTrackPixelResolution
27 PixelRate = SwathCount*CrossTrackPixelCount
28 DataRate = PixelRate*x(4)
29 PixelIntegrationTime = AlongTrackPixelResolution*x(5)/
    GroundVelocity/CrossTrackPixelCount

```

```

30 FocalLength = x(1)*x(6)/CrossTrackPixelResolution
31 ApertureDiameter = 2.44*x(8)*FocalLength*x(7)/x(6)
32 FOV = IFOV*x ( 5 )
33 Ratio = ApertureDiameter/0.406
34 if Ratio <= 0.5
35     K = 2
36 else
37     K = 1
38 end
39 XDim = Ratio * 2 . 0
40 YDim = Ratio * 0 . 7
41 ZDim = Ratio * 0 . 9
42 PwrEst = K*( Ratio ^3 ) *280
43 MassEst = K*( Ratio ^3 ) *239
44 GSDPayload = 2*x ( 1 ) *1000* tand ( IFOV/2 )

```

D.2.3 ADCS Optimization

```

1
2 #! /usr/bin/env python
3 # =====
4 # Standard Python modules
5 # =====
6 import os, sys, time
7 import pdb
8 import numpy as np
9 import math
10 # Run with Python 2.7 distribution on laptop else crashy crash

```

```

11 # =====
12 # Extension modules
13 # =====
14 #from pyOpt import *
15 from pyOpt import Optimization
16 from pyOpt import KSOPT
17 # =====
18 # Definitions for Obj Function
19 # =====
20 def objfunc(x):
21     #Design Equations for Optical Payload
22     arc = x[13] * 180 / math.pi
23     GravGradient = 3*3986e14/2/(x[0]**3)*abs(x[2]-x[1])*math.sin
24         (2*x[3])
25     SolarRadiation = (1367/3e8*x[6]*(1+x[7])*math.cos(x[8]))*(x
26         [4]-x[5])
27     MagneticField = (2*7.96e15)/(x[0]**3)*x[9]
28     atmos = np.array([[0, 0.00, 1.23, 7.25],
29                     [25, 25.00, 3.899e-2, 6.35],
30                     [30, 30.00, 1.774e-2, 6.68],
31                     [40, 40.00, 3.972e-3, 7.55],
32                     [50, 50.00, 1.057e-3, 8.38],
33                     [60, 60.00, 3.206e-4, 7.71],
34                     [70, 70.00, 8.770e-5, 6.55],
35                     [80, 80.00, 1.905e-5, 5.80],
36                     [90, 90.00, 3.396e-6, 5.38],
37                     [100, 100.00, 5.297e-7, 5.88],
38                     [110, 110.00, 8.594e-8, 5.23],
39                     [120, 120.00, 1.289e-8, 4.63],
40                     [130, 130.00, 1.838e-9, 4.03],
41                     [140, 140.00, 2.517e-10, 3.43],
42                     [150, 150.00, 3.334e-11, 2.83],
43                     [160, 160.00, 4.281e-12, 2.23],
44                     [170, 170.00, 5.358e-13, 1.63],
45                     [180, 180.00, 6.565e-14, 1.03],
46                     [190, 190.00, 7.902e-15, 0.43],
47                     [200, 200.00, 9.369e-16, 0.00}])
48     return [GravGradient, SolarRadiation, MagneticField, atmos]

```

```

36      [ 110, 110.00, 9.661e-8, 7.26 ],
37      [ 120, 120.00, 2.438e-8, 9.47 ],
38      [ 130, 130.00, 8.484e-9, 12.64 ],
39      [ 140, 140.00, 3.845e-9, 16.15 ],
40      [ 150, 150.00, 2.070e-9, 22.52 ],
41      [ 180, 180.00, 5.464e-10, 29.74 ],
42      [ 200, 200.00, 2.789e-10, 37.11 ],
43      [ 250, 250.00, 7.248e-11, 45.55 ],
44      [ 300, 300.00, 2.418e-11, 53.63 ],
45      [ 350, 350.00, 9.518e-12, 53.30 ],
46      [ 400, 400.00, 3.725e-12, 58.52 ],
47      [ 450, 450.00, 1.585e-12, 60.83 ],
48      [ 500, 500.00, 6.967e-13, 63.82 ],
49      [ 600, 600.00, 1.454e-13, 71.84 ],
50      [ 700, 700.00, 3.614e-14, 88.67 ],
51      [ 800, 800.00, 1.170e-14, 124.64 ],
52      [ 900, 900.00, 5.245e-15, 181.05 ],
53      [ 1000, 1000.00, 3.019e-15, 268.00 ]])
54  for i in range(27):
55      if x[0] >= atmos[i,0] and x[0] < atmos[i+1,0]:
56          H = atmos[i,3]
57          rhon = atmos[i,2]
58          base = atmos[i,1]
59      elif x[0] >= atmos[i+1,0]:
60          H = atmos[i+1,3]
61          rhon = atmos[i+1,2]
62          base = atmos[i+1,1]

```

```

63 Density = rhon *math . exp (-(x [ 0 ]/1 0 0 0 - b a s e )/H)
64 vel= math . s q r t (3 . 9 8 6 e14/x [ 0 ])
65 AerodynamicTorque = (0.5*Density*x[10]*x[6]*vel*vel)*(x[14] -
   x[5])
66 DistubranceTorque = AerodynamicTorque + GravGradient +
   MagneticField + SolarRadiation
67 OrbitPeriod = 1.658669e-04*(x[0]/1000) **1.5
68 SlewTorque = 4*x[11]* math . pi/180*x[2]/(x[12]**2)
69 H = DistubranceTorque * OrbitPeriod / 4 * 0.707
70 if H <= 0.015: #Smallest found reaction wheel
71     H = 0 . 0 1 5
72 MagDipole = 1.5* DistubranceTorque/MagneticField
73 RxVol = (20.55*math . log (H)+120.4)*(20.21*math . log (H)+118.0)
   *(2 3 . 6 1 * math . l o g (H)+1 0 0 . 2 )
74 Mtx = (0.1216 + 10.87*MagDipole)
75 Mty = (118.0 + 3.363*MagDipole)
76 Mtz = (100.2 + 26.67*MagDipole)
77 STVol= (-6071* arc + 196.3)*(-6500* arc + 200.3)*(-1.536 e4* arc
   + 3 8 7 )
78 PwrST = -4.592 e4* arc **2 + 750* arc + 5
79 Pwr = -4.592 e4* arc **2 + 750* arc + 5+ 0.466*H + .5106 +
   .0 5 0 2 * MagDipole + .3 9 9
80 Mass = -7296* arc **2 + 31.79* arc + 2.735 + 1.666*H+.1216 +
   .0 0 1 0 2 9 * MagDipole +.3457
81 f=[ 0 . 0 ]* 5
82 f [ 0 ]= -x [ 1 3 ]
83 f [ 1 ]= Pwr

```

```

84     f [ 2 ]= x [ 1 2 ]
85     f [ 3 ]=Mass
86     f [ 4 ]=MagDipole
87     g = [ 0.0]*3
88     g [ 0 ] = Mtx - 100
89     g [ 1 ] = Mty - 100
90     g [ 2 ] = Mtz - 100
91     fail=0
92     return f ,g, fail
93 # =====
94 # Variable Mapping and Constants
95 # =====
96 #     x [ 0 ]= R Radius (m)
97 #     x [ 1 ] = Iy
98 #     x [ 2 ] = Iz
99 #     x [ 3 ] = IncidenceAngle (Theta )
100 #    x [ 4 ] = CenterSolarPressure
101 #    x [ 5 ] = CenterGravity
102 #    x [ 6 ] = SurfaceArea
103 #    x [ 7 ] = ReflectionFactor
104 #    x [ 8 ]=SunIA
105 #    x [ 9 ] = Residual Dipole (D)
106 #    x [ 10 ] = CoeffDrag
107 #    x [ 11 ]=SlewMaxDeg
108 #    x [ 12 ]=SlewMaxTime
109 #    x [ 13 ]= PointKnowledge ( o )
110 #    x [ 14 ] = CenterPressure

```

```

111 # =====
112 # Initialize Optimization Problem
113 # =====
114 optprob = Optimization('ADCS Optimization', objfunc)
115 #optprob.addVar('x1','c',lower=0.1,upper=1.0,value=0.35) # 0.1
116 #optprob.addVar('x2','c',lower=0.0,upper=5.0,value=2.5) # 0 <=y
117 #<=5
118 optprob.addVar('Radius', lower=6621e3, upper=6621e3, value=6621
119 e3)
120 optprob.addVar('Iy', lower = 1.9e-3, upper = 2.1e-3, value = 2e
121 -3)
122 optprob.addVar('Iz', lower = 1.7e-3, upper = 1.8e-3, value =
123 1.75e-3)
124 optprob.addVar('IA', lower=0., upper = 5., value = 0.)
125 optprob.addVar('CSP', lower=.02, upper = .02, value = .02)
126 optprob.addVar('CG', lower = 0.0, upper = 0.0, value = 0.0)
127 optprob.addVar('SA', lower = .0292, upper = .0298, value =
128 .0294)
129 optprob.addVar('Reflect', lower = 0.5, upper = 0.8, value =
0.65)
130 optprob.addVar('SunIA', lower = 0.0, upper= 30*math.pi/180,
131 value = 0.0)
132 optprob.addVar('RD', lower = 1.0, upper = 1.2, value = 1.1)
133 optprob.addVar('Cd', lower = 2.0, upper = 2.2, value = 2.1)
134 optprob.addVar('SlewAng', lower = 10.0*math.pi/180, upper =
135 35.0*math.pi/180, value = 30.0*math.pi/180)

```

```

129 opt_prob.addVar('SlewTime', lower = 4.0, upper = 60.0, value =
10.0)

130 optprob.addVar('PointKnwledge',lower = .007*math.pi/180, upper
= .021 * math.pi/180, value= .015 * math.pi/180)

131 optprob.addVar('Cp',lower = .01,upper = .03,value = .02)

132 optprob.addObj('f')

133 optprob.addCon('g',type='i',lower = -1e21,upper = 0.0)

134 print optprob #VFY

135 # =====

136 # Initialize Solver and Solve/Record

137 # =====

138 ksopt = KSOPT()

139 ksopt.setOption('IPRINT',2)

140 ksopt.setOption('IFILE','ADCS KS Soln.txt')

141 ksopt(optprob,sens_type='FD',store_hst=True)

142 optprob.write2file('ADCSOpt.txt')

143 print optprob.solution(0)

```

D.3 Codes for Benchmarks

D.3.1 Benchmark Visualization

```

1 %%Example Search Space for Constrained Optimization Problems

2 % Justin Ancheta

3 % March 2nd 2018

4 % Code for visualizing the benchmark optimization problem for
% masters proj.

5 close all; clear all;clc;

6 %%Objective Functions, Constraints, Search Region

```

```

7  fone = @(x) x;
8  ftwo = @(x,y) (1+y)/x;
9  gone = @(x,y) y + 9*x - 6; %gone must be greater than or equal
   to 0
10 gtwo = @(x,y) -y + 9*x - 1; %gtwo must be greater than or equal
    to 0
11 %%Visual Search Region
12 figure
13 [x1,x2] = meshgrid([0.1:0.001:1],[0.0:0.01:5]);
14 zed = ones(size(x1));
15 bound1 = x2 + 9*x1 - 6 >= 0;
16 bound2 = -x2 + 9*x1 - 1 >= 0;
17 zed(~bound1)=0;
18 zed(~bound2)=0;
19 contourf(x1,x2,zed)
20 title('Region available in design space')
21 xlabel('x_1 = x')
22 ylabel('x_2 = y')
23 cmap = jet(2);
24 cmap(1,:)= [1,1,1];
25 colormap(cmap);
26 colorbar('Ticks',[0.25 0.75], 'TickLabels',{'Unavailable','
   Available'})
27 %%Finding the values off 1 and f2
28 %%Creating the design space
29 data x1 = x1.* zed;
30 data x2 = x2.* zed;

```

```

31 size_data = size(x1);
32 lengthx = size_data(1);
33 lengthy = size_data(2);
34 outf1 = zeros(lengthx, lengthy);
35 outf2 = outf1;
36 for i = 1:lengthx
37     for j = 1:lengthy
38         outf1(i,j) = fone(datax1(i,j));
39         outf2(i,j) = ftwo(datax1(i,j), datax2(i,j));
40     end
41 end
42 outf1(outf1==0) = NaN;
43 %% f1 v f2 v a r s
44 out2f1 = reshape(outf1, [lengthx*lengthy 1]);
45 out2f2 = reshape(outf2, [lengthx*lengthy 1]);
46 %%Viewing f1 and f2
47 %Function 1
48 figure
49 h = surf(x1, x2, outf1);
50 set(h, 'LineStyle', 'none')
51 title('Output off 1')
52 xlabel('x_1 = x')
53 ylabel('x_2 = y')
54 zlabel('f1')
55 colorbar
56 %Function 2
57 figure

```

```

58 h = surf(x1,x2,outf2);
59 set(h,'LineStyle','none')
60 title('Output off2')
61 xlabel('x_1 = x')
62 ylabel('x_2 = y')
63 zlabel('f2')
64 colorbar
65 %f1 v f2
66 figure
67 plot(out2f1,out2f2)
68 xlabel('f1')
69 ylabel('f2')
70 title('f1 vs f2')
71 %%Pareto Frontier
72 fitfunction=@(x)[x(1),(1+x(2))/x(1)];
73 nvars=2;
74 a=[-9,-1;-9,1];%same as above bounds but meant for leq not geq
75 b=[-6,-1];
76 lb=[0.1 0];
77 ub=[1, 5];
78 [ParFront,fval]=gamultiobj(fitfunction,nvars,a,b,[],[],lb,ub);
79 %%View Pareto Frontier
80 figure
81 plot(fval(:,1),fval(:,2),'r*')
82 hold on
83 xlabel('f1')
84 ylabel('f2')

```

```

85 title('Pareto Front')
86 %% KS from pyOpt
87 fileID = 'BenchOptData.csv';
88 dataKSOPT = csvread(fileID,1,0);
89 i_ters = size(dataKSOPT)
90 for i=1:i_ters(1)
91     dataKSOPT(i,4) = fone(dataKSOPT(i,1));
92     dataKSOPT(i,5) = ftwo(dataKSOPT(i,1),dataKSOPT(i,2));
93 end
94 sz = 5;
95 scatter(dataKSOPT(1,4),dataKSOPT(1,5),'ko','filled')
96 scatter(dataKSOPT(:,4),dataKSOPT(:,5),sz,'c*')
97 legend('Pareto front','KS Solution Final','KS Initial Guess','KS Evaluations')
98 %% Visualizing KS
99 figure
100 plot3(dataKSOPT(:,1),dataKSOPT(:,2),dataKSOPT(:,3))
101 hold on
102 plot3(dataKSOPT(1,1),dataKSOPT(1,2),dataKSOPT(1,3),'ro')
103 plot3(dataKSOPT(end,1),dataKSOPT(end,2),dataKSOPT(end,3),'ko')
104 xlabel('x1')
105 ylabel('x2')
106 zlabel('KS')
107 legend('KS','KS_o','KS_f')
108 title('Evaluation of KS')

```

D.3.2 Benchmark Optimization

```
1 #!/usr/bin/env python
2 # =====
3 # Standard Python modules
4 # -----
5 import os, sys, time
6 import pdb
7 # Run with Python 2.7 distribution on laptop else crashy crash
8 # =====
9 # Extension modules
10 # -----
11 #from pyOpt import *
12 from pyOpt import Optimization
13 from pyOpt import KSOPT
14 # -----
15 # Definitions for Obj Function
16 # -----
17 def objfunc(x):
18     c = x[0]
19     d = (x[1]+1)/x[0]
20     f=[0.0]*2
21     f[0] = c
22     f[1] = d
23     g = [0.0]*2
24     g[0] = -9.*x[0] - x[1] + 6
25     g[1] = -9.*x[0] + x[1] + 1
26
27 fail=0
```

```

28     return f,g, fail
29 # =====
30 # Initialize Optimization Problem
31 # -----
32 optprob = Optimization('Benchmark ConstEx Constrained Problem',o
bjfunc)
33 optprob.addVar('x1','c',lower=0.1,upper=1.0,value=0.35)
34 optprob.addVar('x2','c',lower=0.0,upper=5.0,value=2.5)
35 optprob.addObj('f')
36 opt_prob.addCon('g1','i')
37 opt_prob.addCon('g2','i')
38 print optprob #VFY
39 # =====
40 # Initialize Solver and Solve/Record
41 # -----
42 ksopt = KSOPT()
43 ksopt.setOption('IPRINT',2)
44 ksopt(optprob,sens_type='FD',store_hst=True)
45 optprob.write2file('FileTest.txt')
46 print optprob.solution(0)

```

D.4 MBSE Supporting Functions

D.4.1 NBody Function

¹ %%N Body Function

² % Justin Ancheta

³ % December 18 2017 – updated 12/18/2017

⁴ % rev 0.00

```

5 %%Revision log
6 % 12/18/17 – Base Code Started
7 %
8 %%Purpose and Use
9 %

10 % This function file will generate the set of functions for the
   integrator.

11 % nbody=f(ic,i,m) where ic(i) is a [7*n+1,1] set of positions
   and velocities

12 % given in the form of [ r1 , r2 , r3 , ..., rn , v1 , v2 , v3 , ..., vn , m1 , ..., mn
   , n ]

13 %

14 %%Construction of set of functions for Integrators

15 % The set of equations needed based on i are

16 % [ v1x , v1y , v1z , v2x , v2y , v2z , ..., vnx , vny , vnz , a1x , a1y , a1z , ..., anx , any
   , anz ]

17 % as y = [ rx ry rz vx vy vz ] and y' = [ vx vy vz ax ay az ]

18 function dx = nbody(t,y,m)

19 G = 6.67408e-20; %km^3/( kg s^2 )

20 n = length(m);

21 endval = 6*n;

22 dx = zeros(6*n,1);

23 xpos = y(1:3:endval/2);

24 ypos = y(2:3:endval/2);

25 zpos = y(3:3:endval/2);

26 tx = b_sxfun(@minus,xpos,xpos'); %difference between x of i and j
27 ty = b_sxfun(@minus,ypos,ypos'); %see above for y

```

```

28 t z = b s x f u n ( @minus , zpos , zpos' ); %s e e above f o r z
29 r = s q r t ( tx .^2+ ty .^2+ t z .^2 ) .^3 ; %cubed d i s t a n c e b e t w e e n I a n d J
30 %% c h a n g i n g y' ( 1 : e n d / 2 ) t o p r e v i o u s y' ' v a l u e s
31 f o r i = 1 : 3 * n
32 dx ( i ) = y ( i + 3 * n );
33 e n d
34 %% C a l c u l a t i n g x y a n d z a c c e l e r a t i o n s
35 r = r + e y e ( n ); %t o p r e v e n t s i n g u l a r i t i e s
36 m t = r e p m a t ( m , n , 1 ) ' ; %r e p e a t s m f o r f o r c e s
37 f x = m t . / r . * t x ;
38 f x ( 1 : ( n + 1 ) : n * n ) = 0 ;
39 f x i = s u m ( f x , 1 );
40 f y = m t . / r . * t y ;
41 f y ( 1 : ( n + 1 ) : n * n ) = 0 ;
42 f y i = s u m ( f y , 1 );
43 f z = m t . / r . * t z ;
44 f z ( 1 : ( n + 1 ) : n * n ) = 0 ;
45 f z i = s u m ( f z , 1 );
46 f o r i = 1 : n
47 dx ( i * 3 + n * 3 - 2 ) = G * f x i ( i );
48 dx ( i * 3 + n * 3 - 1 ) = G * f y i ( i );
49 dx ( i * 3 + n * 3 ) = G * f z i ( i );
50 e n d
51 e n d

```

D.4.2 Solar Line of Sight with Penumbra

```

1 f u n c t i o n y = f c n ( u )

```

```

2 % BASED ON HWANGS DISSERTATION SMOOTHING FUNCTION FOR UMBRA

3 y = 0;

4 Re = 6371.01;

5 PosSun = [ u(1); u(2); u(3) ];

6 PosEarth = [ u(4); u(5); u(6) ];

7 PosSat = [ u(7); u(8); u(9) ];

8 alp = u(10);

9 SatEarth = PosSat - PosEarth;

10 EarthSun = PosEarth - PosSun;

11 EarthSun = EarthSun /norm ( EarthSun );

12 ds = norm ( cross ( SatEarth , EarthSun ) );

13 eta = (ds-alp*Re)/(Re-alp*Re);

14 check = dot ( SatEarth , EarthSun );

15 if check >= 0

16     y = 1;

17 elseif ds > Re

18     y = 1;

19 elseif ds < alp *Re

20     y = 0;

21 else

22     y = 3*eta^2-2*eta^3;

23 end

```

D.5 Simulink Run and Test Code

```

1 %%N-Body Simulation Simulink Analysis

2 clc; clear all; close all;

3 format long g

```

⁴ %% Rotations

⁵ %

⁶ % ICRF/BCRF—GCRF TBD; GCRF ICRF BCRF ARE ESSENTIALLY ALIGNED FOR MOST

⁷ % APPLICATIONS . THIS WILL REQUIRE ACTUAL WORK AND RESEARCH TO DO RIGHT.

⁸ % ASSUME EFFECTS ARE SMALL FOR THE TIME BEING .

⁹ % IAU , SOFA Tools for Earth Attitude]

¹⁰ %

¹¹ %% Various Constants and Inputs

¹² SimTime = (60 *60 *24) * 5 ; %1 day simulation

¹³ DistAutoKM = 1.496e+8;

¹⁴ TimeDaytoSec = 60 *60 *24 ;

¹⁵ SunAlpha = 0.9 ;

¹⁶ % Solar Array Design Options

¹⁷ PowerType = 'DET' ; %Case sensitive: Options include DET (direct energy transfer) or PPT(Peak Power Tracking)

¹⁸ Peclipse = 100; %Watts needed power eclipse

¹⁹ Pday = 100 ; %Watts needed power during time in sun

²⁰ SunTempMax = 100; %Maximum temperture of solar cell array

²¹ EclipseTempMax = -80; %Minimum temperatre of solar cell array

²² %% Benchmark against JPL Horizons for Earth Pos

²³ % HORZDATA= csvread('EarthTestXYZ.csv',1);

²⁴ % % Earth Sun Moon Initial Conditions March 25, 2018 from Horizons

²⁵ % MassSun = 1.988544e30 ; %kg

²⁶ % MassEarth = 5.97219e24 ; %kg

```

27 % MassMoon = 734.9e20 ; %kg
28 % MassJupiter = 1898.13e24 ;
29 % MassSat = 10 ; %kg
30 % RadSun = 6.963e5 ; %km
31 % RadEarth = 6371.01 ; %km
32 % RadMoon = 1737.4 ; %km
33 % PosSunAU = [1.293353689013552e-03; 6.522361385771349e
               -03; -1.079851494007183 e-04];
34 % VelSunAUD = [ -6.409885860066381e-06; 4.440045984244416e
                  -06; 1.528999606408731e-07];
35 % PosEarthAU = [ -9.933675647884848E-01; -6.380096968050979 e-02;
                   -9.938491024392269 e-05 ];
36 % VelEarthAUD = [ 9.341394242566131e-04; -1.722037211216111 e
                  -02; 3.297113152345686e-07];
37 % PosMoonAU = [ -9.937383674834914e-01; -6.135886608208557 e-02;
                  -2.263388774617808 e-04 ];
38 % VelMoonAUD = [ 3.321828061507152e-04; -1.731613336450174 e-02;
                   4.558197105418077e-05];
39 % PosJupiterAU = [ -3.852523741724474e0; -3.800676827730020e0;
                     1.019361973208450e-01];
40 % VelJupiterAUD = [ 5.211670508998708e-03; -5.013451102063293 e-03;
                      -9.574580960891983 e-05];
41 % PosSatAU = [ -9.933738053211382E-01; -6.384356151687003E-02;
                  -8.512557260487344E-05];
42 % VelSatAUD = [ 3.699397572966039E-03; -1.867888405149421E
                  -02; -3.136616450617170E-03];
43 % PosSun = PosSunAU*DistAUtoKM ;

```

```

44 % PosEarth = PosEarthAU*DistAUtoKM ;
45 % PosMoon = PosMoonAU*DistAUtoKM ;
46 % PosJupiter = PosJupiterAU *DistAUtoKM ;
47 % PosSat = PosSatAU*DistAUtoKM ;
48 % VelSun = VelSunAUD*DistAUtoKM/ TimeDaytoSec ;
49 % VelEarth = VelEarthAUD*DistAUtoKM/ TimeDaytoSec ;
50 % VelMoon = VelMoonAUD*DistAUtoKM/ TimeDaytoSec ;
51 % VelJupiter = VelJupiterAUD *DistAUtoKM/ TimeDaytoSec ;
52 % VelSat = VelSatAUD*DistAUtoKM/ TimeDaytoSec ;
53 sim ('NBODYSIMULINK') ;
54 %% Compare to Benchmark
55 % This is for fixed step size of 60s and one day only for testing
.
.
56 % if SimTime == 86400
57 % figure
58 % plot3(HORZDATA(:,2),HORZDATA(:,3),HORZDATA(:,4))
59 % hold on
60 % plot3(body2xyz.data(:,1),body2xyz.data(:,2),body2xyz.data
(:,3)) %Earth
61 % title('Benchmark of 1 Day from IC')
62 % legend('HORIZONS-ISS','NbodySim')
63 % RelativePosOffsetJPL = 100* abs([ body2xyz.data(:,1),body2xyz
.d a ta(:,2),body2xyz .d a ta(:,3)]-[HORZDATA(:,2),HORZDATA(:,3),
HORZDATA(:,4)]./[HORZDATA(:,2),HORZDATA(:,3),HORZDATA(:,4)]);
64 % MaxErrorXYZ = max(RelativePosOffsetJPL)
65 % MinErrorXYZ = min(RelativePosOffsetJPL)
66 % end

```

```

67 %%Sun around B a r y c e n t e r
68 % f i g u r e
69 % p l o t 3 ( body1xyz . d a t a ( : , 1 ) , body1xyz . d a t a ( : , 2 ) , body1xyz . d a t a ( : , 3 ) )
    %Sun
70 %%P l a n e t s around B a r y c e n t e r
71   f i g u r e
72   p l o t 3 ( body1xyz . d a t a ( : , 1 ) , body1xyz . d a t a ( : , 2 ) , body1xyz . d a t a ( : , 3 ) ) %
    Sun
73 %
74 % Sun barely moves from barycenter, only viewable around 1e6
    s c a l e
75 %
76 h o l d o n
77 p l o t 3 ( body2xyz . d a t a ( : , 1 ) , body2xyz . d a t a ( : , 2 ) , body2xyz . d a t a ( : , 3 ) ) %
    Earth
78 p l o t 3 ( body3xyz . d a t a ( : , 1 ) , body3xyz . d a t a ( : , 2 ) , body3xyz . d a t a ( : , 3 ) ) %
    Moon
79 p l o t 3 ( body4xyz . d a t a ( : , 1 ) , body4xyz . d a t a ( : , 2 ) , body4xyz . d a t a ( : , 3 ) ) %
    J u p i t e r
80 s c a t t e r 3 ( 0 , 0 , 0 ) %B A R Y C E N T E R
81 g r i d o n
82 t i t l e ( ' P o s i t i o n w r t B a r y c e n t e r o f S o l a r S y s t e m ' )
83 l e g e n d ( ' S u n ' , ' E a r t h ' , ' M o o n ' , ' J u p i t e r ' )
84 x l a b e l ( ' x ( k m ) ' )
85 y l a b e l ( ' y ( k m ) ' )
86 z l a b e l ( ' z ( k m ) ' )
87 %% Earth Moon Sat wrt to Sun

```

```

88 EarthSun = [ body2xyz . d a ta (:, 1), body2xyz . d a ta (:, 2), body2xyz . d a ta
( :, 3 ) ] - [ body1xyz . data (:, 1), body1xyz . data (:, 2), body1xyz . data
( :, 3 ) ];
89 MoonSun = [ body3xyz . d a ta (:, 1), body3xyz . d a ta (:, 2), body3xyz . d a ta
( :, 3 ) ] - [ body1xyz . data (:, 1), body1xyz . data (:, 2), body1xyz . data
( :, 3 ) ];
90 SatSun = [ body5xyz . d a ta (:, 1), body5xyz . d a ta (:, 2), body5xyz . d a ta
( :, 3 ) ] - [ body1xyz . data (:, 1), body1xyz . data (:, 2), body1xyz . data
( :, 3 ) ];
91 figure
92 plot3(EarthSun (:, 1), EarthSun (:, 2), EarthSun (:, 3))
93 hold on
94 plot3(MoonSun (:, 1), MoonSun (:, 2), MoonSun (:, 3))
95 plot3(SatSun (:, 1), SatSun (:, 2), SatSun (:, 3))
96 title('Position w.r.t. Sun')
97 legend('Earth', 'Moon', 'Sat')
98 grid on
99 xlabel('x (km)')
100 ylabel('y (km)')
101 zlabel('z (km)')
102 %% Moon/ Sat with respect to Earth
103 MoonEarth = [ body3xyz . data (:, 1), body3xyz . data (:, 2), body3xyz . data
( :, 3 ) ] - [ body2xyz . data (:, 1), body2xyz . data (:, 2), body2xyz . data
( :, 3 ) ];
104 SatEarth = [ body5xyz . data (:, 1), body5xyz . data (:, 2), body5xyz . data
( :, 3 ) ] - [ body2xyz . data (:, 1), body2xyz . data (:, 2), body2xyz . data
( :, 3 ) ];

```

```

105 [Ex,Ey,Ez] = sphere(20);
106 xEast = RadEarth * Ex;
107 yNorth = RadEarth * Ey;
108 zUp = RadEarth * Ez;
109 figure
110 plot3(MoonEarth(:,1),MoonEarth(:,2),MoonEarth(:,3))
111 hold on
112 plot3(SatEarth(:,1),SatEarth(:,2),SatEarth(:,3))
113 surf(xEast,yNorth,zUp,'FaceColor','blue','FaceAlpha',0.5)
114 title('Moon/Sat Orbit around Earth')
115 legend('Moon','Satellite')
116 axlim = 5e5;
117 axis([-axlim axlim -axlim axlim -axlim axlim])
118 grid on
119 xlabel('x (km)')
120 ylabel('y (km)')
121 zlabel('z (km)')
122 %%LOS over time (ISS on March 25th 2018) – Check against STKS
123 till
124 % This is only useful in really small durations (< 1day),
125 % otherwise you get
126 % a really solid block which is useless.
127 % figure
128 % plot(LOS.time(:,1),LOS.data(:,1))
129 % title('LOS-{ Earth } over Time of Sat')

```

```

130 % xlabel(' Time ( hour ) ')
131 % ylabel(' LOS ')
132 %%Finding Solar Array Power Size
133 switch PowerType
134     case 'DET'
135         Xe = 0.65 ;
136        Xd = 0.85 ;
137     case 'PPT'
138         Xe = 0.6 ;
139         Xd = 0.8 ;
140     otherwise %ideal
141         Xe = 1 ;
142         Xd = 1 ;
143 end
144 LOSDayFrac = mean (LOS.data(:,1));
145 LOSNightFrac = 1 - LOSDayFrac ;
146 PsaReqEst = (Peclipse*LOSNightFrac/Xe + Pday*LOSDayFrac/Xd);
147 %% Altitude over time
148 Altitude = [1:1:length(SatEarth)];
149 for i = 1:length(SatEarth)
150     Altitude(i) = dot(SatEarth(i,:),SatEarth(i,:)/norm(SatEarth(i
151 ,:))) - 6371;
152 end
153 figure
154 plot(Altitude)

```