DEC 4, 2020 6:00 P.M. TO 9:30 P.M. PROCTOR: HUMMEL & LIU

## **INSTRUCTIONS:**

- 1. Answer ONLY the specified number of questions from the options provided in each section. Do not answer more than the required number of questions. Each section takes one hour.
- 2. Your answers must be on the paper provided. No more than one answer per page. Do not answer two questions on the same sheet of paper.
- 3. If you use more than one sheet of paper for a question, write "Page 1 of 2" and "Page 2 of 2."
- 4. Write ONLY on one side of each sheet. Use only pen. Answers in pencil will be disqualified.
- 5. Write ---- END ---- at the end of each answer.
- 6. Write your exam identification number in the upper right-hand corner of each sheet of paper.
- 7. Write the question number in the upper right-hand corner of each sheet of paper.

## Section 1: Microeconomic Theory—Answer Any Two Questions.

**1A**. (Liu) An American university has enough places for 9000 students. Government restrictions mean that at least 75% of the places must be given to US students but the remainder may be given to non-US citizens. There are 5000 residential places available on campus.

All overseas students and at least one-quarter of the US students must be given places on campus. The university get \$12000 in tuition fees for each US student and \$15000 for each overseas student. It wants to maximize the fees received.

Using the letter x for the number of places given to US students and y for the number of places for overseas students,

- (1) write down an expression for the objective function and state whether it is to be maximized or minimized;
- (2) write down the constraints that define the feasible region and explain your reasoning carefully;
- (3) identify which aspect of the original problem has been overlooked in parts (a) and (b);
- (4) graph the feasible region.

**1B**. (Hajikhameneh) Grace's preferences are described by the utility function  $U(x_1, x_2) = 2lnx_1 + 2lnx_2$ . Her income is *I* and prices of both good are  $p_1$  and  $p_2$ , respectively.

- i. Find her uncompensated demand functions for  $x_1^*$  and  $x_2^*$  using the Lagrangian method.
- ii. Derive Grace's indirect utility and expenditure functions.
- iii. Calculate the income and substitution effects for  $x_1$ .

**1C**. (Hajikhameneh) Find and describe the Bayesian–Nash equilibrium in the following game. There are two players in this game; Player 1 and 2. The top and bottom payoffs belong to Player 1 and Player 2, respectively.

